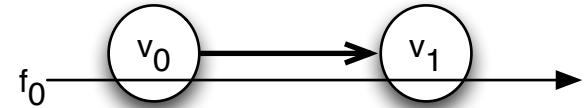


### Tandem \_1SC \_1Flow



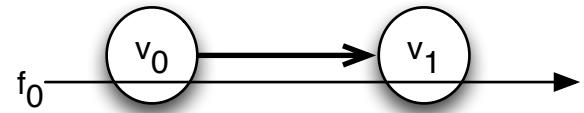
- $\beta_{v_0} = \beta_{v_1} = \beta_{R_{v_i}, T_{v_i}} = \beta_{10,10}, i \in \{0,1\}$
- $\alpha^{f_0} = \gamma_{r^{f_0}, b^{f_0}} = \gamma_{5,25}$

TFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0} = \alpha^{f_0}$		
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$	$= \gamma_{5,25}$ FIFO per mico flow $\beta_{v_0} = b_{v_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$
	$B_{v_0}^{f_0}$		$\alpha_{v_0}(T_{v_0}) = 5 \cdot 10 + 25$ $= 75$
$v_0 v_1$	$\alpha_{v_0 v_1} = (\alpha_{v_0})^*$	$r_{v_0 v_1}$ $b_{v_0 v_1}$ $=$	$= r_{v_0} = r^{f_0} = 5$ $\alpha_{v_0}(T_{v_0}) = 75$ $= \gamma_{5,75}$
	$\alpha_{v_1} = \alpha_{v_0 v_1}$		$= \gamma_{5,75}$
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{v_1}$ $10 \cdot [t - 10]^+ = 75$ $t = 17\frac{1}{2}$	FIFO per micro flow $\beta_{v_1} = b_{v_1}$ $10 \cdot [t - 10]^+ = 75$ $t = 17\frac{1}{2}$
	$B_{v_1}^{f_0}$		$\alpha_{v_1}(T_{v_1}) = 5 \cdot 10 + 75$ $= 125$
	$D^{f_0}$		$\sum_{i=0}^1 D_{v_i}^{f_0} = 30$
	$B^{f_0}$		$\max_{i=\{0,1\}} b_{v_i}^{f_0} = 125$

SFA		FIFO_MUX   ARB_MUX
$v_0$	$\alpha_{v_0}^{xf_0}$	$= \gamma_{0,0}$
	$\beta_{v_0}^{\text{l.o.} f_0} = [\beta_{v_0} - \alpha_{v_0}^{xf_0}]^+ = \beta_{v_0}$	$= \beta_{10,10}$
$v_0 v_1$	$\alpha_{v_0 v_1}^{xf_0}$	$= \gamma_{0,0}$
	$\alpha_{v_1}^{xf_0} = \alpha_{v_0 v_1}^{xf_0}$	$= \gamma_{0,0}$
$v_1$	$\beta_{v_1}^{\text{l.o.} f_0} = [\beta_{v_1} - \alpha_{v_1}^{xf_0}]^+ = \beta_{v_1}$	$= \beta_{10,10}$
	$\beta_{\text{e2e}}^{\text{l.o.} f_0} = \beta_{R_{\text{e2e}}^{\text{l.o.} f_0}, T_{\text{e2e}}^{\text{l.o.} f_0}}$	$\bigotimes_{i=0}^1 \beta_{v_i}^{\text{l.o.} f_0} = \beta_{10,20}$
$D^{f_0}$		$\beta_{\text{e2e}}^{\text{l.o.} f_0} = b^{f_0}$
		$10 \cdot [t - 20]^+ = 25$
		$t = 22\frac{1}{2}$
$B^{f_0}$		$\alpha^{f_0}(T_{\text{e2e}}^{\text{l.o.} f_0}) = 5 \cdot 20 + 25$
		$= 125$

PMOO		ARB_MUX
e2e	$\beta_{\text{e2e}}^{f_0}$	$\bigotimes_{i=0}^1 \beta_{v_i} = \beta_{10,20}$
	$\alpha_{\text{e2e}}^{x f_0}$	$= \gamma_{0,0}$
	$\beta_{\text{e2e}}^{\text{l.o.} f_0} = [\beta_{\text{e2e}}^{f_0} - \alpha_{\text{e2e}}^{x f_0}]^+ = \beta_{\text{e2e}}^{f_0}$	$= \beta_{10,20}$
$D^{f_0}$		$\begin{aligned}\beta_{\text{e2e}}^{\text{l.o.} f_0} &= b^{f_0} \\ 10 \cdot [t - 20]^+ &= 25 \\ t &= 22\frac{1}{2}\end{aligned}$
$B^{f_0}$		$\begin{aligned}\alpha^{f_0}(T_{\text{e2e}}^{\text{l.o.} f_0}) &= 5 \cdot 20 + 25 \\ &= 125\end{aligned}$

### Tandem \_ 2SCs \_ 1Flow



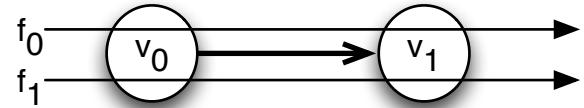
- $\beta_{v_0} = \beta_{R_{v_0}, T_{v_0}} = \beta_{10,10}$
- $\beta_{v_1} = \beta_{R_{v_1}, T_{v_1}} = \beta_{6,6}$
- $\alpha^{f_0} = \gamma_{r^{f_0}, b^{f_0}} = \gamma_{5,25}$

TFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0} = \alpha^{f_0}$	$= \gamma_{5,25}$	
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$	FIFO per micro flow $\beta_{v_0} = b_{v_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$
	$B_{v_0}^{f_0}$	$\alpha_{v_0}(T_{v_0}) = 5 \cdot 10 + 25 = 75$	
$v_0 v_1$	$\alpha_{v_0 v_1} = (\alpha_{v_0})^*$	$r_{v_0 v_1}$	$= r_{v_0} = r^{f_0} = 5$
		$b_{v_0 v_1}$	$\alpha_{v_0}(T_{v_0}) = 75$
		$=$	$= \gamma_{5,75}$
$v_1$	$\alpha_{v_1} = \alpha_{v_0 v_1}$	$= \gamma_{5,75}$	
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{v_1}$ $6 \cdot [t - 6]^+ = 75$ $t = 18\frac{1}{2}$	FIFO per micro flow $\beta_{v_1} = b_{v_1}$ $6 \cdot [t - 6]^+ = 75$ $t = 18\frac{1}{2}$
	$B_{v_1}^{f_0}$	$\alpha_{v_1}(T_{v_1}) = 5 \cdot 6 + 75 = 105$	
$D^{f_0}$		$\sum_{i=0}^1 D_{v_i}^{f_0} = 31$	
$B^{f_0}$		$\max_{i=\{0,1\}} b_{v_i}^{f_0} = 105$	

SFA		FIFO_MUX   ARB_MUX
$v_0$	$\alpha_{v_0}^{x f_0}$	$= \gamma_{0,0}$
	$\beta_{v_0}^{\text{l.o.} f_0} = [\beta_{v_0} - \alpha_{v_0}^{x f_0}]^+ = \beta_{v_0}$	$= \beta_{10,10}$
$v_0 v_1$	$\alpha_{v_0 v_1}^{x f_0}$	$= \gamma_{0,0}$
	$\alpha_{v_1}^{x f_0} = \alpha_{v_0 v_1}^{x f_0}$	$= \gamma_{0,0}$
$v_1$	$\beta_{v_1}^{\text{l.o.} f_0} = [\beta_{v_1} - \alpha_{v_1}^{x f_0}]^+ = \beta_{v_1}$	$= \beta_{6,6}$
	$\beta_{e2e}^{\text{l.o.} f_0} = \beta_{R_{e2e}^{\text{l.o.} f_0}, T_{e2e}^{\text{l.o.} f_0}}$	$\bigotimes_{i=0}^1 \beta_{v_i}^{\text{l.o.} f_0} = \beta_{6,16}$
$D^{f_0}$		$\beta_{e2e}^{\text{l.o.} f_0} = b^{f_0}$
		$6 \cdot [t - 16]^+ = 25$
$B^{f_0}$		$t = 20\frac{1}{6}$
		$\alpha^{f_0}(T_{e2e}^{\text{l.o.} f_0}) = 5 \cdot 16 + 25$
		$= 105$

PMOO		ARB_MUX
e2e	$\beta_{\text{e2e}}^{f_0}$	$\bigotimes_{i=0}^1 \beta_{v_i} = \beta_{6,16}$
	$\alpha_{\text{e2e}}^{x f_0}$	$= \gamma_{0,0}$
	$\beta_{\text{e2e}}^{\text{l.o.} f_0} = [\beta_{\text{e2e}}^{f_0} - \alpha_{\text{e2e}}^{x f_0}]^+ = \beta_{\text{e2e}}^{f_0}$	$= \beta_{6,16}$
$D^{f_0}$		$\beta_{\text{e2e}}^{\text{l.o.} f_0} = b^{f_0}$ $6 \cdot [t - 16]^+ = 25$ $t = 20\frac{1}{6}$
$B^{f_0}$		$\alpha^{f_0}(T_{\text{e2e}}^{\text{l.o.} f_0}) = 5 \cdot 16 + 25$ $= 105$

## Tandem \_ 1SC \_ 2Flows \_ 1AC \_ 1Path



- $\beta_{v_0} = \beta_{v_1} = \beta_{R_{v_i}, T_{v_i}} = \beta_{10,10}, i \in \{0,1\}$
- $\alpha^{f_0} = \alpha^{f_1} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}, j \in \{0,1\}$

**Flows**  $f_0, f_1$

TFA results will be equal for all flows as they share the same path of servers.

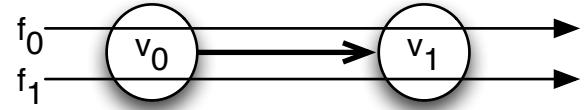
SFA, PMOO results will be equal for all flows as they share the same path of servers and the same arrival curves.

TFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0} = \alpha^{f_0} + \alpha^{f_1}$		$= \gamma_{10,50}$
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}$ $10 \cdot [t - 10]^+ = 50$ $t = 15$	$\beta_{v_0} = \alpha_{v_0}$ $10 \cdot [t - 10]^+ = 10 \cdot t + 50$ $0 \cdot t = 150$ $\Rightarrow D_{v_0}^{f_0} = \infty$
	$B_{v_0}^{f_0}$		$\alpha_{v_0}(T_{v_0}) = 10 \cdot 10 + 50$ $= 150$
$v_0 v_1$	$r_{v_0 v_1}$		$= 10$
	$\alpha_{v_0 v_1} = (\alpha_{v_0})^*$		$\alpha_{v_0}(T_{v_0}) = 150$
	$=$		$= \gamma_{10,150}$
$v_1$	$\alpha_{v_1} = \alpha_{v_0 v_1}$		$= \gamma_{10,150}$
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{v_1}$ $10 \cdot [t - 10]^+ = 150$ $t = 25$	$\beta_{v_1} = \alpha_{v_1}$ $10 \cdot [t - 10]^+ = 10 \cdot t + 150$ $0 \cdot t = 250$ $\Rightarrow D_{v_1}^{f_0} = \infty$
	$B_{v_1}^{f_0}$		$\alpha_{v_1}(T_{v_1}) = 10 \cdot 10 + 150$ $= 250$
$D^{f_0}$		$\sum_{i=0}^1 D_{v_i}^{f_0} = 40$	$\sum_{i=0}^1 D_{v_i}^{f_0} = \infty$
$B^{f_0}$		$\max_{i=\{0,1\}} b_{v_i}^{f_0} = 250$	

SFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0}^{xf_0} = \alpha^{f_1}$		$= \gamma_{5,25}$
	$\beta_{v_0}^{\text{l.o.}, f_0} = [\beta_{v_0} - \alpha_{v_0}^{xf_0}]^+$	$R_{v_0}^{\text{l.o.}, f_0}$	$= 5$
		$T_{v_0}^{\text{l.o.}, f_0}$	$\beta_{v_0} = b_{v_0}^{xf_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$
		$=$	$\beta_{v_0} = \alpha_{v_0}^{xf_0}$ $10 \cdot [t - 10]^+ = 5 \cdot t + 25$ $t = 25$
$v_0 v_1$	$\alpha_{v_0 v_1}^{xf_0}$	$r_{v_0 v_1}^{xf_0}$	$r_{v_0}^{f_1} = r^{f_1} = 5$
		$b_{v_0 v_1}^{xf_0}$	$\alpha_{v_0}^{xf_0}(T_{v_0}) = 5 \cdot 10 + 25$ $= 75$
		$=$	$= \gamma_{5,75}$
$v_1$	$\alpha_{v_1}^{xf_0} = \alpha_{v_0 v_1}^{xf_0}$		$= \gamma_{5,75}$
	$\beta_{v_1}^{\text{l.o.}, f_0} = [\beta_{v_1} - \alpha_{v_1}^{xf_0}]^+$	$R_{v_1}^{\text{l.o.}, f_0}$	$= 5$
		$T_{v_1}^{\text{l.o.}, f_0}$	$\beta_{v_1} = b_{v_1}^{xf_0}$ $10 \cdot [t - 10]^+ = 75$ $t = 17\frac{1}{2}$
		$=$	$\beta_{v_1} = \alpha_{v_1}^{xf_0}$ $10 \cdot [t - 10]^+ = 5 \cdot t + 75$ $t = 35$
	$\beta_{e2e}^{\text{l.o.}, f_0} = \beta_{R_{e2e}^{\text{l.o.}, f_0}, T_{e2e}^{\text{l.o.}, f_0}}$	$\bigotimes_{i=0}^1 \beta_{v_i}^{\text{l.o.}, f_0} = \beta_{5,30}$	$\bigotimes_{i=0}^1 \beta_{v_i}^{\text{l.o.}, f_0} = \beta_{5,60}$
	$D^{f_0}$	$\beta_{e2e}^{\text{l.o.}, f_0} = b^{f_0}$ $5 \cdot [t - 30]^+ = 25$ $t = 35$	$\beta_{e2e}^{\text{l.o.}, f_0} = b^{f_0}$ $5 \cdot [t - 60]^+ = 25$ $t = 65$
	$B^{f_0}$	$\alpha^{f_0}(T_{e2e}^{\text{l.o.}, f_0}) = 5 \cdot 30 + 25$ $= 175$	$\alpha^{f_0}(T_{e2e}^{\text{l.o.}, f_0}) = 5 \cdot 60 + 25$ $= 325$

PMOO		ARB_MUX
e2e	$\beta_{\text{e2e}}^{f_0}$	$\bigotimes_{i=0}^1 \beta_{v_i} = \beta_{10,20}$
	$\alpha_{\text{e2e}}^{xf_0} = \alpha^{f_1}$	$= \gamma_{5,25}$
	$\beta_{\text{e2e}}^{\text{l.o.} f_0} = [\beta_{\text{e2e}}^{f_0} - \alpha_{\text{e2e}}^{xf_0}]^+$	$R_{\text{e2e}}^{\text{l.o.} f_0}$
		$T_{\text{e2e}}^{\text{l.o.} f_0}$
$D^{f_0}$		$\beta_{\text{e2e}}^{\text{l.o.} f_0} = b^{f_0}$ $5 \cdot [t - 45]^+ = 25$ $t = 50$
$B^{f_0}$		$\alpha^{f_0}(T_{\text{e2e}}^{\text{l.o.} f_0}) = 5 \cdot 45 + 25$ $= 250$

## Tandem \_ 2SCs \_ 2Flows \_ 1AC \_ 1Path



- $\beta_{v_0} = \beta_{R_{v_0}, T_{v_0}} = \beta_{10,10}$
- $\beta_{v_1} = \beta_{R_{v_1}, T_{v_1}} = \beta_{6,6}$
- $\alpha^{f_0} = \alpha^{f_1} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{2\frac{1}{2}, 12\frac{1}{2}}, j \in \{0, 1\}$

**Flows**  $f_0, f_1$

TFA results will be equal for all flows as they share the same path of servers.

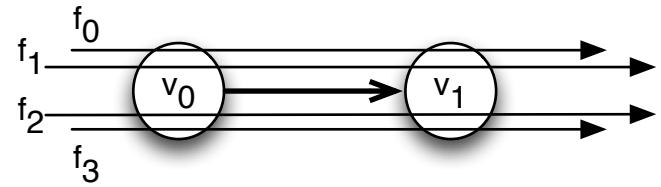
SFA, PMOO results will be equal for all flows as they share the same path of servers and the same arrival curves.

TFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0} = \alpha^{f_0} + \alpha^{f_1}$	$\sum_{j=0}^1 \alpha^{f_j} = \gamma_{5,25}$	
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$	$\beta_{v_0} = \alpha_{v_0}$ $10 \cdot [t - 10]^+ = 5 \cdot t + 25$ $t = 25$
	$B_{v_0}^{f_0}$	$\alpha_{v_0}(T_{v_0}) = 5 \cdot 10 + 25$ = 75	
$v_0 v_1$	$r_{v_0 v_1}$		= 5
	$\alpha_{v_0 v_1} = (\alpha_{v_0})^*$	$b_{v_0 v_1}$	$\alpha_{v_0}(T_{v_0}) = 75$
		=	$= \gamma_{5,75}$
$v_1$	$\alpha_{v_1} = \alpha_{v_0 v_1}$		= $\gamma_{5,75}$
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{v_1}$ $6 \cdot [t - 6]^+ = 75$ $t = 18\frac{1}{2}$	$\beta_{v_1} = \alpha_{v_1}$ $6 \cdot [t - 6]^+ = 5 \cdot t + 75$ $t = 111$
	$B_{v_1}^{f_0}$	$\alpha_{v_1}(T_{v_1}) = 5 \cdot 6 + 75$ = 105	
$D^{f_0}$		$\sum_{i=0}^1 D_{v_i}^{f_0} = 31$	$\sum_{i=0}^1 D_{v_i}^{f_0} = 136$
$B^{f_0}$		$\max_{i=\{0,1\}} b_{v_i}^{f_0} = 105$	

SFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0}^{xf_0} = \alpha^{f_1}$		$= \gamma_{2\frac{1}{2}, 12\frac{1}{2}}$
	$\beta_{v_0}^{\text{l.o.} f_0} = [\beta_{v_0} - \alpha_{v_0}^{xf_0}]^+$	$R_{v_0}^{\text{l.o.} f_0}$	$= 7\frac{1}{2}$
		$T_{v_0}^{\text{l.o.} f_0}$	$\beta_{v_0} = b_{v_0}^{xf_0}$ $10 \cdot [t - 10]^+ = 12\frac{1}{2}$ $t = 11\frac{1}{4}$
			$\beta_{v_0} = \alpha_{v_0}^{xf_0}$ $10 \cdot [t - 10]^+ = 2\frac{1}{2} \cdot t + 12\frac{1}{2}$ $t = 15$
$v_0 v_1$		$r_{v_0 v_1}^{xf_0}$	$= 2\frac{1}{2}$
$v_1$	$\alpha_{v_0 v_1}^{xf_0}$	$b_{v_0 v_1}^{xf_0}$	$\alpha_{v_0}^{xf_0}(T_{v_0}) = 2\frac{1}{2} \cdot 10 + 12\frac{1}{2}$ $= 37\frac{1}{2}$
			$= \gamma_{2\frac{1}{2}, 37\frac{1}{2}}$
$v_1$	$\alpha_{v_1}^{xf_0} = \alpha_{v_0 v_1}^{xf_0}$		$= \gamma_{2\frac{1}{2}, 37\frac{1}{2}}$
	$\beta_{v_1}^{\text{l.o.} f_0} = [\beta_{v_1} - \alpha_{v_1}^{xf_0}]^+$	$R_{v_1}^{\text{l.o.} f_0}$	$= 3\frac{1}{2}$
		$T_{v_1}^{\text{l.o.} f_0}$	$\beta_{v_1} = b_{v_1}^{xf_0}$ $6 \cdot [t - 6]^+ = 37\frac{1}{2}$ $t = 12\frac{1}{4}$
			$\beta_{v_1} = \alpha_{v_1}^{xf_0}$ $6 \cdot [t - 6]^+ = 2\frac{1}{2} \cdot t + 37\frac{1}{2}$ $t = 21$
$D^{f_0}$		$\beta_{e2e}^{\text{l.o.} f_0} = \beta_{R_{e2e}^{\text{l.o.} f_0}, T_{e2e}^{\text{l.o.} f_0}}$	$\bigotimes_{i=0}^1 \beta_{v_i}^{\text{l.o.} f_0} = \beta_{3\frac{1}{2}, 23\frac{1}{2}}$
$B^{f_0}$		$\beta_{e2e}^{\text{l.o.} f_0} = b^{f_0}$	$\bigotimes_{i=0}^1 \beta_{v_i}^{\text{l.o.} f_0} = \beta_{3\frac{1}{2}, 36}$
		$3\frac{1}{2} \cdot [t - 23\frac{1}{2}]^+ = 12\frac{1}{2}$	$\beta_{e2e}^{\text{l.o.} f_0} = b^{f_0}$
		$t = 27\frac{1}{14}$	$3\frac{1}{2} \cdot [t - 36]^+ = 12\frac{1}{2}$ $t = 39\frac{4}{7}$
		$\alpha^{f_0}(T_{e2e}^{\text{l.o.} f_0}) = 2\frac{1}{2} \cdot 23\frac{1}{2} + 12\frac{1}{2}$ $= 71\frac{1}{4}$	$\alpha^{f_0}(T_{e2e}^{\text{l.o.} f_0}) = 2\frac{1}{2} \cdot 36 + 12\frac{1}{2}$ $= 102\frac{1}{2}$

PMOO		ARB_MUX
e2e	$\beta_{\text{e2e}}^{f_0}$	$\bigotimes_{i=0}^1 \beta_{v_i} = \beta_{6,16}$
	$\alpha_{\text{e2e}}^{xf_0} = \alpha^{f_1}$	$= \gamma_{2\frac{1}{2}, 12\frac{1}{2}}$
	$\beta_{\text{e2e}}^{\text{l.o.} f_0} = [\beta_{\text{e2e}}^{f_0} - \alpha_{\text{e2e}}^{xf_0}]^+$	$= 3\frac{1}{2}$
	$R_{\text{e2e}}^{\text{l.o.} f_0}$	$\beta_{\text{e2e}}^{f_0} = \alpha_{\text{e2e}}^{xf_0}$
	$T_{\text{e2e}}^{\text{l.o.} f_0}$	$6 \cdot [t - 16]^+ = 2\frac{1}{2} \cdot t + 12\frac{1}{2}$
	$=$	$t = 31$
$D^{f_0}$		$\beta_{\text{e2e}}^{\text{l.o.} f_0} = b^{f_0}$ $3\frac{1}{2} \cdot [t - 31]^+ = 12\frac{1}{2}$ $t = 34\frac{4}{7}$
$B^{f_0}$		$\alpha^{f_0}(T_{\text{e2e}}^{\text{l.o.} f_0}) = 2\frac{1}{2} \cdot 31 + 12\frac{1}{2}$ $= 90$

## Tandem \_ 1SCs \_ 4Flows \_ 1ACs \_ 1Path



- $\beta_{v_0} = \beta_{v_1} = \beta_{R_{v_i}, T_{v_i}} = \beta_{10,10}, i \in \{0, 1\}$
- $\alpha^{f_i} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{2,10}, j \in \{0, 3\}$

**Flows**  $f_j, j \in \{0, 1, 2, 3\}$

TFA results will be equal for all flows as they share the same path of servers.

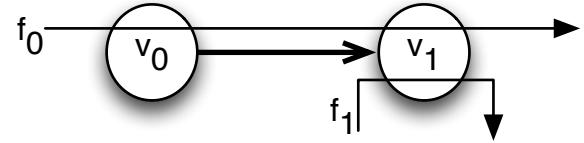
SFA, PMOO results will be equal for all flows as they share the same path of servers and the same arrival curves.

TFA		FIFO_MUX	ARB_MUX	
$v_0$	$\alpha_{v_0} = \sum_{j=0}^3 \alpha^{f_j}$		$= \gamma_{8,40}$	
	$D_{v_0}^{f_j}$	$\beta_{v_0} = b_{v_0}$ $10 \cdot [t - 10]^+ = 40$ $t = 14$	$\beta_{v_0} = \alpha_{v_0}$ $10 \cdot [t - 10]^+ = 8 \cdot t + 40$ $t = 70$	
	$B_{v_0}^{f_j}$	$\alpha_{v_0}(T_{v_0}) = 8 \cdot 10 + 40$ = 120		
$v_0 v_1$	$r_{v_0 v_1}$		= 8	
	$\alpha_{v_0 v_1} = (\alpha_{v_0})^*$	$b_{v_0 v_1}$	$\alpha_{v_0}(T_{v_0}) = 120$	
		=	$= \gamma_{8,120}$	
$v_1$	$\alpha_{v_1} = \alpha_{v_0 v_1}$		= $\gamma_{8,120}$	
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{v_1}$ $10 \cdot [t - 10]^+ = 120$ $t = 22$	$\beta_{v_1} = \alpha_{v_1}$ $10 \cdot [t - 10]^+ = 8 \cdot t + 120$ $t = 110$	
	$B_{v_1}^{f_0}$	$\alpha_{v_1}(T_{v_1}) = 8 \cdot 10 + 120$ = 200		
$D^{f_0}$		$\sum_{i=0}^1 D_{v_i}^{f_j} = 36$	$\sum_{i=0}^1 D_{v_i}^{f_j} = 180$	
$B^{f_0}$		$\max_{i=\{0,1\}} b_{v_i}^{f_j} = 200$		

SFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0}^{xf_j} = \sum_{k=0}^2 \alpha^{f_k}$	$= \gamma_{6,30}$	
	$\beta_{v_0}^{\text{l.o.} f_j} = [\beta_{v_0} - \alpha_{v_0}^{xf_j}]^+$	$= 4$	
	$R_{v_0}^{\text{l.o.} f_j}$	$\beta_{v_0} = b_{v_0}^{xf_j}$ $T_{v_0}^{\text{l.o.} f_j}$ $10 \cdot [t - 10]^+ = 30$ $t = 13$	$\beta_{v_0} = \alpha_{v_0}^{xf_j}$ $10 \cdot [t - 10]^+ = 6 \cdot t + 30$ $t = 32\frac{1}{2}$
	$=$	$= \beta_{4,13}$	$= \beta_{4,32\frac{1}{2}}$
$v_0 v_1$	$\alpha_{v_0 v_1}^{xf_j}$	$r_{v_0 v_1}^{xf_j}$	$= r_{v_0}^{xf_j} = 6$
		$b_{v_0 v_1}^{xf_j}$	$\alpha_{v_0}^{xf_j}(T_{v_0}) = 6 \cdot 10 + 30$ $= 90$
		$=$	$= \gamma_{6,90}$
$v_1$	$\alpha_{v_1}^{xf_j} = \alpha_{v_0 v_1}^{xf_j}$	$= \gamma_{6,90}$	
	$\beta_{v_1}^{\text{l.o.} f_j} = [\beta_{v_1} - \alpha_{v_1}^{xf_j}]^+$	$= 4$	
	$R_{v_1}^{\text{l.o.} f_j}$	$\beta_{v_1} = b_{v_1}^{xf_j}$ $T_{v_1}^{\text{l.o.} f_j}$ $10 \cdot [t - 10]^+ = 90$ $t = 19$	$\beta_{v_1} = \alpha_{v_1}^{xf_j}$ $10 \cdot [t - 10]^+ = 4 \cdot t + 90$ $t = 47\frac{1}{2}$
	$=$	$= \beta_{4,19}$	$= \beta_{4,47\frac{1}{2}}$
$\beta_{e2e}^{\text{l.o.} f_j}$		$\bigotimes_{i=0}^1 \beta_{v_i}^{\text{l.o.} f_j} = \beta_{4,32}$	$\bigotimes_{i=0}^1 \beta_{v_i}^{\text{l.o.} f_j} = \beta_{4,80}$
$D^{f_j}$		$\beta_{e2e}^{\text{l.o.} f_j} = b^{f_j}$ $4 \cdot [t - 32]^+ = 10$ $t = 34\frac{1}{2}$	$\beta_{e2e}^{\text{l.o.} f_j} = b^{f_j}$ $4 \cdot [t - 80]^+ = 10$ $t = 82\frac{1}{2}$
$B^{f_j}$		$\alpha^{f_j}(T_{e2e}^{\text{l.o.} f_j}) = 2 \cdot 32 + 10$ $= 74$	$\alpha^{f_j}(T_{e2e}^{\text{l.o.} f_j}) = 2 \cdot 80 + 10$ $= 170$

PMOO		ARB_MUX
e2e	$\beta_{\text{e2e}}^{f_j}$	$\bigotimes_{i=0}^1 \beta_{v_i} = \beta_{10,20}$
	$\alpha_{\text{e2e}}^{xf_j} = \sum_{j=0}^2 \alpha^{f_j}$	$= \gamma_{6,30}$
	$\beta_{\text{e2e}}^{\text{l.o.} f_j} = [\beta_{\text{e2e}}^{f_j} - \alpha_{\text{e2e}}^{xf_j}]^+$	$R_{\text{e2e}}^{\text{l.o.} f_j} = 4$
	$T_{\text{e2e}}^{\text{l.o.} f_j}$	$\beta_{\text{e2e}}^{f_j} = \alpha_{\text{e2e}}^{xf_j}$ $10 \cdot [t - 20]^+ = 6 \cdot t + 30$ $t = 57\frac{1}{2}$
	$=$	$= \beta_{4,57\frac{1}{2}}$
	$D^{f_j}$	$\beta_{\text{e2e}}^{\text{l.o.} f_j} = b^{f_j}$ $4 \cdot [t - 57\frac{1}{2}]^+ = 10$ $t = 60$
$B^{f_j}$		$\alpha^{f_j}(T_{\text{e2e}}^{\text{l.o.} f_j}) = 2 \cdot 57\frac{1}{2} + 10$ $= 125$

Tandem \_ 1SC \_ 2Flows \_ 1AC \_ 2Paths



- $\beta_{v_0} = \beta_{v_1} = \beta_{R_{v_i}, T_{v_i}} = \beta_{20,20}, i \in \{0,1\}$

- $\alpha^{f_0} = \alpha^{f_1} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}, j \in \{0,1\}$

**Flow  $f_0$**

TFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0} = \alpha^{f_0}$	$= \gamma_{5,25}$	
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b^{f_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$	FIFO per micro flow $\beta_{v_0} = b^{f_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$
	$B_{v_0}^{f_0}$	$\alpha_{v_0}(T_{v_0}) = 5 \cdot 20 + 25 = 125$	
$v_0 v_1$	$r_{v_0 v_1}$	$= 5$	
	$\alpha_{v_0 v_1} = (\alpha_{v_0})^*$	$\alpha_{v_0}(T_{v_0}) = 125$	
	$b_{v_0 v_1}$	$= \gamma_{5,125}$	
$v_1$	$\alpha_{v_1} = \alpha^{f_1} + \alpha_{v_0 v_1}$	$= \gamma_{5,25} + \gamma_{5,125} = \gamma_{10,150}$	
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{v_1}$ $20 \cdot [t - 20]^+ = 150$ $t = 27\frac{1}{2}$	$\beta_{v_1} = \alpha_{v_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 150$ $t = 55$
	$B_{v_1}^{f_0}$	$\alpha_{v_1}(T_{v_1}) = 10 \cdot 20 + 150 = 350$	
$D^{f_0}$		$\sum_{i=0}^1 D_{v_i}^{f_0} = 48\frac{3}{4}$	$\sum_{i=0}^1 D_{v_i}^{f_0} = 76\frac{1}{4}$
$B^{f_0}$		$\max_{i=\{0,1\}} b_{v_i}^{f_0} = 350$	

PMOO and SFA yield the same result because there is no tandem of servers to be convoluted before subtracting common crossflows.

SFA, PMOO		FIFO_MUX (SFA only)	ARB_MUX
$v_0$	$\alpha_{v_0}^{x f_0}$		$= \gamma_{0,0}$
	$\beta_{v_0}^{\text{l.o.} f_0} = \beta_{v_0}$		$= \beta_{20,20}$
$v_0 v_1$	$\alpha_{v_0 v_1}^{x f_0}$		$= \gamma_{0,0}$
$v_1$	$\alpha_{v_1}^{x f_0} = \alpha^{f_1} + \alpha_{v_0 v_1}^{x f_0}$		$= \gamma_{5,25}$
	$\beta_{v_1}^{\text{l.o.} f_0} = [\beta_{v_1} - \alpha_{v_1}^{x f_0}]^+$	$R_{v_1}^{\text{l.o.} f_0}$	$= 15$
		$T_{v_1}^{\text{l.o.} f_0}$	$\beta_{v_1} = b_{v_1}^{x f_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$
		$=$	$\beta_{v_1} = \alpha_{v_1}^{x f_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$
$\beta_{e2e}^{\text{l.o.} f_0} = \beta_{R_{e2e}^{\text{l.o.} f_0}, T_{e2e}^{\text{l.o.} f_0}}$		$\bigotimes_{i=0}^1 \beta_i^{\text{l.o.} f_0} = \beta_{15,41\frac{1}{4}}$	$\bigotimes_{i=0}^1 \beta_i^{\text{l.o.} f_0} = \beta_{15,48\frac{1}{3}}$
$D^{f_0}$		$\beta_{e2e}^{\text{l.o.} f_0} = b^{f_0}$ $15 \cdot [t - 41\frac{1}{4}]^+ = 25$ $t = 42\frac{11}{12}$	$\beta_{e2e}^{\text{l.o.} f_0} = b^{f_0}$ $15 \cdot [t - 48\frac{1}{3}]^+ = 25$ $t = 50$
$B^{f_0}$		$\alpha^{f_0}(T_{e2e}^{\text{l.o.} f_0}) = 5 \cdot 41\frac{1}{4} + 25$ $= 231\frac{1}{4}$	$\alpha^{f_0}(T_{e2e}^{\text{l.o.} f_0}) = 5 \cdot 48\frac{1}{3} + 25$ $= 266\frac{2}{3}$

**Flow**  $f_1$

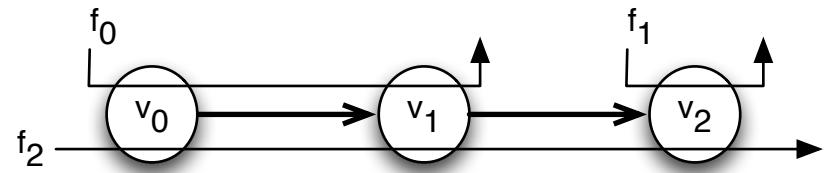
computeOutputBound( $v_0, f_0$ ) = $(\alpha_{v_0}^{f_0})^*$		FIFO_MUX   ARB_MUX
$(\alpha_{v_0}^{f_0})^* = \alpha_{v_0 v_1}^{f_0}$	$r_{v_0 v_1}^{f_0}$	= 5
	$b_{v_0 v_1}^{f_0}$	$\alpha_{v_0}(T_{v_0}) = 125$
	=	= $\gamma_{5,125}$

TFA		FIFO_MUX	ARB_MUX
$v_1$	$\alpha_{v_1} = \alpha^{f_1} + \alpha_{v_0 v_1}^{f_0}$	$= \gamma_{5,25} + \gamma_{5,125} = \gamma_{10,150}$	
	$D_{v_1}^{f_1}$	$\beta_{v_1} = b_{v_1}$ $20 \cdot [t - 20]^+ = 150$ $t = 27\frac{1}{2}$	$\beta_{v_1} = \alpha_{v_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 150$ $t = 55$
	$B_{v_1}^{f_1}$	$\alpha_{v_1}(T_{v_1}) = 10 \cdot 20 + 150$ $= 350$	
	$D^{f_1}$	$\sum_{i=0}^1 D_{v_i}^{f_1} = 27\frac{1}{2}$	$\sum_{i=0}^1 D_{v_i}^{f_1} = 55$
	$B^{f_1}$	$\max_{i=\{0,1\}} b_{v_i}^{f_1} = 350$	

PMOO and SFA yield the same result because there is no tandem of servers to be convoluted before subtracting common crossflows.

SFA, PMOO		FIFO_MUX (SFA only)	ARB_MUX
$v_0 v_1$		$\alpha_{v_0 v_1}^{x f_1}$	$= \gamma_{5,125}$
$v_1$		$\alpha_{v_1}^{x f_1} = \alpha_{v_0 v_1}^{x f_1}$	$= \gamma_{5,125}$
$\beta_{v_1}^{\text{l.o.} f_1} = [\beta_{v_1} - \alpha_{v_1}^{x f_1}]^+ = \beta_{R_{v_1}^{\text{l.o.} f_1}, T_{v_1}^{\text{l.o.} f_1}}$		$R_{v_1}^{\text{l.o.} f_1}$	$= 15$
$T_{v_1}^{\text{l.o.} f_1}$		$\beta_{v_1} = b_{v_1}^{x f_1}$ $20 \cdot [t - 20]^+ = 125$ $t = 26 \frac{1}{4}$	$\beta_{v_1} = \alpha_{v_1}^{x f_1}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 125$ $t = 35$
$=$		$= \beta_{15,26 \frac{1}{4}}$	$= \beta_{15,35}$
$\beta_{e2e}^{\text{l.o.} f_1} = \beta_{R_{e2e}^{\text{l.o.} f_1}, T_{e2e}^{\text{l.o.} f_1}}$		$\bigotimes_{i=0}^1 \beta_{v_i}^{\text{l.o.} f_1} = \beta_{15,26 \frac{1}{4}}$	$\bigotimes_{i=0}^1 \beta_{v_i}^{\text{l.o.} f_1} = \beta_{15,35}$
$D^{f_1}$		$\beta_{e2e}^{\text{l.o.} f_1} = b^{f_1}$ $15 \cdot [t - 26 \frac{1}{4}]^+ = 25$ $t = 27 \frac{11}{12}$	$\beta_{e2e}^{\text{l.o.} f_1} = b^{f_1}$ $15 \cdot [t - 35]^+ = 25$ $t = 36 \frac{2}{3}$
$B^{f_1}$		$\alpha^{f_1}(T_{e2e}^{\text{l.o.} f_1}) = 5 \cdot 26 \frac{1}{4} + 25$ $= 156 \frac{1}{4}$	$\alpha^{f_1}(T_{e2e}^{\text{l.o.} f_1}) = 5 \cdot 35 + 25$ $= 200$

### Tandem \_1SC \_3Flows \_1AC \_3Paths



- $\beta_{v_0} = \beta_{v_1} = \beta_{v_2} = \beta_{R_{v_i}, T_{v_i}} = \beta_{20,20}$ ,  $i \in \{0, 1, 2\}$
- $\alpha^{f_0} = \alpha^{f_1} = \alpha^{f_2} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}$ ,  $j \in \{0, 1, 2\}$

**Flow  $f_0$  (comparable to Tandem \_1SC \_2Flows \_1AC \_1Path)**

TFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0} = \alpha^{f_0} + \alpha^{f_1}$		$= \gamma_{10,50}$
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}$ $20 \cdot [t - 20]^+ = 50$ $t = 22\frac{1}{2}$	$\beta_{v_0} = \alpha_{v_0}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 50$ $t = 45$
	$B_{v_0}^{f_0}$	$\alpha_{v_0}(T_{v_0}) = 20 \cdot 10 + 50$ = 250	
$v_0 v_1$	$\alpha_{v_0 v_1} = (\alpha_{v_0})^*$	$r_{v_0 v_1}$ $\bar{b}_{v_0 v_1}$ =	= 10 $\alpha_{v_0}(T_{v_0}) = 250$ $= \gamma_{10,250}$
	$\alpha_{v_1} = \alpha_{v_0 v_1}$		$= \gamma_{10,250}$
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{v_1}$ $20 \cdot [t - 20]^+ = 250$ $t = 32\frac{1}{2}$	$\beta_{v_1} = \alpha_{v_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 250$ $t = 65$
$B_{v_1}^{f_0}$		$\alpha_{v_1}(T_{v_1}) = 10 \cdot 20 + 250$ = 450	
$D^{f_0}$		$\sum_{i=0}^1 D_{v_i}^{f_0} = 55$	$\sum_{i=0}^1 D_{v_i}^{f_0} = 110$
$B^{f_0}$		$\max_{i=\{0,1\}} b_{v_i}^{f_0} = 450$	

SFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0}^{x f_0} = \alpha^{f_2}$	$R_{v_0}^{\text{l.o.} f_0}$	$= \gamma_{5,25}$
	$\beta_{v_0}^{\text{l.o.} f_0} = [\beta_{v_0} - \alpha_{v_0}^{x f_0}]^+$	$T_{v_0}^{\text{l.o.} f_0}$	$= 5$
			$\beta_{v_0} = b_{v_0}^{x f_0}$
			$20 \cdot [t - 20]^+ = 25$
$v_0 v_1$	$\alpha_{v_0 v_1}^{x f_0} = \alpha_{v_0}^{x f_0} \oslash \beta_{v_0} = \alpha^{f_2} \oslash \beta_{v_0}$ (This is computeSfaOutputBound)	$t = 21\frac{1}{4}$	$20 \cdot [t - 20]^+ = 5 \cdot t + 25$
		$= \beta_{15,21\frac{1}{4}}$	$t = 28\frac{1}{3}$
		$r_{v_0 v_1}^{x f_0}$	$= 5$
		$b_{v_0 v_1}^{x f_0}$	$\alpha_{v_0}^{x f_0}(T_{v_0}) = 5 \cdot 20 + 25$
$v_1$	$\alpha_{v_1}^{x f_0} = \alpha_{v_0 v_1}^{x f_0}$	$R_{v_1}^{\text{l.o.} f_0}$	$= \gamma_{5,125}$
	$\beta_{v_1}^{\text{l.o.} f_0} = [\beta_{v_1} - \alpha_{v_1}^{x f_0}]^+$	$T_{v_1}^{\text{l.o.} f_0}$	$= 15$
			$\beta_{v_1} = b_{v_1}^{x f_0}$
			$20 \cdot [t - 20]^+ = 125$
	$\beta_{e2e}^{1.o.f_0} = \beta_{R_{e2e}^{\text{l.o.} f_0}, T_{e2e}^{\text{l.o.} f_0}}$	$t = 26\frac{1}{4}$	$20 \cdot [t - 20]^+ = 5 \cdot t + 125$
		$= \beta_{15,26\frac{1}{4}}$	$t = 35$
		$\otimes_{i=0}^1 \beta_{v_i}^{\text{l.o.} f_0} = \beta_{15,47\frac{1}{2}}$	$\otimes_{i=0}^1 \beta_{v_i}^{\text{l.o.} f_0} = \beta_{15,63\frac{1}{3}}$
		$\beta_{e2e}^{\text{l.o.} f_0} = b^{f_0}$	$\beta_{e2e}^{\text{l.o.} f_0} = b^{f_0}$
	$D^{f_0}$	$15 \cdot [t - 47\frac{1}{2}]^+ = 25$	$15 \cdot [t - 63\frac{1}{3}]^+ = 25$
		$t = 49\frac{1}{6}$	$t = 65$
		$\alpha^{f_0}(T_{e2e}^{\text{l.o.} f_0}) = 5 \cdot 47\frac{1}{2} + 25$	$\alpha^{f_0}(T_{e2e}^{\text{l.o.} f_0}) = 5 \cdot 63\frac{1}{3} + 25$
		$= 262\frac{1}{2}$	$= 341\frac{2}{3}$

PMOO		ARB_MUX
e2e	$\beta_{\text{e2e}}^{f_0}$	$\bigotimes_{i=0}^1 \beta_{v_i} = \beta_{20,40}$
	$\alpha_{\text{e2e}}^{xf_0} = \alpha^{f_2}$	$= \gamma_{5,25}$
	$\beta_{\text{e2e}}^{\text{l.o.} f_0} = [\beta_{\text{e2e}}^{f_0} - \alpha_{\text{e2e}}^{xf_0}]^+$	$R_{\text{e2e}}^{\text{l.o.} f_0}$
		$T_{\text{e2e}}^{\text{l.o.} f_0}$
		$=$
$D^{f_0}$		$\beta_{\text{e2e}}^{\text{l.o.} f_0} = b^{f_0}$ $15 \cdot [t - 55]^+ = 25$ $t = 56\frac{2}{3}$
$B^{f_0}$		$\alpha^{f_0}(T_{\text{e2e}}^{\text{l.o.} f_0}) = 5 \cdot 55 + 25$ $= 300$

**Flow  $f_1$  (comparable with Node \_2Flows \_2ACs)**

computeOutputBound( $v_0, f_2$ ) = $(\alpha_{v_0}^{f_2})^*$	FIFO_MUX	ARB_MUX
$\beta_{v_0}^{l.o.f_2} = [\beta_{v_0} - \alpha^{xf_2}]^+ = [\beta_{v_0} - \alpha^{f_0}]^+ = \beta_{R_{v_0}^{l.o.f_2}, T_{v_0}^{l.o.f_2}}$	$R_{v_0}^{l.o.f_2}$ $T_{v_0}^{l.o.f_2}$ =	= 15 $\beta_{v_0} = b_{v_0}^{f_2}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$ $= \beta_{15, 21\frac{1}{4}}$ = 5 $\alpha^{f_2}(T_{v_0}^{l.o.f_2}) = 131\frac{1}{4}$ $= \gamma_{5, 131\frac{1}{4}}$
$(\alpha_{v_0}^{f_2})^* = \alpha_{v_0 v_1}^{f_2} = \alpha^{f_2} \oslash \beta_{v_0}^{l.o.f_2}$	$r_{v_0 v_1}^{f_2}$ $b_{v_0 v_1}^{f_2}$ =	$\beta_{v_0} = \alpha_{v_0}^{f_2}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$ $= \beta_{15, 28\frac{1}{3}}$ = 5 $\alpha^{f_2}(T_{v_0}^{l.o.f_2}) = 166\frac{2}{3}$ $= \gamma_{5, 166\frac{2}{3}}$
computeOutputBound( $v_0, f_0 = (\alpha_{v_0}^{f_0})^*$ $(\alpha_{v_0}^{f_0})^* = (\alpha_{v_0}^{f_2})^*$	FIFO_MUX	ARB_MUX
computeOutputBound( $v_1, f_2$ ) = $(\alpha_{v_1}^{f_2})^*$	FIFO_MUX	ARB_MUX
$\beta_{v_1}^{l.o.f_2} = [\beta_{v_1} - \alpha_{v_1}^{xf_2}]^+ = [\beta_{v_1} - (\alpha_{v_0}^{f_0})^*]^+ = \beta_{R_{v_1}^{l.o.f_2}, T_{v_1}^{l.o.f_2}}$	$R_{v_1}^{l.o.f_2}$ $T_{v_1}^{l.o.f_2}$ =	= 15 $\beta_{v_1} = b_{v_0 v_1}^{f_0}$ $20 \cdot [t - 20]^+ = 131\frac{1}{4}$ $t = 26\frac{9}{16}$ $= \beta_{15, 26\frac{9}{16}}$ = 5 $\alpha_{v_0}^{f_2}(T_{v_1}^{l.o.f_2}) = 264\frac{1}{16}$ $= \gamma_{5, 264\frac{1}{16}}$
$(\alpha_{v_1}^{f_2})^* = \alpha_{v_1 v_2}^{f_2} = (\alpha_{v_0}^{f_2})^* \oslash \beta_{v_1}^{l.o.f_2}$	$r_{v_1 v_2}^{f_2}$ $b_{v_1 v_2}^{f_2}$ =	$\beta_{v_1} = \alpha_{v_0 v_1}^{f_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 166\frac{2}{3}$ $t = 37\frac{7}{9}$ $= \beta_{15, 37\frac{7}{9}}$ = 5 $(\alpha_{v_0}^{f_2})^*(T_{v_1}^{l.o.f_2}) = 355\frac{5}{9}$ $= \gamma_{5, 355\frac{5}{9}}$

TFA		FIFO_MUX	ARB_MUX
$v_2$	$\alpha_{v_2} = \alpha^{f_1} + \alpha_{v_1 v_2}^{f_2}$	$\gamma_{5,25} + \gamma_{5,264\frac{1}{16}} = \gamma_{10,289\frac{1}{16}}$ $\beta_{v_2} = b_{v_2}$ $D_{v_2}^{f_1}$ $20 \cdot [t - 20]^+ = 289\frac{1}{16}$ $t = 34\frac{29}{64}$	$\gamma_{5,25} + \gamma_{5,355\frac{5}{9}} = \gamma_{10,380\frac{5}{9}}$ $\beta_{v_2} = \alpha_{v_2}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 380\frac{5}{9}$ $t = 78\frac{5}{90}$
	$B_{v_2}^{f_1}$	$\alpha_{v_2}(T_{v_2}) = 10 \cdot 20 + 289\frac{1}{16}$ $= 489\frac{1}{16}$	$\alpha_{v_2}(T_{v_2}) = 10 \cdot 20 + 380\frac{5}{9}$ $= 580\frac{5}{9}$
	$D^{f_1}$	$= 34\frac{29}{64}$	$= 78\frac{5}{90}$
	$B^{f_1}$	$= 489\frac{1}{16}$	$= 580\frac{5}{9}$

SFA		FIFO_MUX	ARB_MUX
$v_2$	$\beta_{v_2}^{\text{l.o.}f_1} = [\beta_{v_2} - \alpha_{v_2}^{xf_1}]^+ = [\beta_{v_2} - \alpha_{v_1 v_2}^{f_2}]^+$	$R_{v_2}^{\text{l.o.}f_1}$	$= R_{v_2} - r_{v_1 v_2}^{f_2} = 15$
		$\beta_{v_1} = b_{v_1 v_2}^{f_2}$	$\beta_{v_1} = \alpha_{v_1 v_2}^{f_2}$
		$20 \cdot [t - 20]^+ = 264 \frac{1}{16}$	$20 \cdot [t - 20]^+ = 5 \cdot t + 355 \frac{5}{9}$
		$t = 33 \frac{13}{64}$	$t = 50 \frac{10}{27}$
$\beta_{\text{e2e}}^{\text{l.o.}f_1} = \beta_{v_2}^{\text{l.o.}f_1}$		$= \beta_{15,33 \frac{13}{64}}$	$= \beta_{15,50 \frac{10}{27}}$
$D^{f_1}$		$\beta_{v_2}^{\text{l.o.}f_1} = b^{f_1}$	$\beta_{v_2}^{\text{l.o.}f_1} = b^{f_1}$
		$15 \cdot [t - 33 \frac{13}{64}]^+ = 25$	$15 \cdot [t - 50 \frac{10}{27}]^+ = 25$
		$t = 34 \frac{167}{192}$	$t = 52 \frac{1}{27}$
$B^{f_1}$		$\alpha^{f_1}(T_{v_2}^{\text{l.o.}f_1}) = 5 \cdot 33 \frac{13}{64} + 25 = 191 \frac{1}{64}$	$\alpha^{f_1}(T_{\text{e2e}}^{\text{l.o.}f_1}) = 5 \cdot 50 \frac{10}{27} + 25 = 276 \frac{23}{27}$

A recursive SFA calculation using  $f_2$ 's SFA left-over service curve to calculate  $\alpha_{v_1 v_2}^{f_2}$  yields slightly tighter bounds, however, it is not implemented in the DISCO Network Calculator yet.

SFA		FIFO_MUX	ARB_MUX
$v_1 v_2$	$\beta_{v_0 v_1}^{\text{l.o.} f_0} = \beta_{\text{e2e}}^{\text{l.o.} f_0}$ (see SFA for $f_0$ above)	$= \beta_{15,47\frac{1}{2}}$	$= \beta_{15,63\frac{1}{3}}$
	$\alpha_{v_1 v_2}^{x f_1} = \alpha^{f_2} \oslash \beta_{\text{e2e}}^{\text{l.o.} f_0}$	$r_{v_1 v_2}^{x f_1}$ $b_{v_1 v_2}^{x f_1}$ =	$= r^{f_2} = 5$ $\alpha^{f_2}(T_{v_0 v_1}^{\text{l.o.} f_0}) = 5 \cdot 47\frac{1}{2} + 25$ $= 262\frac{1}{2}$ $= \gamma_{5,262\frac{1}{2}}$ $\alpha^{f_2}(T_{v_0 v_1}^{\text{l.o.} f_0}) = 5 \cdot 63\frac{1}{3} + 25$ $= 341\frac{2}{3}$ $= \gamma_{5,341\frac{2}{3}}$
	$\alpha_{v_2}^{x f_1} = \alpha_{v_1 v_2}^{x f_1}$	$R_{v_2}^{\text{l.o.} f_1}$	$= \gamma_{5,262\frac{1}{2}}$ $= 15$
	$\beta_{v_2}^{\text{l.o.} f_1} = [\beta_{v_2} - \alpha_{v_2}^{x f_1}]^+ = [\beta_{v_2} - \alpha_{v_1 v_2}^{x f_1}]^+$	$\beta_{v_2} = b_{v_2}^{x f_1}$ $T_{v_2}^{\text{l.o.} f_1}$ $t = 33\frac{1}{8}$ =	$\beta_{v_2} = \alpha_{v_2}^{x f_1}$ $20 \cdot [t - 20]^+ = 262\frac{1}{2}$ $t = 49\frac{4}{9}$ $= \beta_{15,33\frac{1}{8}}$ $= \beta_{15,49\frac{4}{9}}$
$\beta_{\text{e2e}}^{\text{l.o.} f_1} = \beta_{v_2}^{\text{l.o.} f_1}$		$= \beta_{15,33\frac{1}{8}}$	$= \beta_{15,49\frac{4}{9}}$
$D^{f_1}$		$\beta_{\text{e2e}}^{\text{l.o.} f_1} = b^{f_1}$ $15 \cdot [t - 33\frac{1}{8}]^+ = 25$ $t = 34\frac{19}{24}$	$\beta_{\text{e2e}}^{\text{l.o.} f_1} = b^{f_1}$ $15 \cdot [t - 49\frac{4}{9}]^+ = 25$ $t = 51\frac{1}{9}$
$B^{f_1}$		$\alpha^{f_1}(T_{\text{e2e}}^{\text{l.o.} f_1}) = 5 \cdot 33\frac{1}{8} + 25$ $= 190\frac{5}{8}$	$\alpha^{f_1}(T_{\text{e2e}}^{\text{l.o.} f_1}) = 5 \cdot 49\frac{4}{9} + 25$ $= 272\frac{2}{9}$

In contrast to the SFA, the PMOO analysis calculates output bounds needed to abstract the topology to a tandem recursively.

PMOO		ARB_MUX
$v_1 v_2$	$\beta_{v_0 v_1}^{\text{l.o.} f_2} = \beta_{\text{e2e}}^{\text{l.o.} f_0}$ (compare with PMOO for $f_0$ above)	$= \beta_{15,55}$
	$\alpha_{v_1 v_2}^{x f_1} = \alpha^{f_2} \oslash \beta_{v_0 v_1}^{\text{l.o.} f_2}$	$r_{v_1 v_2}^{x f_1} = 5$
		$b_{v_1 v_2}^{x f_1} = \alpha^{f_2}(T_{v_0 v_1}^{\text{l.o.} f_0}) = 5 \cdot 55 + 25$
		$= 300$
$v_2$	$\alpha_{v_2}^{x f_1} = \alpha_{v_1 v_2}^{x f_1}$	$= \gamma_{5,300}$
	$\beta_{v_2}^{\text{l.o.} f_1} = [\beta_{v_2} - \alpha_{v_2}^{x f_1}]^+ = [\beta_{v_2} - \alpha_{v_1 v_2}^{x f_1}]^+$	$R_{v_2}^{\text{l.o.} f_1} = 15$
		$\beta_{v_2} = \alpha_{v_2}^{x f_1}$
		$T_{v_2}^{\text{l.o.} f_1} = 20 \cdot [t - 20]^+ = 5 \cdot t + 300$
		$t = 46\frac{2}{3}$
		$= \beta_{15,46\frac{2}{3}}$
	$\beta_{\text{e2e}}^{\text{l.o.} f_1} = \beta_{v_2}^{\text{l.o.} f_1}$	$= \beta_{15,46\frac{2}{3}}$
	$D^{f_1}$	$\beta_{\text{e2e}}^{\text{l.o.} f_1} = b^{f_1}$
		$15 \cdot [t - 46\frac{2}{3}]^+ = 25$
$B^{f_1}$		$t = 48\frac{1}{3}$
		$\alpha^{f_1}(T_{\text{e2e}}^{\text{l.o.} f_1}) = 5 \cdot 46\frac{2}{3} + 25$
		$= 258\frac{1}{3}$

### Flow $f_2$

TFA bounds for flow  $f_2$  can be calculated from the results for  $f_0$  and  $f_2$ , although that is not the way the DISCO Network Calculator retrieves the bounds. Here's potential for the Network Calculator to increase performance by reusing cached results.

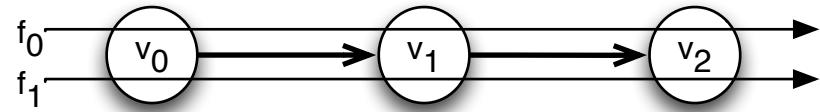
TFA	FIFO_MUX	ARB_MUX
$D^{f_2} = D^{f_0} + D^{f_1}$	$55 + 34\frac{29}{64} = 89\frac{29}{64}$	$110 + 78\frac{5}{90} = 188\frac{5}{90}$
$B^{f_2} = \max\{B^{f_0}, B^{f_1}\}$	$\max\{450, 489\frac{1}{16}\} = 489\frac{1}{16}$	$\max\{450, 508\frac{5}{9}\} = 508\frac{5}{9}$

Although SFA does not recursively calculate the necessary output bounds, it yields the right result if there's no cross traffic coming from outside the flow of interest's path.

SFA			FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0}^{xf_2} = \alpha^{f_0}$	$R_{v_0}^{\text{l.o.} f_2}$	$= \gamma_{5,25}$	
	$\beta_{v_0}^{\text{l.o.} f_2} = [\beta_{v_0} - \alpha_{v_0}^{xf_2}]^+ = [\beta_{v_0} - \alpha_{v_0}^{f_0}]^+$	$T_{v_0}^{\text{l.o.} f_2}$	$= 5$	
			$\beta_{v_0} = b_{v_0}^{xf_2}$	$\beta_{v_0} = \alpha_{v_0}^{xf_2}$
			$20 \cdot [t - 20]^+ = 25$	$20 \cdot [t - 20]^+ = 5 \cdot t + 25$
$v_0 v_1$	$\alpha_{v_0 v_1}^{xf_2} = \alpha_{v_0}^{xf_2} \oslash \beta_{v_0} = \alpha^{f_0} \oslash \beta_{v_0}$ (This is computeSfaOuputBound)	$T_{v_0}^{\text{l.o.} f_2}$	$t = 21\frac{1}{4}$	$t = 28\frac{1}{3}$
		$=$	$= \beta_{15,21\frac{1}{4}}$	$= \beta_{15,28\frac{1}{3}}$
		$r_{v_0 v_1}^{xf_2}$	$= 5$	
$v_1$	$\alpha_{v_1}^{xf_2} = \alpha_{v_0 v_1}^{xf_2}$	$b_{v_0 v_1}^{xf_2}$	$\alpha_{v_0}^{xf_2}(T_{v_0}) = 5 \cdot 20 + 25$	
		$=$	$= 125$	
		$=$	$= \gamma_{5,125}$	
		$R_{v_1}^{\text{l.o.} f_2}$	$= \gamma_{5,125}$	
$v_1 v_2$	$\alpha_{v_1 v_2}^{xf_2}$ (This is computeSfaOuputBound)	$T_{v_1}^{\text{l.o.} f_2}$	$= 15$	
		$=$	$= \beta_{15,26\frac{1}{4}}$	$= \beta_{15,35}$
		$=$	$= \gamma_{0,0}$	
		$=$	$= \gamma_{5,25}$	
$v_2$	$\alpha_{v_2}^{xf_2} = \alpha^{f_1} + \alpha_{v_1 v_2}^{xf_2}$	$R_{v_2}^{\text{l.o.} f_2}$	$= 15$	
		$T_{v_2}^{\text{l.o.} f_2}$	$\beta_{v_2} = b_{v_2}^{xf_2}$	$\beta_{v_2} = \alpha_{v_2}^{xf_2}$
		$=$	$20 \cdot [t - 20]^+ = 25$	$20 \cdot [t - 20]^+ = 5 \cdot t + 25$
		$=$	$t = 21\frac{1}{4}$	$t = 28\frac{1}{3}$
	$\beta_{e2e}^{\text{l.o.} f_2}$	$=$	$= \beta_{15,21\frac{1}{4}}$	$= \beta_{15,28\frac{1}{3}}$
		$\otimes_{i=0}^2 \beta_{v_i}^{\text{l.o.} f_2} = \beta_{15,68\frac{3}{4}}$	$\otimes_{i=0}^2 \beta_{v_i}^{\text{l.o.} f_0} = \beta_{15,91\frac{2}{3}}$	
		$\beta_{e2e}^{\text{l.o.} f_2} = b^{f_2}$	$\beta_{e2e}^{\text{l.o.} f_2} = b^{f_2}$	
		$15 \cdot [t - 68\frac{3}{4}]^+ = 25$	$15 \cdot [t - 91\frac{2}{3}]^+ = 25$	
	$D^{f_2}$	$t = 70\frac{5}{12}$	$t = 93\frac{1}{3}$	
		$\alpha^{f_2}(T_{v_2}^{\text{l.o.} f_2}) = 5 \cdot 68\frac{3}{4} + 25$	$\alpha^{f_2}(T_{e2e}^{\text{l.o.} f_2}) = 5 \cdot 91\frac{2}{3} + 25$	
		$= 368\frac{3}{4}$	$= 483\frac{1}{3}$	
	$B^{f_2}$			

PMOO		ARB_MUX
$v_0 v_1$	$\beta_{v_0 v_1}^{\text{l.o.} f_2} = \beta_{\text{e2e}}^{\text{l.o.} f_0}$	$= \beta_{15,55}$
$v_2$	$\beta_{\text{e2e}}^{\text{l.o.} f_2} = \beta_{v_2}^{\text{l.o.} f_1}$	$= \beta_{15,28\frac{1}{3}}$
$\beta_{\text{e2e}}^{\text{l.o.} f_2} = \beta_{\text{e2e}}^{\text{l.o.} f_0} \otimes \beta_{v_2}^{\text{l.o.} f_1}$	$= \beta_{15,55} \otimes \beta_{15,28\frac{1}{3}} = \beta_{15,83\frac{1}{3}}$	$\beta_{\text{e2e}}^{\text{l.o.} f_2} = b^{f_1}$
$D^{f_2}$	$15 \cdot [t - 83\frac{1}{3}] = 25$	$t = 85$
$B^{f_2}$	$\alpha^{f_0}(T_{\text{e2e}}^{\text{l.o.} f_0}) = 5 \cdot 83\frac{1}{3} + 25$ $= 441\frac{2}{3}$	

## Tandem \_ 1SC \_ 2Flows \_ 1AC \_ 1Path \_ v2



- $\beta_{v_0} = \beta_{v_1} = \beta_{v_2} = \beta_{R_{v_i}, T_{v_i}} = \beta_{20,20}$ ,  $i \in \{0, 1\}$
- $\alpha^{f_0} = \alpha^{f_1} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}$ ,  $j \in \{0, 1\}$

**Flows**  $f_0$ ,  $f_1$

TFA results will be equal for all flows as they share the same path of servers.

SFA, PMOO results will be equal for all flows as they share the same path of servers and the same arrival curves.

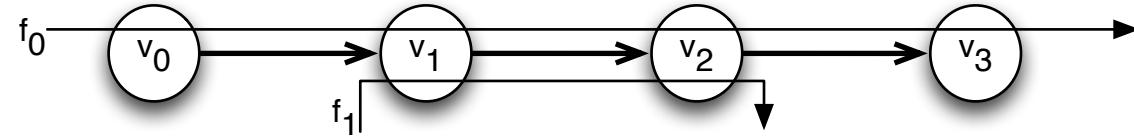
Here you see the third parameter's magic. It enables calculating the output bound for an aggregate.

TFA		FIFO_MUX		ARB_MUX		
$v_0$	$\alpha_{v_0} = \alpha^{f_0} + \alpha^{f_1}$	$= \gamma_{10,50}$				
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}$ $20 \cdot [t - 20]^+ = 50$ $t = 22\frac{1}{2}$	$\beta_{v_0} = \alpha_{v_0}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 50$ $t = 45$			
	$B_{v_0}^{f_0}$	$\alpha_{v_0}(T_{v_0}) = 10 \cdot 20 + 50$ $= 250$				
$v_0 v_1$	$\alpha_{v_0 v_1} = (\alpha_{v_0})^*$	$r_{v_0 v_1}$	$= 10$			
		$b_{v_0 v_1}$	$\alpha_{v_0}(T_{v_0}) = 250$			
		$=$	$= \gamma_{10,250}$			
$v_1$	$\alpha_{v_1} = \alpha_{v_0 v_1}$		$= \gamma_{10,250}$			
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{v_1}$ $20 \cdot [t - 20]^+ = 250$ $t = 32\frac{1}{2}$	$\beta_{v_1} = \alpha_{v_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 250$ $t = 65$			
		$\alpha_{v_1}(T_{v_1}) = 10 \cdot 20 + 250$ $= 450$				
$v_1 v_2$	$\alpha_{v_1 v_2} = (\alpha_{v_1})^*$	$r_{v_1 v_2}$	$= 10$			
		$b_{v_1 v_2}$	$\alpha_{v_1}(T_{v_1}) = 450$			
		$=$	$= \gamma_{10,450}$			
$v_2$	$\alpha_{v_2}^{f_0} = \alpha_{v_1 v_2}$		$= \gamma_{10,450}$			
	$D_{v_2}^{f_0}$	$\beta_{v_2} = b_{v_2}$ $20 \cdot [t - 20]^+ = 450$ $t = 42\frac{1}{2}$	$\beta_{v_2} = \alpha_{v_2}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 450$ $t = 85$			
		$\alpha_{v_1}(T_{v_1}) = 10 \cdot 20 + 450$ $= 650$				
$D^{f_0}$		$\sum_{i=0}^2 D_{v_i}^{f_0} = 97\frac{1}{2}$	$\sum_{i=0}^2 D_{v_i}^{f_0} = 195$			
$B^{f_0}$		$\max_{i=\{0,1,2\}} b_{v_i}^{f_0} = 650$				

SFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0}^{xf_0} = \alpha^{f_1}$	$R_{v_0}^{l.o.f_0}$	$= \gamma_{5,25}$ $= 15$
	$\beta_{v_0}^{l.o.f_0} = [\beta_{v_0} - \alpha_{v_0}^{xf_0}]^+ = \beta_{R_{v_0}^{l.o.f_0}, T_{v_0}^{l.o.f_0}}$	$T_{v_0}^{l.o.f_0}$	$\beta_{v_0} = b_{v_0}^{xf_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 22\frac{1}{4}$ $= \beta_{15,21\frac{1}{4}}$
			$\beta_{v_0} = \alpha_{v_0}^{xf_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$ $= \beta_{15,28\frac{1}{3}}$
$v_0v_1$	$\alpha_{v_0v_1}^{xf_0} = (\alpha_{v_0}^{xf_0})^*$	$r_{v_0v_1}^{xf_0}$	$= 5$
		$b_{v_0v_1}^{xf_0}$	$\alpha_{v_0}^{xf_0}(T_{v_0}) = 5 \cdot 20 + 25$ $= 125$
			$= \gamma_{5,125}$
$v_1$	$\alpha_{v_1}^{xf_0} = \alpha_{v_0v_1}^{xf_0}$	$R_{v_1}^{l.o.f_0}$	$= \gamma_{5,125}$ $= 15$
	$\beta_{v_1}^{l.o.f_0} = [\beta_{v_1} - \alpha_{v_1}^{xf_0}]^+$	$T_{v_1}^{l.o.f_0}$	$\beta_{v_1} = b_{v_1}^{xf_0}$ $20 \cdot [t - 20]^+ = 125$ $t = 26\frac{1}{4}$ $= \beta_{15,26\frac{1}{4}}$
			$\beta_{v_1} = \alpha_{v_1}^{xf_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 125$ $t = 35$ $= \beta_{15,35}$
$v_1v_2$	$\alpha_{v_1v_2}^{xf_0} = (\alpha_{v_1}^{xf_0})^*$	$r_{v_1v_2}^{xf_0}$	$= 5$
		$b_{v_1v_2}^{xf_0}$	$\alpha_{v_1}^{xf_0}(T_{v_1}) = 5 \cdot 20 + 125$ $= 225$
			$= \gamma_{5,225}$
$v_2$	$\alpha_{v_2}^{xf_0} = \alpha_{v_1v_2}^{xf_0}$	$R_{v_2}^{l.o.f_0}$	$= \gamma_{5,225}$ $= 15$
	$\beta_{v_2}^{l.o.f_0} = [\beta_{v_2} - \alpha_{v_2}^{xf_0}]^+$	$T_{v_2}^{l.o.f_0}$	$\beta_{v_2} = b_{v_2}^{xf_0}$ $20 \cdot [t - 20]^+ = 225$ $t = 31\frac{1}{4}$ $= \beta_{15,31\frac{1}{4}}$
			$\beta_{v_2} = \alpha_{v_2}^{xf_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 225$ $t = 41\frac{2}{3}$ $= \beta_{15,41\frac{2}{3}}$
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$		$\bigotimes_{i=0}^2 \beta_{v_i}^{l.o.f_0} = \beta_{5,78\frac{3}{4}}$	$\bigotimes_{i=0}^2 \beta_{v_i}^{l.o.f_0} = \beta_{5,105}$
$D^{f_0}$		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $15 \cdot [t - 78\frac{3}{4}]^+ = 25$ $t = 80\frac{5}{12}$	$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $15 \cdot [t - 105]^+ = 25$ $t = 106\frac{2}{3}$
$B^{f_0}$		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 78\frac{3}{4} + 25$ $= 418\frac{3}{4}$	$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 105 + 25$ $= 550$

PMOO		ARB_MUX
e2e	$\beta_{\text{e2e}}^{f_0}$	$\bigotimes_{i=0}^2 \beta_{v_i} = \beta_{20,60}$
	$\alpha_{\text{e2e}}^{xf_0} = \alpha^{f_1}$	$= \gamma_{5,25}$
	$\beta_{\text{e2e}}^{\text{l.o.} f_0} = [\beta_{\text{e2e}}^{f_0} - \alpha_{\text{e2e}}^{xf_0}]^+$	$R_{\text{e2e}}^{\text{l.o.} f_0}$
		$= 15$
		$\beta_{\text{e2e}}^{f_0} = \alpha_{\text{e2e}}^{xf_0}$
		$20 \cdot [t - 60]^+ = 5 \cdot t + 25$
		$t = 81\frac{2}{3}$
		$= \beta_{15,81\frac{2}{3}}$
$D^{f_0}$		$\beta_{\text{e2e}}^{\text{l.o.} f_0} = b^{f_0}$
		$15 \cdot [t - 81\frac{2}{3}]^+ = 25$
		$t = 83\frac{1}{3}$
$B^{f_0}$		$\alpha^{f_0}(T_{\text{e2e}}^{\text{l.o.} f_0}) = 5 \cdot 81\frac{2}{3} + 25$
		$= 433\frac{1}{3}$

## Tandem \_ 1SC \_ 2Flows \_ 1AC \_ 2Path \_ v2



- $\beta_{v_0} = \beta_{v_1} = \beta_{v_2} = \beta_{v_3} = \beta_{R_{v_i}, T_{v_i}} = \beta_{20,20}, i \in \{0, 1\}$
- $\alpha^{f_0} = \alpha^{f_1} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}, j \in \{0, 1\}$

computeOutputBound( $v_0, f_0$ ) = $(\alpha_{v_0}^{f_0})^* = \alpha_{v_0 v_1}^{f_0}$	FIFO_MUX	ARB_MUX
$\alpha_{v_0}^{x f_0}$	$= \gamma_{0,0}$	
$\beta_{v_0}^{\text{l.o.} f_0} = [\beta_{v_0} - \alpha_{v_0}^{x f_0}]^+ = \beta_{v_0}$	$= \beta_{20,20}$	
$\alpha_{v_0 v_1}^{f_0} = \alpha^{f_0} \oslash \beta_{v_0}^{\text{l.o.} f_0} = \alpha^{f_0} \oslash \beta_{v_0}$	$r_{v_0 v_1}^{f_0}$ $b_{v_0 v_1}^{f_0}$ =	$= 5$ $\alpha^{f_0}(T_{v_0}^{\text{l.o.} f_0}) = 125$ $= \gamma_{5,125}$
computeOutputBound( $v_1, f_0$ ) = $(\alpha_{v_1}^{f_0})^* = \alpha_{v_1 v_2}^{f_0}$	FIFO_MUX	ARB_MUX
$\alpha_{v_1}^{x f_0} = \alpha^{f_1}$	$= \gamma_{5,25}$	
$\beta_{v_1}^{\text{l.o.} f_0} = [\beta_{v_1} - \alpha_{v_1}^{x f_0}]^+$	$R_{v_1}^{\text{l.o.} f_0}$ $T_{v_1}^{\text{l.o.} f_0}$ =	$= 15$ $\beta_{v_1} = b_{v_1}^{x f_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$ $= \beta_{15,21\frac{1}{4}}$ $= 5$
$\alpha_{v_1 v_2}^{f_0} = \alpha_{v_1}^{f_0} \oslash \beta_{v_1}^{\text{l.o.} f_0} = \alpha_{v_0 v_1}^{f_0} \oslash \beta_{v_1}^{\text{l.o.} f_0}$	$r_{v_1 v_2}^{f_0}$ $b_{v_1 v_2}^{f_0}$ =	$\beta_{v_1} = \alpha_{v_1}^{x f_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$ $= \beta_{15,28\frac{1}{3}}$ $= \gamma_{5,231\frac{1}{4}}$ $= \gamma_{5,266\frac{2}{3}}$
computeOutputBound( $v_1, f_1$ ) = $(\alpha_{v_1}^{f_1})^* = \alpha_{v_1 v_2}^{f_1}$	FIFO_MUX	ARB_MUX
$\alpha_{v_1}^{x f_1} = \alpha_{v_0 v_1}^{f_0}$	$= \gamma_{5,125}$	
$\beta_{v_1}^{\text{l.o.} f_1} = [\beta_{v_1} - \alpha_{v_1}^{x f_1}]^+$	$R_{v_1}^{\text{l.o.} f_1}$ $T_{v_1}^{\text{l.o.} f_1}$ =	$= 15$ $\beta_{v_1} = b_{v_1}^{x f_1}$ $20 \cdot [t - 20]^+ = 125$ $t = 26\frac{1}{4}$ $= \beta_{15,26\frac{1}{4}}$ $= 5$
$\alpha_{v_1 v_2}^{f_1} = \alpha_{v_1}^{f_1} \oslash \beta_{v_1}^{\text{l.o.} f_1} = \alpha^{f_1} \oslash \beta_{v_1}^{\text{l.o.} f_1}$	$r_{v_1 v_2}^{f_1}$ $b_{v_1 v_2}^{f_1}$ =	$\beta_{v_1} = \alpha_{v_1}^{x f_1}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 125$ $t = 35$ $= \beta_{15,35}$ $= \alpha^{f_1}(T_{v_1}^{\text{l.o.} f_1}) = 156\frac{1}{4}$ $= \gamma_{5,156\frac{1}{4}}$ $= 200$ $= \gamma_{5,200}$
computeOutputBound( $v_2, f_0$ ) = $(\alpha_{v_2}^{f_0})^* = \alpha_{v_2 v_3}^{f_0}$	FIFO_MUX	ARB_MUX
$\alpha_{v_2}^{x f_0} = \alpha_{v_1 v_2}^{f_1}$	$= \gamma_{5,156\frac{1}{4}}$	$= \gamma_{5,200}$
$\beta_{v_2}^{\text{l.o.} f_0} = [\beta_{v_2} - \alpha_{v_2}^{x f_0}]^+$	$R_{v_2}^{\text{l.o.} f_0}$ $T_{v_2}^{\text{l.o.} f_0}$ =	$= 15$ $\beta_{v_2} = b_{v_2}^{x f_0}$ $20 \cdot [t - 20]^+ = 156\frac{1}{4}$ $t = 27\frac{13}{16}$ $= \beta_{15,27\frac{13}{16}}$ $= 5$
$\alpha_{v_2 v_3}^{f_0} = \alpha_{v_2}^{f_0} \oslash \beta_{v_2}^{\text{l.o.} f_0} = \alpha_{v_1 v_2}^{f_0} \oslash \beta_{v_1}^{\text{l.o.} f_0}$	$r_{v_2 v_3}^{f_0}$ $b_{v_2 v_3}^{f_0}$ =	$\beta_{v_2} = \alpha_{v_2}^{x f_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 200$ $t = 40$ $= \beta_{15,40}$ $= \alpha_{v_1 v_2}^{f_0}(T_{v_2}^{\text{l.o.} f_0}) = 370\frac{5}{16}$ $= \gamma_{5,370\frac{5}{16}}$ $= \alpha_{v_1 v_2}^{f_0}(T_{v_2}^{\text{l.o.} f_0}) = 466\frac{2}{3}$ $= \gamma_{5,466\frac{2}{3}}$

computeFifoOutputBound( $v_1, f_1$ ) = $(\alpha_{v_1}^{f_1})^* = \alpha_{v_1 v_2}^{f_1}$ for $f_0$ as flow of interest	FIFO_MUX	ARB_MUX
$\alpha_{v_1}^{x f_1}$	$= \gamma_{0,0}$	
$\beta_{v_1}^{\text{l.o.} f_1} = [\beta_{v_1} - \alpha_{v_1}^{x f_1}]^+$	$= \beta_{20,20}$	
$\alpha_{v_1 v_2}^{f_1} = \alpha_{v_1}^{f_1} \oslash \beta_{v_1}^{\text{l.o.} f_1} = \alpha^{f_1} \oslash \beta_{v_1}$	$r_{v_1 v_2}^{f_1}$ $b_{v_1 v_2}^{f_1}$ =	$= 5$ $\alpha^{f_1}(T_{v_1}^{\text{l.o.} f_1}) = 125$ $= \gamma_{5,125}$
computeFifoOutputBound( $v_1, f_0$ ) = $(\alpha_{v_1}^{f_0})^* = \alpha_{v_1 v_2}^{f_0}$ for $f_1$ as flow of interest	FIFO_MUX	ARB_MUX
$\alpha_{v_1}^{x f_0}$	$= \gamma_{0,0}$	
$\beta_{v_1}^{\text{l.o.} f_0} = [\beta_{v_1} - \alpha_{v_1}^{x f_0}]^+$	$= \beta_{20,20}$	
$\alpha_{v_1 v_2}^{f_0} = \alpha_{v_0 v_1}^{f_0} \oslash \beta_{v_1}^{\text{l.o.} f_0} = (\alpha_{v_0}^{f_0})^* \oslash \beta_{v_1}$	$r_{v_1 v_2}^{f_0}$ $b_{v_1 v_2}^{f_0}$ =	$= 5$ $\alpha_{v_0 v_1}^{f_0}(T_{v_1}^{\text{l.o.} f_0}) = 225$ $= \gamma_{5,225}$

### **Flow $f_0$**

At  $v_2v_3$  you can see the reason the network calculator moves backwards from a node to the flow of interest's source. Otherwise you don't know which flows you need separately lateron and thus could not tell which computeOutputBound calculations were necessary.

TFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0} = \alpha^{f_0}$	$= \gamma_{5,25}$	
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$	FIFO per microflow $\beta_{v_0} = b_{v_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$
	$B_{v_0}^{f_0}$	$\alpha_{v_0}(T_{v_0}) = 5 \cdot 20 + 25 = 125$	
$v_0 v_1$	$\alpha_{v_0 v_1} = (\alpha_{v_0})^*$	$= \gamma_{5,125}$	
$v_1$	$\alpha_{v_1} = \alpha^{f_1} + \alpha_{v_0 v_1}$	$= \gamma_{5,25} + \gamma_{5,125} = \gamma_{10,150}$	
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{v_1}$ $20 \cdot [t - 20]^+ = 150$ $t = 27\frac{1}{2}$	$\beta_{v_1} = \alpha_{v_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 150$ $t = 55$
	$B_{v_1}^{f_0}$	$\alpha_{v_1}(T_{v_1}) = 10 \cdot 20 + 150 = 350$	
$v_1 v_2$	$\alpha_{v_1 v_2} = (\alpha_{v_1})^*$	$= \gamma_{10,350}$	
$v_2$	$\alpha_{v_2} = \alpha_{v_1 v_2}$	$= \gamma_{10,350}$	
	$D_{v_2}^{f_0}$	$\beta_{v_2} = b_{v_2}$ $20 \cdot [t - 20]^+ = 350$ $t = 37\frac{1}{2}$	$\beta_{v_2} = \alpha_{v_2}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 350$ $t = 75$
	$B_{v_2}^{f_0}$	$\alpha_{v_2}(T_{v_2}) = 10 \cdot 20 + 350 = 550$	
$v_2 v_3$	$\alpha_{v_2 v_3} = (\alpha_{v_2}^{f_0})^*$	$= \gamma_{5,370\frac{5}{16}}$	$= \gamma_{5,466\frac{2}{3}}$
$v_3$	$\alpha_{v_3} = \alpha_{v_2 v_3}$	$= \gamma_{5,370\frac{5}{16}}$	$= \gamma_{5,466\frac{2}{3}}$
	$D_{v_3}^{f_0}$	$\beta_{v_3} = b_{v_3}$ $20 \cdot [t - 20]^+ = 370\frac{5}{16}$ $t = 38\frac{33}{64}$	FIFO per micro flow $\beta_{v_3} = b_{v_3}$ $20 \cdot [t - 20]^+ = 466\frac{2}{3}$ $t = 43\frac{1}{3}$
	$B_{v_3}^{f_0}$	$\alpha_{v_3}(T_{v_3}) = 5 \cdot 20 + 370\frac{5}{16} = 470\frac{5}{16}$	$\alpha_{v_3}(T_{v_3}) = 5 \cdot 20 + 466\frac{2}{3} = 566\frac{2}{3}$
$D^{f_0}$	$\sum_{i=0}^3 D_{v_i}^{f_0} = 124\frac{49}{64}$		$\sum_{i=0}^3 D_{v_i}^{f_0} = 194\frac{7}{12}$
$B^{f_0}$	$\max_{i=0}^3 b_{v_i}^{f_0} = 550$		$\max_{i=0}^3 b_{v_i}^{f_0} = 566\frac{2}{3}$

SFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0}^{x f_0}$		$= \gamma_{0,0}$
	$\beta_{v_0}^{\text{l.o.} f_0}$		$= \beta_{20,20}$
$v_0 v_1$	$\alpha_{v_0 v_1}^{x f_0}$		$= \gamma_{0,0}$
$v_1$	$\alpha_{v_1}^{x f_0} = \alpha^{f_1} + \alpha_{v_0 v_1}^{x f_0} = \alpha^{f_1}$		$= \gamma_{5,25}$
	$\beta_{v_1}^{\text{l.o.} f_0} = [\beta_{v_1} - \alpha_{v_1}^{x f_0}]^+$	$R_{v_1}^{\text{l.o.} f_0}$	$= 15$
		$T_{v_1}^{\text{l.o.} f_0}$	$\beta_{v_1} = b_{v_1}^{x f_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$
		$=$	$\beta_{v_1} = \alpha_{v_1}^{x f_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$
$v_1 v_2$	$\alpha_{v_1 v_2}^{x f_0} = (\alpha_{v_1}^{x f_0})^* = (\alpha_{v_1}^{f_1})^*$		$= \gamma_{5,125}$
$v_2$	$\alpha_{v_2}^{x f_0} = \alpha_{v_1 v_2}^{x f_0}$		$= \gamma_{5,125}$
	$\beta_{v_2}^{\text{l.o.} f_0} = [\beta_{v_2} - \alpha_{v_2}^{x f_0}]^+$	$R_{v_2}^{\text{l.o.} f_0}$	$= 15$
		$T_{v_2}^{\text{l.o.} f_0}$	$\beta_{v_2} = b_{v_2}^{x f_0}$ $20 \cdot [t - 20]^+ = 125$ $t = 26\frac{1}{4}$
		$=$	$\beta_{v_2} = \alpha_{v_2}^{x f_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 125$ $t = 35$
$v_2 v_3$	$\alpha_{v_0 v_1}^{x f_0}$		$= \gamma_{0,0}$
$v_3$	$\alpha_{v_3}^{x f_0} = \alpha_{v_2 v_3}^{x f_0}$		$= \gamma_{0,0}$
	$\beta_{v_3}^{\text{l.o.} f_0} = [\beta_{v_3} - \alpha_{v_3}^{x f_0}]^+$		$= \beta_{20,20}$
$\beta_{e2e}^{\text{l.o.} f_0} = \beta_{R_{e2e}^{\text{l.o.} f_0}, T_{e2e}^{\text{l.o.} f_0}}$	$\bigotimes_{i=0}^3 \beta_{v_i}^{\text{l.o.} f_0} = \beta_{15,87\frac{1}{2}}$	$\bigotimes_{i=0}^3 \beta_{v_i}^{\text{l.o.} f_0} = \beta_{15,103\frac{1}{3}}$	
$D^{f_0}$	$\beta_{e2e}^{\text{l.o.} f_0} = b^{f_0}$ $15 \cdot [t - 87\frac{1}{2}]^+ = 25$ $t = 89\frac{1}{6}$	$\beta_{e2e}^{\text{l.o.} f_0} = b^{f_0}$ $15 \cdot [t - 103\frac{1}{3}]^+ = 25$ $t = 105$	
$B^{f_0}$	$\alpha^{f_0}(T_{e2e}^{\text{l.o.} f_0}) = 5 \cdot 87\frac{1}{2} + 25$ $= 462\frac{1}{2}$	$\alpha^{f_0}(T_{e2e}^{\text{l.o.} f_0}) = 5 \cdot 103\frac{1}{3} + 25$ $= 541\frac{2}{3}$	

PMOO		ARB_MUX
$v_0$	$\beta_{v_0}^{f_0} = \beta_{v_0}$	$= \beta_{20,20}$
	$\alpha_{v_0}^{x f_0}$	$= \gamma_{0,0}$
	$\beta_{v_0}^{\text{l.o.} f_0} = \beta_{v_0}$	$= \beta_{20,20}$
$v_1 v_2$	$\beta_{v_1 v_2}^{f_0} = \beta_{v_1} \otimes \beta_{v_2}$	$= \beta_{20,40}$
	$\alpha_{v_1 v_2}^{x f_0} = \alpha^{f_1}$	$= \gamma_{5,25}$
	$\beta_{v_1 v_2}^{\text{l.o.} f_0} = [\beta_{v_1 v_2}^{f_0} - \alpha_{v_1 v_2}^{x f_0}]^+$	$R_{v_1 v_2}^{\text{l.o.} f_0}$ $= 15$
		$\beta_{v_1 v_2}^{f_0} = \alpha_{v_1 v_2}^{x f_0}$
		$T_{v_1 v_2}^{\text{l.o.} f_0}$ $20 \cdot [t - 40]^+ = 5 \cdot t + 25$ $t = 55$
	$=$	$= \beta_{15,55}$
$v_3$	$\beta_{v_0}^{f_0} = \beta_{v_0}$	$= \beta_{20,20}$
	$\alpha_{v_0}^{x f_0}$	$= \gamma_{0,0}$
	$\beta_{v_0}^{\text{l.o.} f_0} = \beta_{v_0}$	$= \beta_{20,20}$
$e2e$	$\beta_{e2e}^{f_0} = \beta_{v_0}^{f_0} \otimes \beta_{v_1 v_2}^{f_0} \otimes \beta_{v_2}^{f_0}$	$= \beta_{15,95}$
	$\alpha_{e2e}^{x f_0}$	$= \gamma_{0,0}$
	$\beta_{e2e}^{\text{l.o.} f_0} = [\beta_{e2e}^{f_0} - \alpha_{e2e}^{x f_0}]^+$	$= \beta_{15,95}$
$D^{f_0}$		$\beta_{e2e}^{\text{l.o.} f_0} = b^{f_0}$ $15 \cdot [t - 95]^+ = 25$ $t = 96\frac{2}{3}$
$B^{f_0}$		$\alpha^{f_0}(T_{e2e}^{\text{l.o.} f_0}) = 5 \cdot 95 + 25$ $= 500$

**Flow  $f_1$**

		TFA	FIFO_MUX	ARB_MUX
$v_1$	$\alpha_{v_1} = \alpha^{f_1} + \alpha_{v_0 v_1}$		$= \gamma_{5,25} + \gamma_{5,125} = \gamma_{10,150}$	
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{v_1}$ $20 \cdot [t - 20]^+ = 150$ $t = 27\frac{1}{2}$	$\beta_{v_1} = \alpha_{v_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 150$ $t = 55$	
	$B_{v_1}^{f_0}$	$\alpha_{v_1}(T_{v_1}) = 10 \cdot 20 + 150$ = 350		
$v_1 v_2$	$\alpha_{v_1 v_2} = (\alpha_{v_1})^*$	$r_{v_1 v_2}$ $b_{v_1 v_2}$ =	$= 10$ $\alpha_{v_1}(T_{v_1}) = 350$ $= \gamma_{10,350}$	
	$\alpha_{v_2} = \alpha_{v_1 v_2}$		$= \gamma_{10,350}$	
	$D_{v_2}^{f_0}$	$\beta_{v_2} = b_{v_2}$ $20 \cdot [t - 20]^+ = 350$ $t = 37\frac{1}{2}$	$\beta_{v_2} = \alpha_{v_2}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 350$ $t = 75$	
	$B_{v_2}^{f_0}$	$\alpha_{v_2}(T_{v_2}) = 10 \cdot 20 + 350$ = 550		
	$D^{f_0}$	$\sum_{i=1}^2 D_{v_i}^{f_0} = 65$	$\sum_{i=1}^2 D_{v_i}^{f_0} = 130$	
	$B^{f_0}$	$\max_{i=1}^2 b_{v_i}^{f_0} = 550$		

SFA		FIFO_MUX	ARB_MUX
$v_1$	$\alpha_{v_1}^{xf_1} = \alpha_{v_0v_1}^{xf_1} = \alpha_{v_0v_1}^{f_0}$		$= \gamma_{5,125}$
	$\beta_{v_1}^{\text{l.o.} f_1} = [\beta_{v_1} - \alpha_{v_1}^{xf_1}]^+$	$R_{v_1}^{\text{l.o.} f_1}$	$= 15$
		$T_{v_1}^{\text{l.o.} f_1}$	$\beta_{v_1} = b_{v_1}^{xf_1}$ $20 \cdot [t - 20]^+ = 125$ $t = 26\frac{1}{4}$
	$=$		$= \beta_{15,26\frac{1}{4}}$
$v_1v_2$	$\alpha_{v_1v_2}^{xf_1} = (\alpha_{v_1}^{xf_1})^* = (\alpha_{v_1}^{f_1})^*$		$= \gamma_{5,225}$
$v_2$	$\alpha_{v_2}^{xf_1} = \alpha_{v_1v_2}^{xf_1}$		$= \gamma_{5,225}$
	$\beta_{v_2}^{\text{l.o.} f_1} = [\beta_{v_2} - \alpha_{v_2}^{xf_1}]^+$	$R_{v_2}^{\text{l.o.} f_1}$	$= 15$
		$T_{v_2}^{\text{l.o.} f_1}$	$\beta_{v_2} = b_{v_2}^{xf_1}$ $20 \cdot [t - 20]^+ = 225$ $t = 31\frac{1}{4}$
	$=$		$= \beta_{15,31\frac{1}{4}}$
$\beta_{e2e}^{\text{l.o.} f_1} = \beta_{R_{e2e}^{\text{l.o.} f_1}, T_{e2e}^{\text{l.o.} f_1}}$	$\bigotimes_{i=1}^2 \beta_{v_i}^{\text{l.o.} f_1} = \beta_{15,57\frac{1}{2}}$	$\bigotimes_{i=1}^2 \beta_{v_i}^{\text{l.o.} f_1} = \beta_{15,76\frac{2}{3}}$	
$D^{f_1}$	$\beta_{e2e}^{\text{l.o.} f_1} = b^{f_1}$ $15 \cdot [t - 57\frac{1}{2}]^+ = 25$ $t = 59\frac{1}{6}$	$\beta_{e2e}^{\text{l.o.} f_1} = b^{f_1}$ $15 \cdot [t - 76\frac{2}{3}]^+ = 25$ $t = 78\frac{1}{3}$	
$B^{f_1}$	$\alpha^{f_1}(T_{e2e}^{\text{l.o.} f_1}) = 5 \cdot 57\frac{1}{2} + 25$ $= 312\frac{1}{2}$	$\alpha^{f_1}(T_{e2e}^{\text{l.o.} f_1}) = 5 \cdot 76\frac{2}{3} + 25$ $= 408\frac{1}{3}$	

PMOO		ARB_MUX
e2e	$\beta_{e2e}^{f_0} = \beta_{v_1} \otimes \beta_{v_2}$	$= \beta_{20,40}$
	$\alpha_{e2e}^{xf_1} = \alpha_{v_1} = \alpha_{v_0 v_1}^{f_0}$	$= \gamma_{5,125}$
	$\beta_{e2e}^{\text{l.o.} f_1} = [\beta_{e2e}^{f_1} - \alpha_{e2e}^{xf_1}]^+$	$R_{e2e}^{\text{l.o.} f_1} = 15$
		$\beta_{e2e}^{f_1} = \alpha_{e2e}^{xf_1}$
		$20 \cdot [t - 40]^+ = 5 \cdot t + 125$
		$t = 61\frac{2}{3}$
	$=$	$= \beta_{15,61\frac{2}{3}}$
$D^{f_1}$		$\beta_{e2e}^{\text{l.o.} f_1} = b^{f_1}$
		$15 \cdot [t - 61\frac{2}{3}]^+ = 25$
		$t = 63\frac{1}{3}$
$B^{f_1}$		$\alpha^{f_1}(T_{e2e}^{\text{l.o.} f_1}) = 5 \cdot 61\frac{2}{3} + 25$
		$= 333\frac{1}{3}$