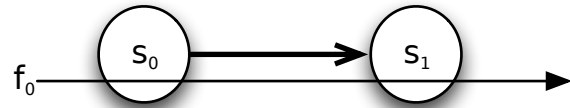


Tandem_1SC_1Flow



- $\beta_{s_0} = \beta_{s_1} = \beta_{R_{s_i}, T_{s_i}} = \beta_{10,10}, i \in \{0,1\}$
- $\mathcal{F} = \{f_0\}$
- $\alpha^{f_0} = \gamma_{r^{f_0}, b^{f_0}} = \gamma_{5,25}$

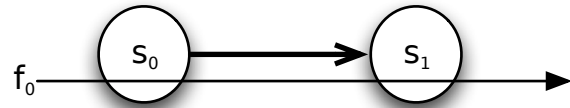
$\text{arrivalBound}(s_1, \{f_0\}, \mathcal{G}), \mathcal{G} \in \mathcal{P}(\mathcal{F}) = \alpha_{s_1}^{f_0}$		FIFO_MUX	ARB_MUX
$\alpha_{s_0}^{f_0}$		$= \gamma_{5,25}$	
$\alpha_{s_0}^{xf_0}$		$= \gamma_{0,0}$	
$\beta_{s_0}^{\text{l.o.}f_0} = \beta_{s_0} \ominus \alpha_{s_0}^{xf_0} = \beta_{R_{s_0}^{\text{l.o.}f_0}, T_{s_0}^{\text{l.o.}f_0}}$		$= \beta_{10,10}$	
$\alpha_{s_1}^{f_0} = \alpha^{f_0} \oslash \beta_{s_0}^{\text{l.o.}f_0} = \gamma_{r_{s_1}^{f_0}, b_{s_1}^{f_0}}$	$r_{s_1}^{f_0}$	$= 5$	
	$b_{s_1}^{f_0}$	$\alpha^{f_0}(T_{s_0}^{\text{l.o.}f_0}) = 5 \cdot 10 + 25 = 75$	
	$=$	$= \gamma_{5,75}$	

TFA		FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0} = \alpha_{s_0}^{f_0}$	$= \gamma_{5,25}$	
	$D_{s_0}^{f_0}$	$\beta_{s_0} = b_{s_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$	FIFO per micro flow $\beta_{s_0} = b_{s_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$
	$B_{s_0}^{f_0}$	$\alpha_{s_0}(T_{s_0}) = 5 \cdot 10 + 25$ $= 75$	
s_1	$\alpha_{s_1} = \alpha_{s_1}^{f_0}$	$= \gamma_{5,75}$	
	$D_{s_1}^{f_0}$	$\beta_{s_1} = b_{s_1}$ $10 \cdot [t - 10]^+ = 75$ $t = 17\frac{1}{2}$	FIFO per micro flow $\beta_{s_1} = b_{s_1}$ $10 \cdot [t - 10]^+ = 75$ $t = 17\frac{1}{2}$
	$B_{s_1}^{f_0}$	$\alpha_{s_1}(T_{s_1}) = 5 \cdot 10 + 75$ $= 125$	
D^{f_0}		$\sum_{i=0}^1 D_{s_i}^{f_0} = 30$	
B^{f_0}		$\max_{i=\{0,1\}} b_{s_i}^{f_0} = 125$	

SFA		FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0}^{xf_0}$	$= \gamma_{0,0}$	
	$\beta_{s_0}^{l.o.f_0} = \beta_{s_0} \ominus \alpha_{s_0}^{xf_0} = \beta_{s_0}$	$= \beta_{10,10}$	
s_1	$\alpha_{s_1}^{xf_0}$	$= \gamma_{0,0}$	
	$\beta_{s_1}^{l.o.f_0} = \beta_{s_1} \ominus \alpha_{s_1}^{xf_0} = \beta_{s_1}$	$= \beta_{10,10}$	
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$		$\bigotimes_{i=0}^1 \beta_{s_i}^{l.o.f_0} = \beta_{10,20}$	
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $10 \cdot [t - 20]^+ = 25$ $t = 22\frac{1}{2}$	
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 20 + 25$ $= 125$	

PMOO		ARB_MUX
s_0	$\alpha_{s_0}^{x'f_0}$	$= \gamma_{0,0}$
	$\alpha_{s_0}^{xf_0}$	$= \gamma_{0,0}$
s_1	$\alpha_{s_0}^{x'f_0}$	$= \gamma_{0,0}$
	$\alpha_{s_0}^{xf_0}$	$= \gamma_{0,0}$
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$	$R_{e2e}^{l.o.f_0} = \bigwedge_{i \in \{0,1\}} (R_{s_i} - r_{s_i}^{xf_0})$	$= (10 - 0) \wedge (10 - 0)$ $= 10$
	$T_{e2e}^{l.o.f_0} = \sum_{i \in \{0,1\}} T_{s_i} + \frac{\sum_{i \in \{0,1\}} (b_{s_i}^{x'f_0} + r_{s_i}^{xf_0} \cdot T_{s_i})}{R_{e2e}^{l.o.f_0}}$	$= 10 + 10 + \frac{0 + 0 \cdot 10 + 0 + 0 \cdot 10}{10}$ $= 20$
	$=$	$= \beta_{10,20}$
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $10 \cdot [t - 20]^+ = 25$ $t = 22\frac{1}{2}$
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 20 + 25$ $= 125$

Tandem_2SCs_1Flow



- $\beta_{s_0} = \beta_{R_{s_0}, T_{s_0}} = \beta_{10,10}$
- $\beta_{s_1} = \beta_{R_{s_1}, T_{s_1}} = \beta_{6,6}$
- $\mathcal{F} = \{f_0\}$
- $\alpha^{f_0} = \gamma_{r^{f_0}, b^{f_0}} = \gamma_{5,25}$

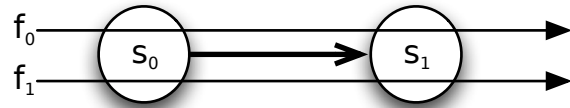
$\text{arrivalBound}(s_1, \{f_0\}, \mathcal{G}), \mathcal{G} \in \mathcal{P}(\mathcal{F}) = \alpha_{s_1}^{f_0}$		FIFO_MUX	ARB_MUX
$\alpha_{s_0}^{f_0}$		$= \gamma_{5,25}$	
$\alpha_{s_0}^{xf_0}$		$= \gamma_{0,0}$	
$\beta_{s_0}^{\text{l.o.}f_0} = \beta_{s_0} \ominus \alpha_{s_0}^{xf_0} = \beta_{R_{s_0}^{\text{l.o.}f_0}, T_{s_0}^{\text{l.o.}f_0}}$		$= \beta_{10,10}$	
$\alpha_{s_1}^{f_0} = \alpha^{f_0} \oslash \beta_{s_0}^{\text{l.o.}f_0} = \gamma_{r_{s_1}^{f_0}, b_{s_1}^{f_0}}$	$r_{s_1}^{f_0}$	$= 5$	
	$b_{s_1}^{f_0}$	$\alpha^{f_0}(T_{s_0}^{\text{l.o.}f_0}) = 5 \cdot 10 + 25 = 75$	
	$=$	$= \gamma_{5,75}$	

TFA		FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0} = \alpha_{s_0}^{f_0}$	$= \gamma_{5,25}$	
	$D_{s_0}^{f_0}$	$\beta_{s_0} = b_{s_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$	FIFO per micro flow $\beta_{s_0} = b_{s_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$
	$B_{s_0}^{f_0}$	$\alpha_{s_0}(T_{s_0}) = 5 \cdot 10 + 25$ $= 75$	
s_1	$\alpha_{s_1} = \alpha_{s_1}^{f_0}$	$= \gamma_{5,75}$	
	$D_{s_1}^{f_0}$	$\beta_{s_1} = b_{s_1}$ $6 \cdot [t - 6]^+ = 75$ $t = 18\frac{1}{2}$	FIFO per micro flow $\beta_{s_1} = b_{s_1}$ $6 \cdot [t - 6]^+ = 75$ $t = 18\frac{1}{2}$
	$B_{s_1}^{f_0}$	$\alpha_{s_1}(T_{s_1}) = 5 \cdot 6 + 75$ $= 105$	
D^{f_0}		$\sum_{i=0}^1 D_{s_i}^{f_0} = 31$	
B^{f_0}		$\max_{i=\{0,1\}} b_{s_i}^{f_0} = 105$	

SFA		FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0}^{xf_0}$	$= \gamma_{0,0}$	
	$\beta_{s_0}^{l.o.f_0} = \beta_{s_0} \ominus \alpha_{s_0}^{xf_0} = \beta_{s_0}$	$= \beta_{10,10}$	
$\text{TODO}_{s_0 s_1}$	$\alpha_{s_0 s_1}^{xf_0}$	$= \gamma_{0,0}$	
s_1	$\alpha_{s_1}^{xf_0} = \alpha_{s_0 s_1}^{xf_0}$	$= \gamma_{0,0}$	
	$\beta_{s_1}^{l.o.f_0} = \beta_{s_1} \ominus \alpha_{s_1}^{xf_0} = \beta_{s_1}$	$= \beta_{6,6}$	
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$		$\bigotimes_{i=0}^1 \beta_{s_i}^{l.o.f_0} = \beta_{6,16}$	
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $6 \cdot [t - 16]^+ = 25$ $t = 20\frac{1}{6}$	
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 16 + 25$ $= 105$	

PMOO		ARB_MUX
s_0	$\alpha_{s_0}^{x'f_0}$	$= \gamma_{0,0}$
	$\alpha_{s_0}^{xf_0}$	$= \gamma_{0,0}$
s_1	$\alpha_{s_1}^{x'f_0}$	$= \gamma_{0,0}$
	$\alpha_{s_0}^{xf_0}$	$= \gamma_{0,0}$
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$	$R_{e2e}^{l.o.f_0} = \bigwedge_{i \in \{0,1\}} (R_{s_i} - r_{s_i}^{xf_0})$	$= (10 - 0) \wedge (6 - 0)$ $= 6$
	$T_{e2e}^{l.o.f_0} = \sum_{i \in \{0,1\}} T_{s_i} + \frac{\sum_{i \in \{0,1\}} (b_{s_i}^{x'f_0} + r_{s_i}^{xf_0} \cdot T_{s_i})}{R_{e2e}^{l.o.f_0}}$	$= 10 + 6 + \frac{0 + 0 \cdot 10 + 0 + 0 \cdot 6}{6}$ $= 16$
	$=$	$= \beta_{6,16}$
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $6 \cdot [t - 16]^+ = 25$ $t = 20\frac{1}{6}$
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 16 + 25$ $= 105$

Tandem_1SC_2Flows_1AC_1Path



- $\beta_{s_0} = \beta_{s_1} = \beta_{R_{s_i}, T_{s_i}} = \beta_{10,10}, i \in \{0,1\}$
- $\mathcal{F} = \{f_0, f_1\}$
- $\alpha^{f_0} = \alpha^{f_1} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}, j \in \{0,1\}$

$\text{arrivalBound}(s_1, \{f_0\}, \{f_1\}) = \alpha_{s_1}^{f_0}$ $= \text{arrivalBound}(s_1, \{f_1\}, \{f_0\}) = \alpha_{s_1}^{f_1}$		FIFO_MUX	ARB_MUX
$\alpha_{s_0}^{f_j}$		$= \gamma_{5,25}$	
$\alpha_{s_0}^{xf_j}$		$= \gamma_{0,0}$	
$\beta_{s_0}^{\text{l.o.}f_j} = \beta_{s_0} \ominus \alpha_{s_0}^{xf_j} = \beta_{R_{s_0}^{\text{l.o.}f_j}, T_{s_0}^{\text{l.o.}f_j}}$		$= \beta_{10,10}$	
$\alpha_{s_1}^{f_j} = \alpha_{s_0}^{f_j} \oslash \beta_{s_0}^{\text{l.o.}f_j} = \gamma_{r_{s_1}^{f_j}, b_{s_1}^{f_j}}$	$r_{s_1}^{f_j}$	$= 5$	
	$b_{s_1}^{f_j}$	$\alpha^{f_0}(T_{s_0}^{\text{l.o.}f_0}) = 5 \cdot 10 + 25 = 75$	
	$=$	$= \gamma_{5,75}$	

$\text{arrivalBound}(s_1, \{f_0, f_1\}, \{\}) = \alpha_{s_1}^{\{f_0, f_1\}}$		FIFO_MUX	ARB_MUX
$\alpha_{s_0}^{\{f_0, f_1\}}$		$= \gamma_{10,50}$	
$\alpha_{s_0}^{x\{f_0, f_1\}}$		$= \gamma_{0,0}$	
$\beta_{s_0}^{\text{l.o.}\{f_0, f_1\}} = \beta_{s_0} \ominus \alpha_{s_0}^{x\{f_0, f_1\}} = \beta_{R_{s_0}^{\text{l.o.}\{f_0, f_1\}}, T_{s_0}^{\text{l.o.}\{f_0, f_1\}}}$		$= \beta_{10,10}$	
$\alpha_{s_1}^{\{f_0, f_1\}} = \alpha_{s_0}^{\{f_0, f_1\}} \oslash \beta_{s_0}^{\text{l.o.}\{f_0, f_1\}} = \gamma_{r_{s_1}^{\{f_0, f_1\}}, b_{s_1}^{\{f_0, f_1\}}}$	$r_{s_1}^{\{f_0, f_1\}}$	$= 10$	
	$b_{s_1}^{\{f_0, f_1\}}$	$\alpha_{s_0}^{\{f_0, f_1\}}(T_{s_0}^{\text{l.o.}\{f_0, f_1\}}) = 10 \cdot 10 + 50 = 150$	
	$=$	$= \gamma_{10,150}$	

Flows $f_j, j \in \{0, 1\}$

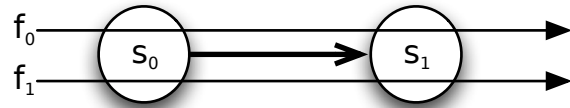
TFA results will be equal for all flows as they share the same path of servers.

TFA		FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0} = \alpha^{f_0} + \alpha^{f_1}$	$= \gamma_{10,50}$	
	$D_{s_0}^{f_j}$	$\beta_{s_0} = b_{s_0}$ $10 \cdot [t - 10]^+ = 50$ $t = 15$	$\beta_{s_0} = \alpha_{s_0}$ $10 \cdot [t - 10]^+ = 10 \cdot t + 50$ $0 \cdot t = 150$ $\Rightarrow D_{s_0}^{f_j} = \infty$
	$B_{s_0}^{f_j}$	$\alpha_{s_0}(T_{s_0}) = 10 \cdot 10 + 50$ $= 150$	
s_1	$\alpha_{s_1} = \alpha_{s_1}^{\{f_0, f_1\}}$	$= \gamma_{10,150}$	
	$D_{s_1}^{f_j}$	$\beta_{s_1} = b_{s_1}$ $10 \cdot [t - 10]^+ = 150$ $t = 25$	$\beta_{s_1} = \alpha_{s_1}$ $10 \cdot [t - 10]^+ = 10 \cdot t + 150$ $0 \cdot t = 250$ $\Rightarrow D_{s_1}^{f_j} = \infty$
	$B_{s_1}^{f_j}$	$\alpha_{s_1}(T_{s_1}) = 10 \cdot 10 + 150$ $= 250$	
D^{f_j}		$\sum_{i=0}^1 D_{s_i}^{f_j} = 40$	$\sum_{i=0}^1 D_{s_i}^{f_j} = \infty$
B^{f_j}		$\max_{i=\{0,1\}} b_{s_i}^{f_j} = 250$	

SFA			FIFO_MUX	ARB_MUX
s0	$\alpha_{s_0}^{xf_j}$		$= \gamma_{5,25}$	
	$\beta_{s_0}^{l.o.f_j} = \beta_{s_0} \ominus \alpha_{s_0}^{xf_i}$	$R_{s_0}^{l.o.f_j}$	$= 5$	
		$T_{s_0}^{l.o.f_j}$	$\beta_{s_0} = b_{s_0}^{xf_j}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$	$\beta_{s_0} = \alpha_{s_0}^{xf_j}$ $10 \cdot [t - 10]^+ = 5 \cdot t + 25$ $t = 25$
		$=$	$= \beta_{5,12\frac{1}{2}}$	$= \beta_{5,25}$
s1	$\alpha_{s_1}^{xf_j}$		$= \gamma_{5,75}$	
	$\beta_{s_1}^{l.o.f_j} = \beta_{s_1} \ominus \alpha_{s_1}^{xf_j}$	$R_{s_1}^{l.o.f_j}$	$= 5$	
		$T_{s_1}^{l.o.f_j}$	$\beta_{s_1} = b_{s_1}^{xf_j}$ $10 \cdot [t - 10]^+ = 75$ $t = 17\frac{1}{2}$	$\beta_{s_1} = \alpha_{s_1}^{xf_j}$ $10 \cdot [t - 10]^+ = 5 \cdot t + 75$ $t = 35$
		$=$	$= \beta_{5,17\frac{1}{2}}$	$= \beta_{5,35}$
$\beta_{e2e}^{l.o.f_j} = \beta_{R_{e2e}^{l.o.f_j}, T_{e2e}^{l.o.f_j}}$		$\bigotimes_{i=0}^1 \beta_{s_i}^{l.o.f_j} = \beta_{5,30}$	$\bigotimes_{i=0}^1 \beta_{s_i}^{l.o.f_j} = \beta_{5,60}$	
D^{f_j}		$\beta_{e2e}^{l.o.f_j} = b^{f_j}$ $5 \cdot [t - 30]^+ = 25$ $t = 35$	$\beta_{e2e}^{l.o.f_j} = b^{f_j}$ $5 \cdot [t - 60]^+ = 25$ $t = 65$	
B^{f_j}		$\alpha^{f_j}(T_{e2e}^{l.o.f_j}) = 5 \cdot 30 + 25$ $= 175$	$\alpha^{f_j}(T_{e2e}^{l.o.f_j}) = 5 \cdot 60 + 25$ $= 325$	

PMOO		ARB_MUX
s_0	$\alpha_{s_0}^{x'f_j}$	$= \gamma_{5,25}$
	$\alpha_{s_0}^{xf_j}$	$= \gamma_{5,25}$
s_1	$\alpha_{s_1}^{x'f_j}$	$= \gamma_{0,0}$
	$\alpha_{s_1}^{xf_j}$	$= \gamma_{5,75}$
$\beta_{e2e}^{l.o.f_j} = \beta_{R_{e2e}^{l.o.f_j}, T_{e2e}^{l.o.f_j}}$	$R_{e2e}^{l.o.f_j} = \bigwedge_{i \in \{0,1\}} (R_{s_i} - r_{s_i}^{xf_j})$	$= (10 - 5) \wedge (10 - 5)$
		$= 5$
	$T_{e2e}^{l.o.f_j} = \sum_{i \in \{0,1\}} T_{s_i} + \frac{\sum_{i \in \{0,1\}} (b_{s_i}^{x'f_j} + r_{s_i}^{xf_j} \cdot T_{s_i})}{R_{e2e}^{l.o.f_j}}$	$= 10 + 10 + \frac{25 + 5 \cdot 10 + 0 + 5 \cdot 10}{5}$
		$= 45$
	$=$	$= \beta_{5,45}$
D^{f_j}		$\beta_{e2e}^{l.o.f_j} = b^{f_j}$ $5 \cdot [t - 45]^+ = 25$ $t = 50$
B^{f_j}		$\alpha^{f_j}(T_{e2e}^{l.o.f_j}) = 5 \cdot 45 + 25$ $= 250$

Tandem_2SCs_2Flows_1AC_1Path



- $\beta_{s_0} = \beta_{R_{s_0}, T_{s_0}} = \beta_{10,10}$
- $\beta_{s_1} = \beta_{R_{s_1}, T_{s_1}} = \beta_{6,6}$
- $\mathcal{F} = \{f_0, f_1\}$
- $\alpha^{f_0} = \alpha^{f_1} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{2\frac{1}{2}, 12\frac{1}{2}}, j \in \{0, 1\}$

$\text{arrivalBound}(s_1, \{f_0\}, \{f_1\}) = \alpha_{s_1}^{f_0}$ $= \text{arrivalBound}(s_1, \{f_1\}, \{f_0\}) = \alpha_{s_1}^{f_1}$		FIFO_MUX	ARB_MUX
$\alpha_{s_0}^{f_j}$		$= \gamma_{2\frac{1}{2}, 12\frac{1}{2}}$	
$\alpha_{s_0}^{xf_j}$		$= \gamma_{0,0}$	
$\beta_{s_0}^{\text{l.o.}f_j} = \beta_{s_0} \ominus \alpha_{s_0}^{xf_j} = \beta_{R_{s_0}^{\text{l.o.}f_j}, T_{s_0}^{\text{l.o.}f_j}}$		$= \beta_{10,10}$	
$\alpha_{s_1}^{f_j} = \alpha_{s_0}^{f_j} \oslash \beta_{s_0}^{\text{l.o.}f_j} = \gamma_{r_{s_1}^{f_j}, b_{s_1}^{f_j}}$	$r_{s_1}^{f_j}$	$= 2\frac{1}{2}$	
	$b_{s_1}^{f_j}$	$\alpha_{s_0}^{f_j}(T_{s_0}^{\text{l.o.}f_j}) = 2\frac{1}{2} \cdot 10 + 12\frac{1}{2} = 37\frac{1}{2}$	
	$=$	$= \gamma_{2\frac{1}{2}, 37\frac{1}{2}}$	

$\text{arrivalBound}(s_1, \{f_0, f_1\}, \{\}) = \alpha_{s_1}^{\{f_0, f_1\}}$		FIFO_MUX	ARB_MUX
$\alpha_{s_0}^{\{f_0, f_1\}}$		$= \gamma_{5,25}$	
$\alpha_{s_0}^{x\{f_0, f_1\}}$		$= \gamma_{0,0}$	
$\beta_{s_0}^{\text{l.o.}\{f_0, f_1\}} = \beta_{s_0} \ominus \alpha_{s_0}^{x\{f_0, f_1\}} = \beta_{R_{s_0}^{\text{l.o.}\{f_0, f_1\}}, T_{s_0}^{\text{l.o.}\{f_0, f_1\}}}$		$= \beta_{10,10}$	
$\alpha_{s_1}^{\{f_0, f_1\}} = \alpha_{s_0}^{\{f_0, f_1\}} \oslash \beta_{s_0}^{\text{l.o.}\{f_0, f_1\}} = \gamma_{r_{s_1}^{\{f_0, f_1\}}, b_{s_1}^{\{f_0, f_1\}}}$	$r_{s_1}^{\{f_0, f_1\}}$	$= 5$	
	$b_{s_1}^{\{f_0, f_1\}}$	$\alpha_{s_0}^{\{f_0, f_1\}}(T_{s_0}^{\text{l.o.}\{f_0, f_1\}}) = 5 \cdot 10 + 25 = 75$	
	$=$	$= \gamma_{5,75}$	

Flows $f_j, j \in \{0, 1\}$

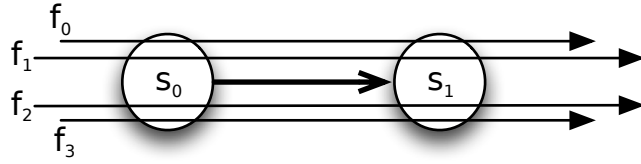
TFA results will be equal for all flows as they share the same path of servers.

TFA		FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0} = \alpha^{f_0} + \alpha^{f_1}$	$= \gamma_{5,25}$	
	$D_{s_0}^{f_j}$	$\beta_{s_0} = b_{s_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$	$\beta_{s_0} = \alpha_{s_0}$ $10 \cdot [t - 10]^+ = 5 \cdot t + 25$ $t = 25$
	$B_{s_0}^{f_j}$	$\alpha_{s_0}(T_{s_0}) = 5 \cdot 10 + 25$ $= 75$	
s_1	$\alpha_{s_1} = \alpha_{s_1}^{\{f_0, f_1\}}$	$= \gamma_{5,75}$	
	$D_{s_1}^{f_j}$	$\beta_{s_1} = b_{s_1}$ $6 \cdot [t - 6]^+ = 75$ $t = 18\frac{1}{2}$	$\beta_{s_1} = \alpha_{s_1}$ $6 \cdot [t - 6]^+ = 5 \cdot t + 75$ $t = 111$
	$B_{s_1}^{f_j}$	$\alpha_{s_1}(T_{s_1}) = 5 \cdot 6 + 75$ $= 105$	
D^{f_j}		$\sum_{i=0}^1 D_{s_i}^{f_j} = 31$	$\sum_{i=0}^1 D_{s_i}^{f_j} = 136$
B^{f_j}		$\max_{i=\{0,1\}} b_{s_i}^{f_j} = 105$	

SFA			FIFO_MUX	ARB_MUX
s ₀	α ^{xf_j} _{s₀}		= γ _{2½,12½}	
	β ^{l.o.f_j} _{s₀} = β _{s₀} ⊖ α ^{xf_j} _{s₀}	R ^{l.o.f_j} _{s₀}	= 7½	
		T ^{l.o.f_j} _{s₀}	β _{s₀} = b ^{xf_j} _{s₀} 10 · [t − 10] ⁺ = 12½ t = 11¼	β _{s₀} = α ^{xf_j} _{s₀} 10 · [t − 10] ⁺ = 2½ · t + 12½ t = 15
		=	= β _{7½,11¼}	
s ₁	α ^{xf_j} _{s₁}		= γ _{2½,37½}	
	β ^{l.o.f_j} _{s₁} = β _{s₁} ⊖ α ^{xf_j} _{s₁}	R ^{l.o.f_j} _{s₁}	= 3½	
		T ^{l.o.f_j} _{s₁}	β _{s₁} = b ^{xf_j} _{s₁} 6 · [t − 6] ⁺ = 37½ t = 12¼	β _{s₁} = α ^{xf_j} _{s₁} 6 · [t − 6] ⁺ = 2½ · t + 37½ t = 21
		=	= β _{3½,12¼}	
β ^{l.o.f_j} _{e2e} = β _{R^{l.o.f_j}_{e2e}, T^{l.o.f_j}_{e2e}}		⊗ ¹ _{i=0} β ^{l.o.f_j} _{s_i} = β _{3½,23½}	⊗ ¹ _{i=0} β ^{l.o.f_j} _{s_i} = β _{3½,36}	
D ^{f_j}		β ^{l.o.f_j} _{e2e} = b ^{f_j} 3½ · [t − 23½] ⁺ = 12½ t = 27¼	β ^{l.o.f_j} _{e2e} = b ^{f_j} 3½ · [t − 36] ⁺ = 12½ t = 39⅔	
B ^{f_j}		α ^{f_j} (T ^{l.o.f_j} _{e2e}) = 2½ · 23½ + 12½ = 71¼	α ^{f_j} (T ^{l.o.f_j} _{e2e}) = 2½ · 36 + 12½ = 102½	

PMOO		ARB_MUX
s_0	$\alpha_{s_0}^{x'f_j}$	$= \gamma_{2\frac{1}{2}, 12\frac{1}{2}}$
	$\alpha_{s_0}^{xf_j}$	$= \gamma_{2\frac{1}{2}, 12\frac{1}{2}}$
s_1	$\alpha_{s_1}^{x'f_j}$	$= \gamma_{0,0}$
	$\alpha_{s_1}^{xf_j}$	$= \gamma_{2\frac{1}{2}, 37\frac{1}{2}}$
$\beta_{e2e}^{l.o.f_j} = \beta_{R_{e2e}^{l.o.f_j}, T_{e2e}^{l.o.f_j}}$	$R_{e2e}^{l.o.f_j} = \bigwedge_{i \in \{0,1\}} (R_{s_i} - r_{s_i}^{xf_j})$	$= (10 - 2\frac{1}{2}) \wedge (6 - 2\frac{1}{2})$
		$= 3\frac{1}{2}$
	$T_{e2e}^{l.o.f_j} = \sum_{i \in \{0,1\}} T_{s_i} + \frac{\sum_{i \in \{0,1\}} (b_{s_i}^{x'f_j} + r_{s_i}^{xf_j} \cdot T_{s_i})}{R_{e2e}^{l.o.f_j}}$	$= 6 + 10 + \frac{12\frac{1}{2} + 2\frac{1}{2} \cdot 10 + 0 + 2\frac{1}{2} \cdot 10}{3\frac{1}{2}}$
	$=$	$= 31$
		$= \beta_{3\frac{1}{2}, 31}$
Df_j		$\beta_{e2e}^{l.o.f_j} = b^{f_j}$ $3\frac{1}{2} \cdot [t - 31]^+ = 12\frac{1}{2}$ $t = 34\frac{4}{7}$
Bf_j		$\alpha^{f_j}(T_{e2e}^{l.o.f_j}) = 2\frac{1}{2} \cdot 31 + 12\frac{1}{2}$ $= 90$

Tandem_1SCs_4Flows_1ACs_1Path



- $\beta_{s_0} = \beta_{s_1} = \beta_{R_{s_i}, T_{s_i}} = \beta_{10,10}, i \in \{0,1\}$
- $\mathcal{F} = \{f_0, f_1, f_2, f_3\}$
- $\alpha^{f_j} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{2,10}, j \in \{0,1,2,3\}$

$\text{arrivalBound}(s_1, xf_j, \{f_j\}) = \alpha_{s_1}^{xf_j}, j \in \{0, 1, 2, 3\}$		FIFO_MUX	ARB_MUX
$\alpha_{s_0}^{xf_j}$		$= \gamma_{6,30}$	
$\alpha_{s_0}^{xxf_j}$		$= \gamma_{0,0}$	
$\beta_{s_0}^{\text{l.o.}xf_j} = \beta_{s_0} \ominus \alpha_{s_0}^{xxf_j} = \beta_{R_{s_0}^{\text{l.o.}xf_j}, T_{s_0}^{\text{l.o.}xf_j}}$		$= \beta_{10,10}$	
$\alpha_{s_1}^{xf_j} = \alpha_{s_0}^{xf_j} \oslash \beta_{s_0}^{\text{l.o.}xf_j} = \gamma_{r_{s_1}^{xf_j}, b_{s_1}^{xf_j}}$	$r_{s_1}^{xf_j}$	$= 6$	
	$b_{s_1}^{xf_j}$	$\alpha_{s_0}^{xf_j}(T_{s_0}^{\text{l.o.}xf_j}) = 6 \cdot 10 + 30 = 90$	
	$=$	$= \gamma_{6,90}$	

$\text{arrivalBound}(s_1, \{f_0, f_1, f_2, f_3\}, \{\}) = \alpha_{s_1}^{\{f_0, f_1, f_2, f_3\}}$		FIFO_MUX	ARB_MUX
$\alpha_{s_0}^{\{f_0, f_1, f_2, f_3\}}$		$= \gamma_{8,40}$	
$\alpha_{s_0}^{x\{f_0, f_1, f_2, f_3\}}$		$= \gamma_{0,0}$	
$\beta_{s_0}^{\text{l.o.}\{f_0, f_1, f_2, f_3\}} = \beta_{s_0} \ominus \alpha_{s_0}^{x\{f_0, f_1, f_2, f_3\}} = \beta_{R_{s_0}^{\text{l.o.}\{f_0, f_1, f_2, f_3\}}, T_{s_0}^{\text{l.o.}\{f_0, f_1, f_2, f_3\}}}$		$= \beta_{10,10}$	
$\alpha_{s_1}^{\{f_0, f_1, f_2, f_3\}} = \alpha_{s_0}^{\{f_0, f_1, f_2, f_3\}} \oslash \beta_{s_0}^{\text{l.o.}\{f_0, f_1, f_2, f_3\}} = \gamma_{r_{s_1}^{\{f_0, f_1, f_2, f_3\}}, b_{s_1}^{\{f_0, f_1, f_2, f_3\}}}$	$r_{s_1}^{\{f_0, f_1, f_2, f_3\}}$	$= 8$	
	$b_{s_1}^{\{f_0, f_1, f_2, f_3\}}$	$\alpha_{s_0}^{\{f_0, f_1, f_2, f_3\}}(T_{s_0}^{\text{l.o.}\{f_0, f_1, f_2, f_3\}}) = 8 \cdot 10 + 40 = 120$	
	$=$	$= \gamma_{8,120}$	

Flows $f_j, j \in \{0, 1, 2, 3\}$

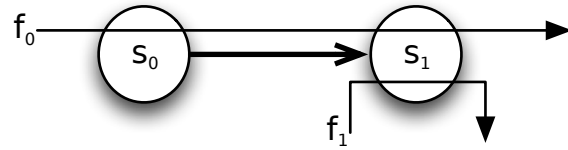
TFA results will be equal for all flows as they share the same path of servers.

TFA		FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0} = \sum_{j=0}^3 \alpha^{f_j}$	$= \gamma_{8,40}$	
	$D_{s_0}^{f_j}$	$\beta_{s_0} = b_{s_0}$ $10 \cdot [t - 10]^+ = 40$ $t = 14$	$\beta_{s_0} = \alpha_{s_0}$ $10 \cdot [t - 10]^+ = 8 \cdot t + 40$ $t = 70$
	$B_{s_0}^{f_j}$	$\alpha_{s_0}(T_{s_0}) = 8 \cdot 10 + 40$ $= 120$	
s_1	$\alpha_{s_1} = \alpha_{s_1}^{\{f_0, f_1, f_2, f_3\}}$	$= \gamma_{8,120}$	
	$D_{s_1}^{f_j}$	$\beta_{s_1} = b_{s_1}$ $10 \cdot [t - 10]^+ = 120$ $t = 22$	$\beta_{s_1} = \alpha_{s_1}$ $10 \cdot [t - 10]^+ = 8 \cdot t + 120$ $t = 110$
	$B_{s_1}^{f_j}$	$\alpha_{s_1}(T_{s_1}) = 8 \cdot 10 + 120$ $= 200$	
D^{f_j}		$\sum_{i=0}^1 D_{s_i}^{f_j} = 36$	$\sum_{i=0}^1 D_{s_i}^{f_j} = 180$
B^{f_j}		$\max_{i=\{0,1\}} b_{s_i}^{f_j} = 200$	

SFA		FIFO_MUX	ARB_MUX	
s ₀	$\alpha_{s_0}^{xf_j} = \sum_{k=0}^2 \alpha^{f_k}$		$= \gamma_{6,30}$	
	$\beta_{s_0}^{l.o.f_j} = \beta_{s_0} \ominus \alpha_{s_0}^{xf_j}$	$R_{s_0}^{l.o.f_j}$	$= 4$	
		$T_{s_0}^{l.o.f_j}$	$\beta_{s_0} = b_{s_0}^{xf_j}$ $10 \cdot [t - 10]^+ = 30$ $t = 13$	$\beta_{s_0} = \alpha_{s_0}^{xf_j}$ $10 \cdot [t - 10]^+ = 6 \cdot t + 30$ $t = 32\frac{1}{2}$
		$=$	$= \beta_{4,13}$	$= \beta_{4,32\frac{1}{2}}$
s ₁	$\alpha_{s_1}^{xf_j} = \alpha_{s_1}^{xf_j}$		$= \gamma_{6,90}$	
	$\beta_{s_1}^{l.o.f_j} = \beta_{s_1} \ominus \alpha_{s_1}^{xf_j}$	$R_{s_1}^{l.o.f_j}$	$= 4$	
		$T_{s_1}^{l.o.f_j}$	$\beta_{s_1} = b_{s_1}^{xf_j}$ $10 \cdot [t - 10]^+ = 90$ $t = 19$	$\beta_{s_1} = \alpha_{s_1}^{xf_j}$ $10 \cdot [t - 10]^+ = 4 \cdot t + 90$ $t = 47\frac{1}{2}$
		$=$	$= \beta_{4,19}$	$= \beta_{4,47\frac{1}{2}}$
$\beta_{e2e}^{l.o.f_j}$		$\bigotimes_{i=0}^1 \beta_{s_i}^{l.o.f_j} = \beta_{4,32}$	$\bigotimes_{i=0}^1 \beta_{s_i}^{l.o.f_j} = \beta_{4,80}$	
D^{f_j}		$\beta_{e2e}^{l.o.f_j} = b^{f_j}$ $4 \cdot [t - 32]^+ = 10$ $t = 34\frac{1}{2}$	$\beta_{e2e}^{l.o.f_j} = b^{f_j}$ $4 \cdot [t - 80]^+ = 10$ $t = 82\frac{1}{2}$	
B^{f_j}		$\alpha^{f_j}(T_{e2e}^{l.o.f_j}) = 2 \cdot 32 + 10$ $= 74$	$\alpha^{f_j}(T_{e2e}^{l.o.f_j}) = 2 \cdot 80 + 10$ $= 170$	

PMOO		ARB_MUX
s_0	$\alpha_{s_0}^{x'f_j}$	$= \gamma_{6,30}$
	$\alpha_{s_0}^{xf_j}$	$= \gamma_{6,30}$
s_1	$\alpha_{s_1}^{x'f_j}$	$= \gamma_{0,0}$
	$\alpha_{s_1}^{xf_j}$	$= \gamma_{6,XXX}$ TODO: see SFA
$\beta_{e2e}^{l.o.f_j} = \beta_{R_{e2e}^{l.o.f_j}, T_{e2e}^{l.o.f_j}}$	$R_{e2e}^{l.o.f_j} = \bigwedge_{i \in \{0,1\}} \left(R_{s_i} - r_{s_i}^{xf_j} \right)$	$= (10 - 6) \wedge (10 - 6)$
	$T_{e2e}^{l.o.f_j} = \sum_{i \in \{0,1\}} T_{s_i} + \frac{\sum_{i \in \{0,1\}} \left(b_{s_i}^{x'f_j} + r_{s_i}^{xf_j} \cdot T_{s_i} \right)}{R_{e2e}^{l.o.f_j}}$	$= 10 + 10 + \frac{30 + 6 \cdot 10 + 0 + 6 \cdot 10}{4}$
	$=$	$= 37\frac{1}{2}$
D^{f_j}		$\beta_{e2e}^{l.o.f_j} = b^{f_j}$
		$4 \cdot [t - 57\frac{1}{2}]^+ = 10$
		$t = 60$
B^{f_j}		$\alpha^{f_j}(T_{e2e}^{l.o.f_j}) = 2 \cdot 57\frac{1}{2} + 10$
		$= 125$

Tandem_1SC_2Flows_1AC_2Paths



- $\beta_{s_0} = \beta_{s_1} = \beta_{R_{s_i}, T_{s_i}} = \beta_{20,20}, i \in \{0,1\}$
- $\mathcal{F} = \{f_0, f_1\}$
- $\alpha^{f_0} = \alpha^{f_1} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}, j \in \{0,1\}$

arrivalBound($s_1, \{f_0\}, \mathcal{G}$) $\mathcal{G} = \mathcal{P}(\mathcal{F}) = \alpha_{s_1}^{f_0}$		FIFO_MUX	ARB_MUX
$\alpha_{s_0}^{f_0}$		$= \gamma_{5,25}$	
$\alpha_{s_0}^{xf_0}$		$= \gamma_{0,0}$	
$\beta_{s_0}^{l.o.f_0} = \beta_{s_0} \ominus \alpha_{s_0}^{xf_0} = \beta_{R_{s_0}^{l.o.f_0}, T_{s_0}^{l.o.f_0}}$		$= \beta_{10,10}$	
$\alpha_{s_1}^{f_0} = \alpha_{s_0}^{f_0} \oslash \beta_{s_0}^{l.o.f_0} = \gamma_{r_{s_1}^{f_0}, b_{s_1}^{f_0}}$	$r_{s_1}^{f_0}$	$= 5$	
	$b_{s_1}^{f_0}$	$\alpha^{f_0}(T_{s_0}^{l.o.f_0}) = 5 \cdot 10 + 25 = 125$	
	$=$	$= \gamma_{5,125}$	

Flow f_0

TFA		FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0} = \alpha^{f_0}$	$= \gamma_{5,25}$	
	$D_{s_0}^{f_0}$	$\beta_{s_0} = b^{f_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$	FIFO per micro flow $\beta_{s_0} = b^{f_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$
	$B_{s_0}^{f_0}$	$\alpha_{s_0}(T_{s_0}) = 5 \cdot 20 + 25$ $= 125$	
s_1	$\alpha_{s_1} = \alpha_{s_1}^{f_0}$	$= \gamma_{5,25} + \gamma_{5,125} = \gamma_{10,150}$	
	$D_{s_1}^{f_0}$	$\beta_{s_1} = b_{s_1}$ $20 \cdot [t - 20]^+ = 150$ $t = 27\frac{1}{2}$	$\beta_{s_1} = \alpha_{s_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 150$ $t = 55$
	$B_{s_1}^{f_0}$	$\alpha_{s_1}(T_{s_1}) = 10 \cdot 20 + 150$ $= 350$	
D^{f_0}		$\sum_{i=0}^1 D_{s_i}^{f_0} = 48\frac{3}{4}$	$\sum_{i=0}^1 D_{s_i}^{f_0} = 76\frac{1}{4}$
B^{f_0}		$\max_{i=\{0,1\}} b_{s_i}^{f_0} = 350$	

SFA		FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0}^{xf_0}$	$= \gamma_{0,0}$	
	$\beta_{s_0}^{l.o.f_0} = \beta_{s_0}$	$= \beta_{20,20}$	
s_1	$\alpha_{s_1}^{xf_0} = \alpha_{s_1}^{f_1}$		$= \gamma_{5,25}$
	$\beta_{s_1}^{l.o.f_0} = \beta_{s_1} \ominus \alpha_{s_1}^{xf_0}$	$R_{s_1}^{l.o.f_0}$	$= 15$
		$\beta_{s_1} = b_{s_1}^{xf_0}$	$\beta_{s_1} = \alpha_{s_1}^{xf_0}$
		$20 \cdot [t - 20]^+ = 25$	$20 \cdot [t - 20]^+ = 5 \cdot t + 25$
		$t = 21\frac{1}{4}$	$t = 28\frac{1}{3}$
		$=$	$= \beta_{15,21\frac{1}{4}}$
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$		$\bigotimes_{i=0}^1 \beta_{s_i}^{l.o.f_0} = \beta_{15,41\frac{1}{4}}$	$\bigotimes_{i=0}^1 \beta_{s_i}^{l.o.f_0} = \beta_{15,48\frac{1}{3}}$
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$	$\beta_{e2e}^{l.o.f_0} = b^{f_0}$
		$15 \cdot [t - 41\frac{1}{4}]^+ = 25$	$15 \cdot [t - 48\frac{1}{3}]^+ = 25$
		$t = 42\frac{11}{12}$	$t = 50$
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 41\frac{1}{4} + 25$	$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 48\frac{1}{3} + 25$
		$= 231\frac{1}{4}$	$= 266\frac{2}{3}$

PMOO		ARB_MUX
s_0	$\alpha_{s_0}^{x'f_0}$	$= \gamma_{0,0}$
	$\alpha_{s_0}^{xf_0}$	$= \gamma_{0,0}$
s_1	$\alpha_{s_1}^{x'f_0}$	$= \gamma_{5,25}$
	$\alpha_{s_1}^{xf_0}$	$= \gamma_{5,25}$
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$	$R_{e2e}^{l.o.f_0} = \bigwedge_{i \in \{0,1\}} (R_{s_i} - r_{s_i}^{xf_0})$	$= (20 - 5) \wedge (20 - 5)$
		$= 15$
	$T_{e2e}^{l.o.f_0} = \sum_{i \in \{0,1\}} T_{s_i} + \frac{\sum_{i \in \{0,1\}} (b_{s_i}^{x'f_0} + r_{s_i}^{xf_0} \cdot T_{s_i})}{R_{e2e}^{l.o.f_0}}$	$= 20 + 20 + \frac{0 + 0 \cdot 20 + 25 + 5 \cdot 20}{15}$
	$=$	$= 48\frac{1}{3}$
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$
		$15 \cdot [t - 48\frac{1}{3}]^+ = 25$
		$t = 50$
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 48\frac{1}{3} + 25$
		$= 266\frac{2}{3}$

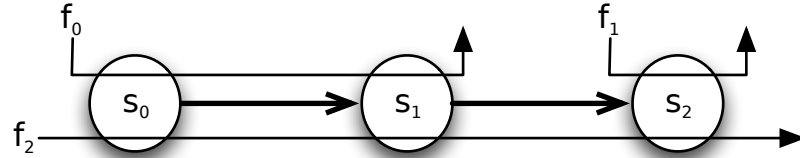
Flow f_1

TFA		FIFO_MUX	ARB_MUX
s_1	$\alpha_{s_1} = \alpha_{s_1}^{f_1} + \alpha_{s_1}^{f_0}$	$= \gamma_{5,25} + \gamma_{5,125} = \gamma_{10,150}$	
	$D_{s_1}^{f_1}$	$\beta_{s_1} = b_{s_1}$ $20 \cdot [t - 20]^+ = 150$ $t = 27\frac{1}{2}$	$\beta_{s_1} = \alpha_{s_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 150$ $t = 55$
	$B_{s_1}^{f_1}$	$\alpha_{s_1}(T_{s_1}) = 10 \cdot 20 + 150$ $= 350$	
D^{f_1}		$\sum_{i=0}^1 D_{s_i}^{f_1} = 27\frac{1}{2}$	$\sum_{i=0}^1 D_{s_i}^{f_1} = 55$
B^{f_1}		$\max_{i=\{0,1\}} b_{s_i}^{f_1} = 350$	

SFA			FIFO_MUX	ARB_MUX
s ₁	α ^{xf₁} _{s₁} = α ^{f₀} _{s₁}		= γ _{5,125}	
	β ^{l.o.f₁} _{s₁} = β _{s₁} ⊖ α ^{xf₁} _{s₁} = β _{R^{l.o.f₁}_{s₁}, T^{l.o.f₁}_{s₁}}	R ^{l.o.f₁} _{s₁}	= 15	
		T ^{l.o.f₁} _{s₁}	$\beta_{s_1} = b_{s_1}^{xf_1}$ $20 \cdot [t - 20]^+ = 125$ $t = 26\frac{1}{4}$	$\beta_{s_1} = \alpha_{s_1}^{xf_1}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 125$ $t = 35$
		=	= β _{15,26¼}	
β ^{l.o.f₁} _{e2e} = β _{R^{l.o.f₁}_{e2e}, T^{l.o.f₁}_{e2e}}			⊗ ¹ _{i=0} β ^{l.o.f₁} _{s_i} = β _{15,26¼}	⊗ ¹ _{i=0} β ^{l.o.f₁} _{s_i} = β _{15,35}
D ^{f₁}			$\beta_{e2e}^{l.o.f_1} = b^{f_1}$ $15 \cdot [t - 26\frac{1}{4}]^+ = 25$ $t = 27\frac{11}{12}$	$\beta_{e2e}^{l.o.f_1} = b^{f_1}$ $15 \cdot [t - 35]^+ = 25$ $t = 36\frac{2}{3}$
B ^{f₁}			$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 26\frac{1}{4} + 25$ $= 156\frac{1}{4}$	$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 35 + 25$ $= 200$

PMOO		ARB_MUX
s_1	$\alpha_{s_1}^{x'f_1}$	$= \gamma_{5,125}$
	$\alpha_{s_1}^{xf_1}$	$= \gamma_{5,125}$
$\beta_{e2e}^{l.o.f_1} = \beta_{R_{e2e}^{l.o.f_1}, T_{e2e}^{l.o.f_1}}$	$R_{e2e}^{l.o.f_1} = R_{s_1} - r_{s_1}^{xf_1}$	$= 20 - 5$
		$= 15$
	$T_{e2e}^{l.o.f_1} = T_{s_1} + \frac{b_{s_1}^{x'f_1} + r_{s_1}^{xf_1} \cdot T_{s_1}}{R_{e2e}^{l.o.f_1}}$	$= 20 + \frac{125 + 5 \cdot 20}{15}$
		$= 35$
	$=$	$= \beta_{15,35}$
D^{f_1}		$\beta_{e2e}^{l.o.f_1} = b^{f_1}$
		$15 \cdot [t - 35]^+ = 25$
		$t = 36\frac{2}{3}$
B^{f_1}		$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 35 + 25$
		$= 200$

Tandem_1SC_3Flows_1AC_3Paths



- $\beta_{s_0} = \beta_{s_1} = \beta_{s_2} = \beta_{R_{s_i}, T_{s_i}} = \beta_{20,20}, i \in \{0, 1, 2\}$
- $\mathcal{F} = \{f_0, f_1, f_2\}$
- $\alpha^{f_0} = \alpha^{f_1} = \alpha^{f_2} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}, j \in \{0, 1, 2\}$

$\text{arrivalBound}(s_1, \{f_0\}, \{f_2\}) = \alpha_{s_1}^{f_0}$ $= \text{arrivalBound}(s_1, \{f_2\}, \{f_0\}) = \alpha_{s_1}^{f_2}$		FIFO_MUX	ARB_MUX
$\alpha_{s_0}^{f_j}, j \in \{0, 2\}$		$= \gamma_{5,25}$	
$\alpha_{s_0}^{xf_j}$		$= \gamma_{0,0}$	
$\beta_{s_0}^{l.o.f_j} = \beta_{s_0} \ominus \alpha_{s_0}^{xf_j} = \beta_{R_{s_0}^{l.o.f_j}, T_{s_0}^{l.o.f_j}}$		$= \beta_{20,20}$	
$\alpha_{s_1}^{f_j} = \alpha_{s_0}^{f_j} \oslash \beta_{s_0}^{l.o.f_j} = \gamma_{r_{s_1}^{f_j}, b_{s_1}^{f_j}}$	$r_{s_1}^{f_j}$	$= 5$	
	$b_{s_1}^{f_j}$	$\alpha_{s_0}^{f_j}(T_{s_0}^{l.o.f_j}) = 5 \cdot 20 + 25 = 125$	
	$=$	$= \gamma_{5,125}$	

$\text{arrivalBound}(s_1, \{f_0\}, \{f_0\}) = \alpha_{s_1}^{f_0}$ $= \text{arrivalBound}(s_1, \{f_2\}, \{f_2\}) = \alpha_{s_1}^{f_2}$		FIFO_MUX	ARB_MUX
$\alpha_{s_0}^{f_j}, j \in \{0, 2\}$		$= \gamma_{5,25}$	
$\alpha_{s_0}^{xf_j}$		$= \gamma_{5,25}$	
$\beta_{s_0}^{l.o.f_j} = \beta_{s_0} \ominus \alpha_{s_0}^{xf_j} = \beta_{R_{s_0}^{l.o.f_j}, T_{s_0}^{l.o.f_j}}$	$R_{s_0}^{l.o.f_j}$	$= 15$	
	$T_{s_0}^{l.o.f_j}$	$\beta_{s_0} = b_{s_0}^{f_j}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$	$\beta_{s_0} = \alpha_{s_0}^{f_j}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$
	$=$	$= \beta_{15, 21\frac{1}{4}}$	$= \beta_{15, 28\frac{1}{3}}$
	$r_{s_1}^{f_j}$	$= 5$	
	$b_{s_1}^{f_j}$	$\alpha_{s_0}^{f_j}(T_{s_0}^{l.o.f_j}) = 131\frac{1}{4}$	$\alpha_{s_0}^{f_j}(T_{s_0}^{l.o.f_j}) = 166\frac{2}{3}$
$\alpha_{s_1}^{f_j} = \alpha_{s_0}^{f_j} \oslash \beta_{s_0}^{l.o.f_j} = \gamma_{r_{s_1}^{f_j}, b_{s_1}^{f_j}}$		$= \gamma_{5, 131\frac{1}{4}}$	$= \gamma_{5, 166\frac{2}{3}}$

$\text{arrivalBound}(s_1, \{f_0, f_2\}, \mathcal{G}), \mathcal{G} \in \mathcal{P}(\{f_1\}) = \alpha_{s_1}^{\{f_0, f_2\}}$		FIFO_MUX	ARB_MUX
$\alpha_{s_0}^{\{f_0, f_2\}}$		$= \gamma_{10,50}$	
$\alpha_{s_0}^{x\{f_0, f_2\}}$		$= \gamma_{0,0}$	
$\beta_{s_0}^{l.o.\{f_0, f_2\}} = \beta_{s_0} \ominus \alpha_{s_0}^{x\{f_0, f_2\}} = \beta_{R_{s_0}^{l.o.\{f_0, f_2\}}, T_{s_0}^{l.o.\{f_0, f_2\}}}$		$= \beta_{20,20}$	
$\alpha_{s_1}^{\{f_0, f_2\}} = \alpha_{s_0}^{\{f_0, f_2\}} \oslash \beta_{s_0}^{l.o.\{f_0, f_2\}} = \gamma_{r_{s_1}^{\{f_0, f_2\}}, b_{s_1}^{\{f_0, f_2\}}}$	$r_{s_1}^{\{f_0, f_2\}}$	$= 10$	
	$b_{s_1}^{\{f_0, f_2\}}$	$\alpha_{s_0}^{\{f_0, f_2\}}(T_{s_0}^{l.o.\{f_0, f_2\}}) = 10 \cdot 20 + 50 = 250$	
	$=$	$= \gamma_{10,250}$	

arrivalBound($s_2, \{f_2\}, \mathcal{G}$), $\mathcal{G} \in \mathcal{P}(\{f_1\}) = \alpha_{s_2}^{f_2}$		FIFO_MUX	ARB_MUX
$\alpha_{s_1}^{f_2}$		$= \gamma_{5,131\frac{1}{4}}$	$= \gamma_{5,166\frac{2}{3}}$
$\alpha_{s_1}^{xf_2}$		$= \gamma_{5,131\frac{1}{4}}$	$= \gamma_{5,166\frac{2}{3}}$
$\beta_{s_1}^{l.o.f_2} = \beta_{s_1} \ominus \alpha_{s_1}^{xf_2} = \beta_{s_1} \ominus (\alpha_{s_0}^{f_0})^* = \beta_{R_{s_1}^{l.o.f_2}, T_{s_1}^{l.o.f_2}}$	$R_{s_1}^{l.o.f_2}$	$= 15$	
	$T_{s_1}^{l.o.f_2}$	$\beta_{s_1} = b_{s_0 s_1}^{f_0}$ $20 \cdot [t - 20]^+ = 131\frac{1}{4}$ $t = 26\frac{9}{16}$	$\beta_{s_1} = \alpha_{s_0 s_1}^{f_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 166\frac{2}{3}$ $t = 37\frac{7}{9}$
	$=$	$= \beta_{15, 26\frac{9}{16}}$	$= \beta_{15, 37\frac{7}{9}}$
	$r_{s_2}^{f_2}$	$= 5$	
$\alpha_{s_2}^{f_2} = \alpha_{s_1}^{f_2} \oslash \beta_{s_1}^{l.o.f_2} = \gamma_{r_{s_2}^{f_2}, b_{s_2}^{f_2}}$	$b_{s_2}^{f_2}$	$\alpha_{s_1}^{f_2}(T_{s_1}^{l.o.f_2}) = 5 \cdot 26\frac{9}{16} + 131\frac{1}{4} = 264\frac{1}{16}$	$\alpha_{s_1}^{f_2}(T_{s_1}^{l.o.f_2}) = 5 \cdot 37\frac{7}{9} + 166\frac{2}{3} = 355\frac{5}{9}$
	$=$	$= \gamma_{5, 264\frac{1}{16}}$	$= \gamma_{5, 355\frac{5}{9}}$

Flow f_0 (comparable to Tandem_1SC_2Flows_1AC_1Path)

TFA		FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0} = \alpha^{f_0} + \alpha^{f_1}$	$= \gamma_{10,50}$	
	$D_{s_0}^{f_0}$	$\beta_{s_0} = b_{s_0}$ $20 \cdot [t - 20]^+ = 50$ $t = 22\frac{1}{2}$	$\beta_{s_0} = \alpha_{s_0}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 50$ $t = 45$
	$B_{s_0}^{f_0}$	$\alpha_{s_0}(T_{s_0}) = 20 \cdot 10 + 50$ $= 250$	
s_1	$\alpha_{s_1} = \alpha_{s_1}^{\{f_0, f_2\}}$	$= \gamma_{10,250}$	
	$D_{s_1}^{f_0}$	$\beta_{s_1} = b_{s_1}$ $20 \cdot [t - 20]^+ = 250$ $t = 32\frac{1}{2}$	$\beta_{s_1} = \alpha_{s_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 250$ $t = 65$
	$B_{s_1}^{f_0}$	$\alpha_{s_1}(T_{s_1}) = 10 \cdot 20 + 250$ $= 450$	
D^{f_0}		$\sum_{i=0}^1 D_{s_i}^{f_0} = 55$	$\sum_{i=0}^1 D_{s_i}^{f_0} = 110$
B^{f_0}		$\max_{i=\{0,1\}} b_{s_i}^{f_0} = 450$	

SFA		FIFO_MUX	ARB_MUX	
s0	$\alpha_{s_0}^{xf_0} = \alpha^{f_2}$		$= \gamma_{5,25}$	
	$\beta_{s_0}^{l.o.f_0} = \beta_{s_0} \ominus \alpha_{s_0}^{xf_0}$	$R_{s_0}^{l.o.f_0}$	$= 5$	
		$T_{s_0}^{l.o.f_0}$	$\beta_{s_0} = b_{s_0}^{xf_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$	$\beta_{s_0} = \alpha_{s_0}^{xf_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$
		$=$	$= \beta_{15,21\frac{1}{4}}$	$= \beta_{15,28\frac{1}{3}}$
s1	$\alpha_{s_1}^{xf_0} = \alpha_{s_1}^{xf_0}$		$= \gamma_{5,125}$	
	$\beta_{s_1}^{l.o.f_0} = \beta_{s_1} \ominus \alpha_{s_1}^{xf_0}$	$R_{s_1}^{l.o.f_0}$	$= 15$	
		$T_{s_1}^{l.o.f_0}$	$\beta_{s_1} = b_{s_1}^{xf_0}$ $20 \cdot [t - 20]^+ = 125$ $t = 26\frac{1}{4}$	$\beta_{s_1} = \alpha_{s_1}^{xf_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 125$ $t = 35$
		$=$	$= \beta_{15,26\frac{1}{4}}$	$= \beta_{15,35}$
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$		$\bigotimes_{i=0}^1 \beta_{s_i}^{l.o.f_0} = \beta_{15,47\frac{1}{2}}$	$\bigotimes_{i=0}^1 \beta_{s_i}^{l.o.f_0} = \beta_{15,63\frac{1}{3}}$	
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $15 \cdot [t - 47\frac{1}{2}]^+ = 25$ $t = 49\frac{1}{6}$	$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $15 \cdot [t - 63\frac{1}{3}]^+ = 25$ $t = 65$	
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 47\frac{1}{2} + 25$ $= 262\frac{1}{2}$	$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 63\frac{1}{3} + 25$ $= 341\frac{2}{3}$	

PMOO		ARB_MUX
s_0	$\alpha_{s_0}^{x'f_0}$	$= \gamma_{5,25}$
	$\alpha_{s_0}^{xf_0}$	$= \gamma_{5,25}$
s_1	$\alpha_{s_1}^{x'f_0}$	$= \gamma_{0,0}$
	$\alpha_{s_1}^{xf_0}$	$= \gamma_{5,125}$
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$	$R_{e2e}^{l.o.f_0} = \bigwedge_{i \in \{0,1\}} (R_{s_i} - r_{s_i}^{xf_0})$	$= (20 - 5) \wedge (20 - 5)$
		$= 15$
	$T_{e2e}^{l.o.f_0} = \sum_{i \in \{0,1\}} T_{s_i} + \frac{\sum_{i \in \{0,1\}} (b_{s_i}^{x'f_0} + r_{s_i}^{xf_0} \cdot T_{s_i})}{R_{e2e}^{l.o.f_0}}$	$= 20 + 20 + \frac{25 + 5 \cdot 20 + 0 + 5 \cdot 20}{15}$
	$=$	$= 55$
		$= \beta_{15,55}$
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $15 \cdot [t - 55]^+ = 25$ $t = 56\frac{2}{3}$
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 55 + 25$ $= 300$

Flow f_1 (comparable with Node_2Flows_2ACs)

TFA		FIFO_MUX	ARB_MUX
s_2	$\alpha_{s_2} = \alpha^{f_1} + \alpha_{s_1 s_2}^{f_2}$	$\gamma_{5,25} + \gamma_{5,264\frac{1}{16}} = \gamma_{10,289\frac{1}{16}}$	$\gamma_{5,25} + \gamma_{5,355\frac{5}{9}} = \gamma_{10,380\frac{5}{9}}$
		$\beta_{s_2} = b_{s_2}$	$\beta_{s_2} = \alpha_{s_2}$
	$D_{s_2}^{f_1}$	$20 \cdot [t - 20]^+ = 289\frac{1}{16}$ $t = 34\frac{29}{64}$	$20 \cdot [t - 20]^+ = 10 \cdot t + 380\frac{5}{9}$ $t = 78\frac{5}{90}$
	$B_{s_2}^{f_1}$	$\alpha_{s_2}(T_{s_2}) = 10 \cdot 20 + 289\frac{1}{16}$ $= 489\frac{1}{16}$	$\alpha_{s_2}(T_{s_2}) = 10 \cdot 20 + 380\frac{5}{9}$ $= 580\frac{5}{9}$
D^{f_1}		$= 34\frac{29}{64}$	$= 78\frac{5}{90}$
B^{f_1}		$= 489\frac{1}{16}$	$= 580\frac{5}{9}$

SFA			FIFO_MUX	ARB_MUX
s_2	$\alpha_{s_2}^{xf_1} = \alpha_{s_2}^{f_2}$		$= \gamma_{5,264 \frac{1}{16}}$	$= \gamma_{5,355 \frac{5}{9}}$
	$\beta_{s_2}^{l.o.f_1} = \beta_{s_2} \ominus \alpha_{s_2}^{xf_1} = \beta_{s_2} \ominus \alpha_{s_1 s_2}^{xf_1}$	$R_{s_2}^{l.o.f_1}$	$= 15$	
		$T_{s_2}^{l.o.f_1}$	$\beta_{s_2} = b_{s_2}^{xf_1}$	$\beta_{s_2} = \alpha_{s_2}^{xf_1}$
			$20 \cdot [t - 20]^+ = 264 \frac{1}{16}$ $t = 33 \frac{13}{64}$	$20 \cdot [t - 20]^+ = 5 \cdot t + 355 \frac{5}{9}$ $t = 50 \frac{10}{27}$
		$=$	$= \beta_{15,33 \frac{13}{64}}$	$= \beta_{15,50 \frac{10}{27}}$
$\beta_{e2e}^{l.o.f_1} = \beta_{s_2}^{l.o.f_1}$			$= \beta_{15,33 \frac{13}{64}}$	$= \beta_{15,50 \frac{10}{27}}$
D^{f_1}			$\beta_{e2e}^{l.o.f_1} = b^{f_1}$ $15 \cdot [t - 33 \frac{13}{64}]^+ = 25$ $t = 34 \frac{167}{192}$	$\beta_{e2e}^{l.o.f_1} = b^{f_1}$ $15 \cdot [t - 50 \frac{10}{27}]^+ = 25$ $t = 52 \frac{1}{27}$
B^{f_1}			$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 33 \frac{13}{64} + 25$ $= 191 \frac{1}{64}$	$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 50 \frac{10}{27} + 25$ $= 276 \frac{23}{27}$

PMOO		ARB_MUX
s_2	$\alpha_{s_2}^{x'f_1}$	$= \gamma_{5,355\frac{5}{9}}$
	$\alpha_{s_2}^{xf_1}$	$= \gamma_{5,355\frac{5}{9}}$
$\beta_{e2e}^{l.o.f_1} = \beta_{R_{e2e}^{l.o.f_1}, T_{e2e}^{l.o.f_1}}$	$R_{e2e}^{l.o.f_1} = R_{s_2} - r_{s_2}^{xf_0}$	$= 20 - 5$
		$= 15$
	$T_{e2e}^{l.o.f_1} = T_{s_2} + \frac{b_{s_2}^{x'f_1} + r_{s_2}^{xf_1} \cdot T_{s_2}}{R_{e2e}^{l.o.f_1}}$	$= 20 + \frac{355\frac{5}{9} + 5 \cdot 20}{15}$
		$= 50\frac{10}{27}$
	$=$	$= \beta_{15,50\frac{10}{27}}$
D^{f_1}		$\beta_{e2e}^{l.o.f_1} = b^{f_1}$
		$15 \cdot [t - 50\frac{10}{27}]^+ = 25$
		$t = 52\frac{1}{27}$
B^{f_1}		$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 50\frac{10}{27} + 25$
		$= 276\frac{23}{27}$

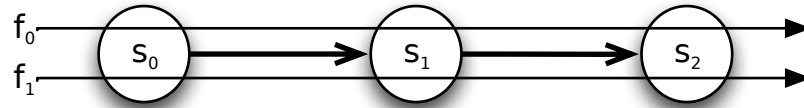
Flow f_2

TFA		FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0} = \alpha_{s_0}^{f_0} + \alpha_{s_0}^{f_1}$	$= \gamma_{10,50}$	
	$D_{s_0}^{f_2}$	$\beta_{s_0} = b_{s_0}$ $20 \cdot [t - 20]^+ = 50$ $t = 22\frac{1}{2}$	$\beta_{s_0} = \alpha_{s_0}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 50$ $t = 45$
	$B_{s_0}^{f_2}$	$\alpha_{s_0}(T_{s_0}) = 20 \cdot 10 + 50$ $= 250$	
s_1	$\alpha_{s_1} = \alpha_{s_1}^{\{f_0, f_1\}}$	$= \gamma_{10,250}$	
	$D_{s_1}^{f_2}$	$\beta_{s_1} = b_{s_1}$ $20 \cdot [t - 20]^+ = 250$ $t = 32\frac{1}{2}$	$\beta_{s_1} = \alpha_{s_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 250$ $t = 65$
	$B_{s_1}^{f_2}$	$\alpha_{s_1}(T_{s_1}) = 10 \cdot 20 + 250$ $= 450$	
s_2	$\alpha_{s_2} = \alpha_{s_2}^{f_1} + \alpha_{s_2}^{f_2}$	$\gamma_{5,25} + \gamma_{5,264\frac{1}{16}} = \gamma_{10,289\frac{1}{16}}$	$\gamma_{5,25} + \gamma_{5,355\frac{5}{9}} = \gamma_{10,380\frac{5}{9}}$
	$D_{s_2}^{f_2}$	$\beta_{s_2} = b_{s_2}$ $20 \cdot [t - 20]^+ = 289\frac{1}{16}$ $t = 34\frac{29}{64}$	$\beta_{s_2} = \alpha_{s_2}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 380\frac{5}{9}$ $t = 78\frac{5}{90}$
	$B_{s_2}^{f_2}$	$\alpha_{s_2}(T_{s_2}) = 10 \cdot 20 + 289\frac{1}{16}$ $= 489\frac{1}{16}$	$\alpha_{s_2}(T_{s_2}) = 10 \cdot 20 + 380\frac{5}{9}$ $= 580\frac{5}{9}$
D^{f_2}		$\sum_{i=0}^2 D_{s_i}^{f_2} = 89\frac{29}{64}$	$\sum_{i=0}^2 D_{s_i}^{f_2} = 188\frac{5}{90}$
B^{f_2}		$\max_{i=\{0,1,2\}} b_{s_i}^{f_0} = 489\frac{1}{16}$	$\max_{i=\{0,1,2\}} b_{s_i}^{f_0} = 580\frac{5}{9}$

SFA			FIFO_MUX	ARB_MUX
s0	$\alpha_{s_0}^{xf_2} = \alpha_{s_0}^{f_0}$		$= \gamma_{5,25}$	
	$\beta_{s_0}^{l.o.f_2} = \beta_{s_0} \ominus \alpha_{s_0}^{xf_2} = \beta_{s_0} \ominus \alpha_{s_0}^{f_0}$	$R_{s_0}^{l.o.f_2}$	$= 5$	
		$T_{s_0}^{l.o.f_2}$	$\beta_{s_0} = b_{s_0}^{xf_2}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$	$\beta_{s_0} = \alpha_{s_0}^{xf_2}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$
		$=$	$= \beta_{15,21\frac{1}{4}}$	$= \beta_{15,28\frac{1}{3}}$
s1	$\alpha_{s_1}^{xf_2} = \alpha_{s_1}^{xf_2}$		$= \gamma_{5,125}$	
	$\beta_{s_1}^{l.o.f_2} = \beta_{s_1} \ominus \alpha_{s_1}^{xf_2}$	$R_{s_1}^{l.o.f_2}$	$= 15$	
		$T_{s_1}^{l.o.f_2}$	$\beta_{s_1} = b_{s_1}^{xf_2}$ $20 \cdot [t - 20]^+ = 125$ $t = 26\frac{1}{4}$	$\beta_{s_1} = \alpha_{s_1}^{xf_2}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 125$ $t = 35$
		$=$	$= \beta_{15,26\frac{1}{4}}$	$= \beta_{15,35}$
s2	$\alpha_{s_2}^{xf_2} = \alpha_{s_2}^{f_1}$		$= \gamma_{5,25}$	
	$\beta_{s_2}^{l.o.f_2} = \beta_{s_2} \ominus \alpha_{s_2}^{xf_2} = \beta_{s_2} \ominus \alpha_{s_2}^{f_1}$	$R_{s_2}^{l.o.f_2}$	$= 15$	
		$T_{s_2}^{l.o.f_2}$	$\beta_{s_2} = b_{s_2}^{xf_2}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$	$\beta_{s_2} = \alpha_{s_2}^{xf_2}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$
		$=$	$= \beta_{15,21\frac{1}{4}}$	$= \beta_{15,28\frac{1}{3}}$
$\beta_{e2e}^{l.o.f_2}$			$\bigotimes_{i=0}^2 \beta_{s_i}^{l.o.f_2} = \beta_{15,68\frac{3}{4}}$	$\bigotimes_{i=0}^2 \beta_{s_i}^{l.o.f_0} = \beta_{15,91\frac{2}{3}}$
D^{f_2}			$\beta_{e2e}^{l.o.f_2} = b^{f_2}$ $15 \cdot [t - 68\frac{3}{4}]^+ = 25$ $t = 70\frac{5}{12}$	$\beta_{e2e}^{l.o.f_2} = b^{f_2}$ $15 \cdot [t - 91\frac{2}{3}]^+ = 25$ $t = 93\frac{1}{3}$
B^{f_2}			$\alpha^{f_2}(T_{s_2}^{l.o.f_2}) = 5 \cdot 68\frac{3}{4} + 25$ $= 368\frac{3}{4}$	$\alpha^{f_2}(T_{e2e}^{l.o.f_2}) = 5 \cdot 91\frac{2}{3} + 25$ $= 483\frac{1}{3}$

PMOO		ARB_MUX
s_0	$\alpha_{s_0}^{x'f_2}$	$= \gamma_{5,25}$
	$\alpha_{s_0}^{xf_2}$	$= \gamma_{5,25}$
s_1	$\alpha_{s_1}^{x'f_2}$	$= \gamma_{0,0}$
	$\alpha_{s_1}^{xf_2}$	$= \gamma_{5,125}$
s_2	$\alpha_{s_2}^{x'f_2}$	$= \gamma_{5,25}$
	$\alpha_{s_2}^{xf_2}$	$= \gamma_{5,25}$
$\beta_{e2e}^{l.o.f_2} = \beta_{R_{e2e}^{l.o.f_2}, T_{e2e}^{l.o.f_2}}$	$R_{e2e}^{l.o.f_2} = \bigwedge_{i \in \{0,1,2\}} (R_{s_i} - r_{s_i}^{xf_2})$	$= (20 - 5) \wedge (20 - 5) \wedge (20 - 5)$
		$= 15$
	$T_{e2e}^{l.o.f_2} = \sum_{i \in \{0,1,2\}} T_{s_i} + \frac{\sum_{i \in \{0,1,2\}} (b_{s_i}^{x'f_2} + r_{s_i}^{xf_2} \cdot T_{s_i})}{R_{e2e}^{l.o.f_0}}$	$= 20 + 20 + 20 + \frac{25 + 5 \cdot 20 + 0 + 5 \cdot 20 + 25 + 5 \cdot 20}{15}$
	$=$	$= 83\frac{1}{3}$
D^{f_2}		$\beta_{e2e}^{l.o.f_2} = b^{f_1}$ $15 \cdot [t - 83\frac{1}{3}] = 25$ $t = 85$
B^{f_2}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 83\frac{1}{3} + 25$ $= 441\frac{2}{3}$

Tandem_1SC_2Flows_1AC_1Path_v2



- $\beta_{s_0} = \beta_{s_1} = \beta_{s_2} = \beta_{R_{s_i}, T_{s_i}} = \beta_{20,20}, i \in \{0,1\}$
- $\mathcal{F} = \{f_0, f_1\}$
- $\alpha^{f_0} = \alpha^{f_1} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}, j \in \{0,1\}$

arrivalBound($s_1, \{f_0, f_1\}, \{\}\rangle = \alpha_{s_1}^{\{f_0, f_1\}}$		FIFO_MUX	ARB_MUX
$\alpha_{s_0}^{\{f_0, f_1\}}$			$= \gamma_{10,50}$
$\alpha_{s_0}^{x\{f_0, f_1\}}$			$= \gamma_{0,0}$
$\beta_{s_0}^{l.o.\{f_0, f_1\}} = \beta_{s_0} \ominus \alpha_{s_0}^{x\{f_0, f_1\}} = \beta_{R_{s_0}^{l.o.\{f_0, f_1\}}, T_{s_0}^{l.o.\{f_0, f_1\}}}$			$= \beta_{20,20}$
$\alpha_{s_1}^{\{f_0, f_1\}} = \alpha_{s_0}^{\{f_0, f_1\}} \odot \beta_{s_0}^{l.o.\{f_0, f_1\}} = \gamma_{r_{s_1}^{\{f_0, f_1\}}, b_{s_1}^{\{f_0, f_1\}}}$	$r_{s_1}^{\{f_0, f_1\}}$		$= 10$
	$b_{s_1}^{\{f_0, f_1\}}$	$\alpha_{s_0}^{\{f_0, f_1\}}(T_{s_0}^{l.o.\{f_0, f_1\}})$	$= 10 \cdot 20 + 50 = 250$
	$=$		$= \gamma_{10,250}$

arrivalBound($s_2, \{f_0, f_1\}, \{\}\rangle = \alpha_{s_2}^{\{f_0, f_1\}}$		FIFO_MUX	ARB_MUX
$\alpha_{s_1}^{\{f_0, f_1\}}$			$= \gamma_{10,250}$
$\alpha_{s_1}^{x\{f_0, f_1\}}$			$= \gamma_{0,0}$
$\beta_{s_1}^{l.o.\{f_0, f_1\}} = \beta_{s_1} \ominus \alpha_{s_1}^{x\{f_0, f_1\}} = \beta_{R_{s_1}^{l.o.\{f_0, f_1\}}, T_{s_1}^{l.o.\{f_0, f_1\}}}$			$= \beta_{20,20}$
$\alpha_{s_2}^{\{f_0, f_1\}} = \alpha_{s_1}^{\{f_0, f_1\}} \odot \beta_{s_1}^{l.o.\{f_0, f_1\}} = \gamma_{r_{s_2}^{\{f_0, f_1\}}, b_{s_2}^{\{f_0, f_1\}}}$	$r_{s_2}^{\{f_0, f_1\}}$		$= 10$
	$b_{s_2}^{\{f_0, f_1\}}$	$\alpha_{s_1}^{\{f_0, f_1\}}(T_{s_1}^{l.o.\{f_0, f_1\}})$	$= 10 \cdot 20 + 250 = 250$
	$=$		$= \gamma_{10,450}$

arrivalBound($s_1, \{f_0\}, \{f_1\}\rangle = \alpha_{s_1}^{f_0}$ = arrivalBound($s_1, \{f_1\}, \{f_0\}\rangle = \alpha_{s_1}^{f_1}$		FIFO_MUX	ARB_MUX
$\alpha_{s_0}^{f_j}$			$= \gamma_{5,25}$
$\alpha_{s_0}^{x f_j}$			$= \gamma_{0,0}$
$\beta_{s_0}^{l.o.f_j} = \beta_{s_0} \ominus \alpha_{s_0}^{x f_j} = \beta_{R_{s_0}^{l.o.f_j}, T_{s_0}^{l.o.f_j}}$			$= \beta_{20,20}$
$\alpha_{s_1}^{f_j} = \alpha_{s_0}^{f_j} \odot \beta_{s_0}^{l.o.f_j} = \gamma_{r_{s_1}^{f_j}, b_{s_1}^{f_j}}$	$r_{s_1}^{f_j}$		$= 5$
	$b_{s_1}^{f_j}$	$\alpha_{s_0}^{f_j}(T_{s_0}^{l.o.f_j})$	$= 5 \cdot 20 + 25 = 125$
	$=$		$= \gamma_{5,125}$

$\text{arrivalBound}(s_2, \{f_0\}, \{f_1\}) = \alpha_{s_2}^{f_0}$ $= \text{arrivalBound}(s_2, \{f_1\}, \{f_0\}) = \alpha_{s_2}^{f_1}$		FIFO_MUX	ARB_MUX
$\alpha_{s_1}^{f_j}$		$= \gamma_{5,125}$	
$\alpha_{s_1}^{xf_j}$		$= \gamma_{0,0}$	
$\beta_{s_1}^{\text{l.o.}f_j} = \beta_{s_1} \ominus \alpha_{s_1}^{xf_j} = \beta_{R_{s_1}^{\text{l.o.}f_j}, T_{s_1}^{\text{l.o.}f_j}}$		$= \beta_{20,20}$	
$\alpha_{s_2}^{f_j} = \alpha_{s_1}^{f_j} \oslash \beta_{s_1}^{\text{l.o.}f_j} = \gamma_{r_{s_2}^{f_j}, b_{s_2}^{f_j}}$	$r_{s_2}^{f_j}$	$= 5$	
	$b_{s_2}^{f_j}$	$\alpha_{s_1}^{f_j}(T_{s_1}^{\text{l.o.}f_j}) = 5 \cdot 20 + 125 = 225$	
	$=$	$= \gamma_{5,125}$	

Flows $f_j, j \in \{0, 1\}$

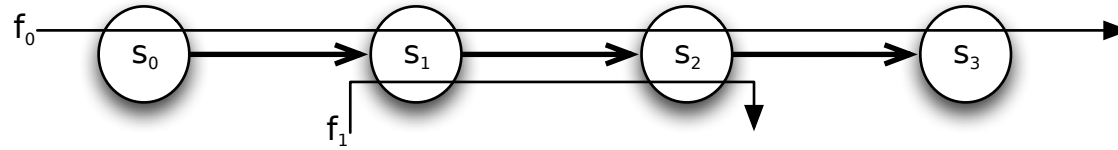
TFA results will be equal for all flows as they share the same path of servers.

TFA		FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0} = \alpha_{s_0}^{f_0} + \alpha_{s_0}^{f_1}$	$= \gamma_{10,50}$	
	$D_{s_0}^{f_j}$	$\beta_{s_0} = b_{s_0}$ $20 \cdot [t - 20]^+ = 50$ $t = 22\frac{1}{2}$	$\beta_{s_0} = \alpha_{s_0}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 50$ $t = 45$
	$B_{s_0}^{f_j}$	$\alpha_{s_0}(T_{s_0}) = 10 \cdot 20 + 50$ $= 250$	
s_1	$\alpha_{s_1} = \alpha_{s_1}^{\{f_0, f_1\}}$	$= \gamma_{10,250}$	
	$D_{s_1}^{f_j}$	$\beta_{s_1} = b_{s_1}$ $20 \cdot [t - 20]^+ = 250$ $t = 32\frac{1}{2}$	$\beta_{s_1} = \alpha_{s_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 250$ $t = 65$
	$B_{s_1}^{f_j}$	$\alpha_{s_1}(T_{s_1}) = 10 \cdot 20 + 250$ $= 450$	
s_2	$\alpha_{s_2} = \alpha_{s_2}^{\{f_0, f_1\}}$	$= \gamma_{10,450}$	
	$D_{s_2}^{f_j}$	$\beta_{s_2} = b_{s_2}$ $20 \cdot [t - 20]^+ = 450$ $t = 42\frac{1}{2}$	$\beta_{s_2} = \alpha_{s_2}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 450$ $t = 85$
	$B_{s_2}^{f_j}$	$\alpha_{s_1}(T_{s_1}) = 10 \cdot 20 + 450$ $= 650$	
D^{f_j}		$\sum_{i=0}^2 D_{s_i}^{f_j} = 97\frac{1}{2}$	$\sum_{i=0}^2 D_{s_i}^{f_j} = 195$
B^{f_j}		$\max_{i=\{0,1,2\}} b_{s_i}^{f_j} = 650$	

SFA			FIFO_MUX	ARB_MUX
s ₀	α ^{xf_j} _{s₀}		= γ _{5,25}	
	β ^{1.o.f_j} _{s₀} = β _{s₀} ⊖ α ^{xf_j} _{s₀} = β _{R^{1.o.f_j}_{s₀}, T^{1.o.f_j}_{s₀}}	R ^{1.o.f_j} _{s₀}	= 15	
		T ^{1.o.f_j} _{s₀}	β _{s₀} = b ^{xf_j} _{s₀} 20 · [t − 20] ⁺ = 25 t = 22 ¹ / ₄	β _{s₀} = α ^{xf_j} _{s₀} 20 · [t − 20] ⁺ = 5 · t + 25 t = 28 ¹ / ₃
		=	= β _{15,21¹/₄}	= β _{15,28¹/₃}
s ₁	α ^{xf_j} _{s₁}		= γ _{5,125}	
	β ^{1.o.f_j} _{s₁} = β _{s₁} ⊖ α ^{xf_j} _{s₁}	R ^{1.o.f_j} _{s₁}	= 15	
		T ^{1.o.f_j} _{s₁}	β _{s₁} = b ^{xf_j} _{s₁} 20 · [t − 20] ⁺ = 125 t = 26 ¹ / ₄	β _{s₁} = α ^{xf_j} _{s₁} 20 · [t − 20] ⁺ = 5 · t + 125 t = 35
		=	= β _{15,26¹/₄}	= β _{15,35}
s ₂	α ^{xf_j} _{s₂}		= γ _{5,225}	
	β ^{1.o.f_j} _{s₂} = β _{s₂} ⊖ α ^{xf_j} _{s₂}	R ^{1.o.f_j} _{s₂}	= 15	
		T ^{1.o.f_j} _{s₂}	β _{s₂} = b ^{xf_j} _{s₂} 20 · [t − 20] ⁺ = 225 t = 31 ¹ / ₄	β _{s₂} = α ^{xf_j} _{s₂} 20 · [t − 20] ⁺ = 5 · t + 225 t = 41 ² / ₃
		=	= β _{15,31¹/₄}	= β _{15,41²/₃}
β ^{1.o.f_j} _{e2e} = β _{R^{1.o.f_j}_{e2e}, T^{1.o.f_j}_{e2e}}			⊗ ² _{i=0} β ^{1.o.f_j} _{s_i} = β _{5,78³/₄}	⊗ ² _{i=0} β ^{1.o.f_j} _{s_i} = β _{5,105}
D ^{f_j}			β ^{1.o.f_j} _{e2e} = b ^{f_j} 15 · [t − 78 ³ / ₄] ⁺ = 25 t = 80 ⁵ / ₁₂	β ^{1.o.f_j} _{e2e} = b ^{f_j} 15 · [t − 105] ⁺ = 25 t = 106 ² / ₃
B ^{f_j}			α ^{f_j} (T ^{1.o.f_j} _{e2e}) = 5 · 78 ³ / ₄ + 25 = 418 ³ / ₄	α ^{f_j} (T ^{1.o.f_j} _{e2e}) = 5 · 105 + 25 = 550

PMOO		ARB_MUX
s_0	$\alpha_{s_0}^{x'f_j}$	$= \gamma_{5,25}$
	$\alpha_{s_0}^{xf_j}$	$= \gamma_{5,25}$
s_1	$\alpha_{s_1}^{x'f_j}$	$= \gamma_{0,0}$
	$\alpha_{s_1}^{xf_j}$	$= \gamma_{5,75}$
s_2	$\alpha_{s_2}^{x'f_j}$	$= \gamma_{0,0}$
	$\alpha_{s_2}^{xf_j}$	$= \gamma_{5,225}$
$\beta_{e2e}^{l.o.f_j} = \beta_{R_{e2e}^{l.o.f_j}, T_{e2e}^{l.o.f_j}}$	$R_{e2e}^{l.o.f_j} = \bigwedge_{i \in \{0,1,2\}} (R_{s_i} - r_{s_i}^{xf_j})$	$= (20 - 5) \wedge (20 - 5) \wedge (20 - 5)$
	$T_{e2e}^{l.o.f_j} = \sum_{i \in \{0,1,2\}} T_{s_i} + \frac{\sum_{i \in \{0,1,2\}} (b_{s_i}^{x'f_j} + r_{s_i}^{xf_j} \cdot T_{s_i})}{R_{e2e}^{l.o.f_j}}$	$= 20 + 20 + 20 + \frac{25 + 5 \cdot 20 + 0 + 5 \cdot 20 + 0 + 5 \cdot 20}{15}$
	$=$	$= 81\frac{2}{3}$
D^{f_j}		$\beta_{e2e}^{l.o.f_j} = b^{f_j}$ $15 \cdot [t - 81\frac{2}{3}]^+ = 25$ $t = 83\frac{1}{3}$
B^{f_j}		$\alpha^{f_j}(T_{e2e}^{l.o.f_j}) = 5 \cdot 81\frac{2}{3} + 25$ $= 433\frac{1}{3}$

Tandem_1SC_2Flows_1AC_2Paths_v2



- $\beta_{s_0} = \beta_{s_1} = \beta_{s_2} = \beta_{s_3} = \beta_{R_{s_i}, T_{s_i}} = \beta_{20,20}, i \in \{0,1\}$
- $\mathcal{F} = \{f_0, f_1\}$

$$\alpha^{f_0} = \alpha^{f_1} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}, j \in \{0,1\}$$

arrivalBound($s_1, \{f_0\}, \mathcal{G}$), $\mathcal{G} = \mathcal{P}(\mathcal{F}) = \alpha_{s_1}^{f_0}$		FIFO_MUX	ARB_MUX
$\alpha_{s_0}^{f_0}$			$= \gamma_{5,25}$
$\alpha_{s_0}^{x f_0}$			$= \gamma_{0,0}$
$\beta_{s_0}^{l.o.f_0} = \beta_{s_0} \ominus \alpha_{s_0}^{x f_0} = \beta_{R_{s_0}^{l.o.f_0}, T_{s_0}^{l.o.f_0}}$			$= \beta_{20,20}$
$\alpha_{s_1}^{f_0} = \alpha_{s_0}^{f_0} \odot \beta_{s_0}^{l.o.f_0} = \gamma_{r_{s_1}^{f_0}, b_{s_1}^{f_0}}$	$r_{s_1}^{f_0}$		$= 10$
	$b_{s_1}^{f_0}$	$\alpha_{s_0}^{f_0}(T_{s_0}^{l.o.f_0}) = 5 \cdot 20 + 25 = 125$	
	$=$		$= \gamma_{5,125}$

arrivalBound($s_2, \{f_0\}, \{f_0\}) = \alpha_{s_2}^{f_0}$		FIFO_MUX	ARB_MUX
$\alpha_{s_1}^{f_0}$			$= \gamma_{5,125}$
$\alpha_{s_1}^{x f_0}$			$= \gamma_{5,25}$
$\beta_{s_1}^{l.o.f_0} = \beta_{s_1} \ominus \alpha_{s_1}^{x f_0}$	$R_{s_1}^{l.o.f_0}$		$= 15$
	$T_{s_1}^{l.o.f_0}$	$\beta_{s_1} = b_{s_1}^{x f_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$	$\beta_{s_1} = \alpha_{s_1}^{x f_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$
	$=$	$= \beta_{15, 21\frac{1}{4}}$	$= \beta_{15, 28\frac{1}{3}}$
	$=$	$= \beta_{15, 21\frac{1}{4}}$	$= \beta_{15, 28\frac{1}{3}}$
$\alpha_{s_2}^{f_0} = \alpha_{s_1}^{f_0} \odot \beta_{s_1}^{l.o.f_0} = \gamma_{r_{s_2}^{f_0}, b_{s_2}^{f_0}}$	$r_{s_2}^{f_0}$		$= 5$
	$b_{s_2}^{f_0}$	$\alpha_{s_1}^{f_0}(T_{s_1}^{l.o.f_0}) = 5 \cdot 21\frac{1}{4} + 125 = 231\frac{1}{4}$	$\alpha_{s_1}^{f_0}(T_{s_1}^{l.o.f_0}) = 5 \cdot 28\frac{1}{3} + 125 = 266\frac{2}{3}$
	$=$	$= \gamma_{5, 231\frac{1}{4}}$	$= \gamma_{5, 266\frac{2}{3}}$

arrivalBound($s_2, \{f_1\}, \{f_0\}) = \alpha_{s_2}^{f_1}$		FIFO_MUX	ARB_MUX
$\alpha_{s_1}^{f_1}$			$= \gamma_{5,25}$
$\alpha_{s_1}^{x f_1}$			$= \gamma_{0,0}$
$\beta_{s_1}^{l.o.f_1} = \beta_{s_1} \ominus \alpha_{s_1}^{x f_1} = \beta_{R_{s_1}^{l.o.f_1}, T_{s_1}^{l.o.f_1}}$			$= \beta_{20,20}$
$\alpha_{s_2}^{f_1} = \alpha_{s_1}^{f_1} \odot \beta_{s_1}^{l.o.f_1} = \gamma_{r_{s_2}^{f_1}, b_{s_2}^{f_1}}$	$r_{s_2}^{f_1}$		$= 10$
	$b_{s_2}^{f_1}$	$\alpha_{s_1}^{f_1}(T_{s_1}^{l.o.f_1}) = 5 \cdot 20 + 25 = 125$	
	$=$	$= \gamma_{5,125}$	

arrivalBound($s_3, \{f_0\}, \{\}$) = $\alpha_{s_3}^{f_0}$		FIFO_MUX	ARB_MUX
$\alpha_{s_2}^{f_0}$		$= \gamma_{5,231\frac{1}{4}}$	$= \gamma_{5,266\frac{2}{3}}$
$\alpha_{s_2}^{xf_0}$		$= \gamma_{5,125}$	
$\beta_{s_2}^{l.o.f_0} = \beta_{s_2} \ominus \alpha_{s_2}^{xf_0}$	$R_{s_2}^{l.o.f_0}$	$= 15$	
	$T_{s_2}^{l.o.f_0}$	$\beta_{s_2} = b_{s_2}^{xf_0}$ $20 \cdot [t - 20]^+ = 156\frac{1}{4}$ $t = 27\frac{13}{16}$	$\beta_{s_2} = \alpha_{s_2}^{xf_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 200$ $t = 40$
	$=$	$= \beta_{15,27\frac{13}{16}}$	$= \beta_{15,40}$
	$r_{s_3}^{f_0}$	$= 5$	
$\alpha_{s_3}^{f_0} = \alpha_{s_2}^{f_0} \oslash \beta_{s_2}^{l.o.f_0} = \gamma_{r_{s_3}^{f_0}, b_{s_3}^{f_0}}$	$b_{s_3}^{f_0}$	$\alpha_{s_2}^{f_0}(T_{s_2}^{l.o.f_0}) = 370\frac{5}{16}$	$\alpha_{s_2}^{f_0}(T_{s_2}^{l.o.f_0}) = 466\frac{2}{3}$
	$=$	$= \gamma_{5,370\frac{5}{16}}$	$= \gamma_{5,466\frac{2}{3}}$

arrivalBound($s_2, \{f_0, f_1\}, \{\}$) = $\alpha_{s_2}^{\{f_0, f_1\}}$		FIFO_MUX	ARB_MUX
$\alpha_{s_1}^{\{f_0, f_1\}}$			$= \gamma_{10,150}$
$\alpha_{s_1}^{x\{f_0, f_1\}}$			$= \gamma_{0,0}$
$\beta_{s_1}^{l.o.\{f_0, f_1\}} = \beta_{s_1} \ominus \alpha_{s_1}^{x\{f_0, f_1\}} = \beta_{R_{s_1}^{l.o.\{f_0, f_1\}}, T_{s_1}^{l.o.\{f_0, f_1\}}}$			$= \beta_{20,20}$
$\alpha_{s_2}^{\{f_0, f_1\}} = \alpha_{s_1}^{\{f_0, f_1\}} \oslash \beta_{s_1}^{l.o.\{f_0, f_1\}} = \gamma_{r_{s_2}^{\{f_0, f_1\}}, b_{s_2}^{\{f_0, f_1\}}}$	$r_{s_2}^{\{f_0, f_1\}}$		$= 10$
	$b_{s_2}^{\{f_0, f_1\}}$	$\alpha_{s_1}^{\{f_0, f_1\}}(T_{s_1}^{l.o.\{f_0, f_1\}}) = 10 \cdot 20 + 150 = 350$	
	$=$		$= \gamma_{10,350}$

arrivalBound($s_2, \{f_0\}, \{f_1\}$) = $\alpha_{s_2}^{f_0}$		FIFO_MUX	ARB_MUX
$\alpha_{s_1}^{f_0}$		$= \gamma_{5,125}$	
$\alpha_{s_1}^{xf_0}$		$= \gamma_{0,0}$	
$\beta_{s_1}^{l.o.f_0} = \beta_{s_1} \ominus \alpha_{s_1}^{xf_0} = \beta_{R_{s_1}^{l.o.f_0}, T_{s_1}^{l.o.f_0}}$		$= \beta_{20,20}$	
$\alpha_{s_2}^{f_0} = \alpha_{s_1}^{f_0} \oslash \beta_{s_1}^{l.o.f_0} = \gamma_{r_{s_2}^{f_0}, b_{s_2}^{f_0}}$	$r_{s_2}^{f_0}$	$= 10$	
	$b_{s_2}^{f_0}$	$\alpha_{s_1}^{f_0}(T_{s_1}^{l.o.f_0}) = 5 \cdot 20 + 125 = 225$	
	$=$	$= \gamma_{5,225}$	

Flow f_0

TFA		FIFO_MUX	ARB_MUX
s_0	α_{s_0}	$= \gamma_{5,25}$	
	$D_{s_0}^{f_0}$	$\beta_{s_0} = b_{s_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$	FIFO per microflow $\beta_{s_0} = b_{s_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$
	$B_{s_0}^{f_0}$	$\alpha_{s_0}(T_{s_0}) = 5 \cdot 20 + 25$ $= 125$	
s_1	$\alpha_{s_1} = \alpha_{s_1}^{f_0} + \alpha_{s_1}^{f_1}$	$= \gamma_{5,125} + \gamma_{5,25} = \gamma_{10,150}$	
	$D_{s_1}^{f_0}$	$\beta_{s_1} = b_{s_1}$ $20 \cdot [t - 20]^+ = 150$ $t = 27\frac{1}{2}$	$\beta_{s_1} = \alpha_{s_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 150$ $t = 55$
	$B_{s_1}^{f_0}$	$\alpha_{s_1}(T_{s_1}) = 10 \cdot 20 + 150$ $= 350$	
s_2	$\alpha_{s_2} = \alpha_{s_2}^{\{f_0, f_1\}}$	$= \gamma_{10,350}$	
	$D_{s_2}^{f_0}$	$\beta_{s_2} = b_{s_2}$ $20 \cdot [t - 20]^+ = 350$ $t = 37\frac{1}{2}$	$\beta_{s_2} = \alpha_{s_2}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 350$ $t = 75$
	$B_{s_2}^{f_0}$	$\alpha_{s_2}(T_{s_2}) = 10 \cdot 20 + 350$ $= 550$	
s_3	$\alpha_{s_3} = \alpha_{s_3}^{f_0}$	$= \gamma_{5,370\frac{5}{16}}$	$= \gamma_{5,466\frac{2}{3}}$
	$D_{s_3}^{f_0}$	$\beta_{s_3} = b_{s_3}$ $20 \cdot [t - 20]^+ = 370\frac{5}{16}$ $t = 38\frac{33}{64}$	FIFO per micro flow $\beta_{s_3} = b_{s_3}$ $20 \cdot [t - 20]^+ = 466\frac{2}{3}$ $t = 43\frac{1}{3}$
	$B_{s_3}^{f_0}$	$\alpha_{s_3}(T_{s_3}) = 5 \cdot 20 + 370\frac{5}{16}$ $= 470\frac{5}{16}$	$\alpha_{s_3}(T_{s_3}) = 5 \cdot 20 + 466\frac{2}{3}$ $= 566\frac{2}{3}$
D^{f_0}		$\sum_{i=0}^3 D_{s_i}^{f_0} = 124\frac{49}{64}$	$\sum_{i=0}^3 D_{s_i}^{f_0} = 194\frac{7}{12}$
B^{f_0}		$\max_{i=0}^3 b_{s_i}^{f_0} = 550$	$\max_{i=0}^3 b_{s_i}^{f_0} = 566\frac{2}{3}$

SFA		FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0}^{xf_0}$	$= \gamma_{0,0}$	
	$\beta_{s_0}^{l.o.f_0}$	$= \beta_{20,20}$	
s_1	$\alpha_{s_1}^{xf_0}$	$= \gamma_{5,25}$	
	$\beta_{s_1}^{l.o.f_0} = \beta_{s_1} \ominus \alpha_{s_1}^{xf_0}$	$R_{s_1}^{l.o.f_0}$	$= 15$
		$T_{s_1}^{l.o.f_0}$	$\beta_{s_1} = b_{s_1}^{xf_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$
		$=$	$= \beta_{15,21\frac{1}{4}}$
s_2	$\alpha_{s_2}^{xf_0}$	$= \gamma_{5,125}$	
	$\beta_{s_2}^{l.o.f_0} = \beta_{s_2} \ominus \alpha_{s_2}^{xf_0}$	$R_{s_2}^{l.o.f_0}$	$= 15$
		$T_{s_2}^{l.o.f_0}$	$\beta_{s_2} = b_{s_2}^{xf_0}$ $20 \cdot [t - 20]^+ = 125$ $t = 26\frac{1}{4}$
		$=$	$= \beta_{15,26\frac{1}{4}}$
s_3	$\alpha_{s_3}^{xf_0}$	$= \gamma_{0,0}$	
	$\beta_{s_3}^{l.o.f_0} = \beta_{s_3} \ominus \alpha_{s_3}^{xf_0}$	$= \beta_{20,20}$	
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$		$\bigotimes_{i=0}^3 \beta_{s_i}^{l.o.f_0} = \beta_{15,87\frac{1}{2}}$	$\bigotimes_{i=0}^3 \beta_{s_i}^{l.o.f_0} = \beta_{15,103\frac{1}{3}}$
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $15 \cdot [t - 87\frac{1}{2}]^+ = 25$ $t = 89\frac{1}{6}$	$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $15 \cdot [t - 103\frac{1}{3}]^+ = 25$ $t = 105$
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 87\frac{1}{2} + 25$ $= 462\frac{1}{2}$	$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 103\frac{1}{3} + 25$ $= 541\frac{2}{3}$

PMOO		ARB_MUX
s_0	$\alpha_{s_0}^{x'f_0}$	$= \gamma_{0,0}$
	$\alpha_{s_0}^{xf_0}$	$= \gamma_{0,0}$
s_1	$\alpha_{s_1}^{x'f_0}$	$= \gamma_{5,25}$
	$\alpha_{s_1}^{xf_0}$	$= \gamma_{5,25}$
s_2	$\alpha_{s_2}^{x'f_0}$	$= \gamma_{0,0}$
	$\alpha_{s_2}^{xf_0}$	$= \gamma_{5,125}$
s_3	$\alpha_{s_3}^{x'f_0}$	$= \gamma_{0,0}$
	$\alpha_{s_3}^{xf_0}$	$= \gamma_{0,0}$
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$	$R_{e2e}^{l.o.f_0} = \bigwedge_{i \in \{0,1,2,3\}} (R_{s_i} - r_{s_i}^{xf_0})$	$= (20 - 0) \wedge (20 - 5) \wedge (20 - 5) \wedge (20 - 0)$
		$=$
	$T_{e2e}^{l.o.f_0} = \sum_{i \in \{0,1,2,3\}} T_{s_i} + \frac{\sum_{i \in \{0,1,2,3\}} (b_{s_i}^{x'f_0} + r_{s_i}^{xf_0} \cdot T_{s_i})}{R_{e2e}^{l.o.f_0}}$	$= 20 + 20 + 20 + 20 + \frac{0 + 0 \cdot 20 + 25 + 5 \cdot 20 + 0 + 5 \cdot 20 + 0 + 0 \cdot 20}{15}$
	$=$	$=$
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$
		$15 \cdot [t - 95]^+ = 25$
		$t = 96\frac{2}{3}$
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 95 + 25$
		$= 500$

Flow f_1

TFA		FIFO_MUX	ARB_MUX
s_1	$\alpha_{s_1} = \alpha_{s_1}^{f_0} + \alpha_{s_1}^{f_1}$	$= \gamma_{5,25} + \gamma_{5,125} = \gamma_{10,150}$	
	$D_{s_1}^{f_1}$	$\beta_{s_1} = b_{s_1}$ $20 \cdot [t - 20]^+ = 150$ $t = 27\frac{1}{2}$	$\beta_{s_1} = \alpha_{s_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 150$ $t = 55$
	$B_{s_1}^{f_1}$	$\alpha_{s_1}(T_{s_1}) = 10 \cdot 20 + 150$ $= 350$	
s_2	$\alpha_{s_2} = \alpha_{s_2}^{\{f_0, f_1\}}$	$= \gamma_{10,350}$	
	$D_{s_2}^{f_1}$	$\beta_{s_2} = b_{s_2}$ $20 \cdot [t - 20]^+ = 350$ $t = 37\frac{1}{2}$	$\beta_{s_2} = \alpha_{s_2}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 350$ $t = 75$
	$B_{s_2}^{f_1}$	$\alpha_{s_2}(T_{s_2}) = 10 \cdot 20 + 350$ $= 550$	
D^{f_1}		$\sum_{i=1}^2 D_{s_i}^{f_1} = 65$	$\sum_{i=1}^2 D_{s_i}^{f_1} = 130$
B^{f_1}		$\max_{i=1}^2 b_{s_i}^{f_1} = 550$	

SFA			FIFO_MUX	ARB_MUX
s1	$\alpha_{s_1}^{xf_1}$		$= \gamma_{5,125}$	
	$\beta_{s_1}^{l.o.f_1} = \beta_{s_1} \ominus \alpha_{s_1}^{xf_1}$	$R_{s_1}^{l.o.f_1}$	$= 15$	
		$T_{s_1}^{l.o.f_1}$	$\beta_{s_1} = b_{s_1}^{xf_1}$ $20 \cdot [t - 20]^+ = 125$ $t = 26\frac{1}{4}$	$\beta_{s_1} = \alpha_{s_1}^{xf_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 125$ $t = 35$
		$=$	$= \beta_{15,26\frac{1}{4}}$	$= \beta_{15,35}$
s2	$\alpha_{s_2}^{xf_1}$		$= \gamma_{5,225}$	
	$\beta_{s_2}^{l.o.f_1} = \beta_{s_2} \ominus \alpha_{s_2}^{xf_1}$	$R_{s_2}^{l.o.f_1}$	$= 15$	
		$T_{s_2}^{l.o.f_1}$	$\beta_{s_2} = b_{s_2}^{xf_1}$ $20 \cdot [t - 20]^+ = 225$ $t = 31\frac{1}{4}$	$\beta_{s_2} = \alpha_{s_2}^{xf_1}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 225$ $t = 41\frac{2}{3}$
		$=$	$= \beta_{15,31\frac{1}{4}}$	$= \beta_{15,41\frac{2}{3}}$
$\beta_{e2e}^{l.o.f_1} = \beta_{R_{e2e}^{l.o.f_1}, T_{e2e}^{l.o.f_1}}$		$\bigotimes_{i=1}^2 \beta_{s_i}^{l.o.f_1} = \beta_{15,57\frac{1}{2}}$	$\bigotimes_{i=1}^2 \beta_{s_i}^{l.o.f_1} = \beta_{15,76\frac{2}{3}}$	
D^{f_1}		$\beta_{e2e}^{l.o.f_1} = b^{f_1}$ $15 \cdot [t - 57\frac{1}{2}]^+ = 25$ $t = 59\frac{1}{6}$	$\beta_{e2e}^{l.o.f_1} = b^{f_1}$ $15 \cdot [t - 76\frac{2}{3}]^+ = 25$ $t = 78\frac{1}{3}$	
B^{f_1}		$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 57\frac{1}{2} + 25$ $= 312\frac{1}{2}$	$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 76\frac{2}{3} + 25$ $= 408\frac{1}{3}$	

PMOO		ARB_MUX
s_1	$\alpha_{s_1}^{x'f_1}$	$= \gamma_{5,125}$
	$\alpha_{s_1}^{xf_1}$	$= \gamma_{5,125}$
s_2	$\alpha_{s_2}^{x'f_1}$	$= \gamma_{0,0}$
	$\alpha_{s_2}^{xf_1}$	$= \gamma_{5,225}$
$\beta_{e2e}^{l.o.f_1} = \beta_{R_{e2e}^{l.o.f_1}, T_{e2e}^{l.o.f_1}}$	$R_{e2e}^{l.o.f_1} = \bigwedge_{i \in \{1,2\}} (R_{s_i} - r_{s_i}^{xf_1})$	$= (20 - 5) \wedge (20 - 5)$
		$= 15$
	$T_{e2e}^{l.o.f_1} = \sum_{i \in \{1,2\}} T_{s_i} + \frac{\sum_{i \in \{1,2\}} (b_{s_i}^{x'f_1} + r_{s_i}^{xf_1} \cdot T_{s_i})}{R_{e2e}^{l.o.f_1}}$	$= 20 + 20 + \frac{125 + 5 \cdot 20 + 0 + 5 \cdot 20}{15}$
	$=$	$= 61\frac{2}{3}$
D^{f_1}		$\beta_{e2e}^{l.o.f_1} = b^{f_1}$ $15 \cdot [t - 61\frac{2}{3}]^+ = 25$ $t = 63\frac{1}{3}$
B^{f_1}		$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 61\frac{2}{3} + 25$ $= 333\frac{1}{3}$