

**Accuracy of Network Calculus for Embedded Systems:
Successes and Challenges**

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ONERA – The French Aerospace Lab

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r e t o u r s u r i n n o v a t i o n

Once upon a time (1999-2004)

Work done (2004-2014)

- Formal framework

- Tightness in theory

- Accuracy in practice

Challenges

Miscellaneous

Conclusion

Theses slides have been made for the support of an open workshop oral discussion, not as a robust and fair overview of the research area.

In particular:

- references have not been chosen to identify the first author(s) of a result, as is standard academic citation policy, but as the ones that I can quickly identify: I have done theses slides in a short time
- the “challenge” list is not a list of “no result” topics, but where, IMHA, lot exiting research is still to be done,
- a lot of interesting results have not been cited, and in particular:
 - all works of the MPA/RTC area [[Wandeler and Thiele, 2006](#)], since the advances in the considered period seems not directly apply on AFDX,
 - all works on Event Stream [[Henia et al., 2005](#), [Rox and Ernst, 2010](#)], MAST [[Gutiérrez et al., 2012](#)] and trajectories [[Bauer et al., 2010](#)], even if it has been applied to AFDX, because this talk about network calculus

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AFDX: Avionic Full Duplex

- Standard ARINC 664 P7
- Ethernet tailored for avionic needs
 - Flows: Virtual links (Token-Bucket + static routing)
 - Network: Full duplex, FIFO + SP

⇒ should have bounded delays ?

⇒ how to compute and prove it ?

- \approx 1999 Rockwell Collins (\approx Airbus) request to Fabrice Frances and Christian Fraboul (Univ. Toulouse, France)

⇒ Jérôme Griedu PhD [[Griedu et al., 2003](#), [Griedu, 2004](#)]
use of *deterministic* network calculus

From Grieu PhD

- AFDX model in network calculus
- Qualified tool (Rockwell Collins)
- Used to certify A380, A350, A400M

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Next steps:

- Better (smaller) bounds
- Modelling new buses, policies...
- Still in “trustable” framework

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[Bouillard et al., 2009, Bouillard et al., 2010a, Bouillard, 2011]
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- Left or right continuity of flows? [Boyer et al., 2013]
 - Left-continuous for all proofs except the ones on packets.
 - Does not really matter...

Network calculus requires implementation of operations: minimum, sum, convolution, deconvolution, horizontal deviation

- Token-bucket and rate-latency ($\gamma_{r,b}(t) = rt + b$, $\beta_{R,T} = R[t - T]^+$: analytical solutions
- Concave/convex piecewise linear functions (CPL, [Cruz, 1998])
 - natural representations
 - long list of implementations (too long for this slide)
 - simple implementation of convolution
- Ultimately pseudo-periodic functions (UPP, [Bouillard and Thierry, 2008])
 - set of any segments
 - with a finite prefix and a periodic “pattern”
- Containers [Le Corronc et al., 2014]
 - efficient “approximation” of operations
 - complexity $O(n)$ or $O(n \log(n))$

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Accuracy in practice

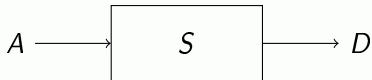
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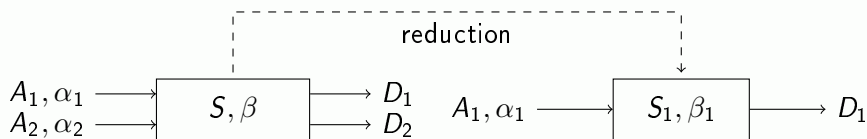
Tightness

The computed bound is *the* worst case, *i.e.* it exists a configuration such that the bound is reached.



Well known for single server, single flow system: for any arrival curve α and service curve β , it exist A_α and S_β such that $d(A_\alpha, D_\beta) = d(\alpha, \beta)$.

Tightness and service policies



Exact delay for

- Blind, SP [Bouillard et al., 2010b]
- FIFO [Bouillard and Stea, 2012]

Conjecture of exactness for

- Non-preemptive SP with fixed sizes [Mangoua Sofack and Boyer, 2012, Chokshi and Bhaduri, 2008]
- Deficit Round Robin [Boyer et al., 2012b]

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- Algebraic solutions can be arbitrary large [[Schmitt et al., 2008](#)]
- Solutions
 - identification of specific sub-cases (topology, policy...)
 - optimisation problem [[Schmitt et al., 2008](#),
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 - restriction to piecewise concave/convex functions

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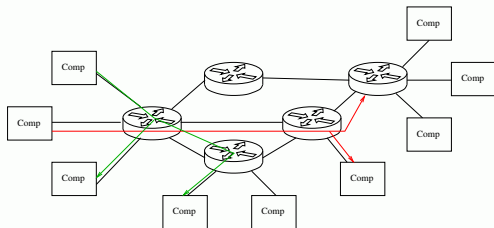
Accuracy in practice

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Accuracy on AFDX configurations



AFDX configurations:

- ≈ 100 sources/sink
- $\approx 5-10$ switches $\Rightarrow \approx 100$ "servers"
- $\approx 10^4$ data flows (Virtual links)
- load $\approx 10\% - 20\%$
- cycle free

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Implemented in RTaW-PEGASE.

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Formal challenges (IMHA)

- Packets
 - packets results are based on maximal size
 - how to mix small and large packet?
 - for packet-based policies
 - first model [[Bouillard et al., 2011](#), [Bouillard et al., 2012](#)]
- Feedback
 - Protocols with feedback: Wormhole routing, TCP
 - Applicative feedback
- Cyclic dependencies [[Jonsson et al., 2008](#)]
- Inversion problem [[Le Corronc et al., 2010](#)]
 - classical approach: from flows and servers, computes delay/memory bounds
 - synthesis problem: which flows/servers to guarantee a bound?

- New networks
 - AVB/TSN
 - ARINC 825
- Network on chip
- Integration scheduler/task and network/messages
 - task release by message reception
 - task duration independent of message size
 - messages send at end of task
- Design help
 - synthesis (inversion)
 - sensitivity analysis
 - ...

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- Coming soon: another book on *deterministic* network calculus
 - Anne Bouillard, Marc Boyer, Euriell Le Corronc
 - Summing up last 10 years
- NetAirBench
 - configuration generator
 - creation of public test benches

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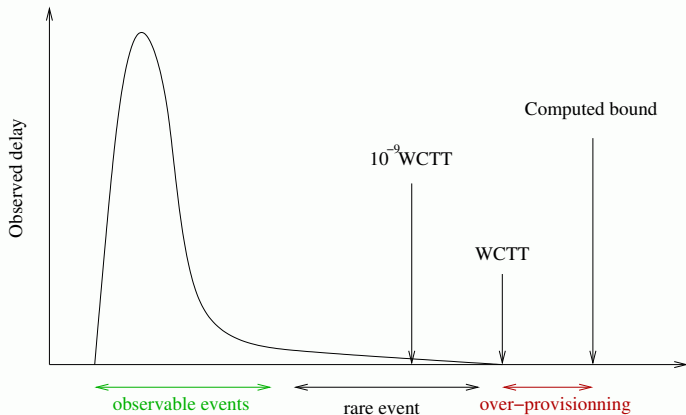
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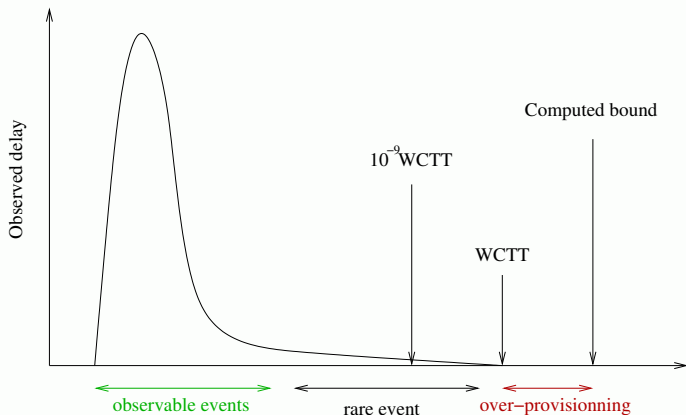
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Questions?

Stochastic bounds for embedded system



Stochastic bounds for embedded system



- How to get input probabilities?
- Where are the stochastic bounds wrt deterministic bounds?



Bauer, H., Scharbarg, J.-L., and Fraboul, C. (2010).

Improving the worst-case delay analysis of an AFDX network using an optimized trajectory approach.

IEEE Trans. Industrial Informatics, 6(4):521–533.



Bouillard, A. (2011).

Composition of service curves in network calculus.

In *Proceedings of the 1st International Workshop on Worst-Case Traversal Time (WCTT'2011)*, WCTT '11, pages 35–42.



Bouillard, A., Farhi, N., and Gaujal, B. (2011).

Packetization and aggregate scheduling.

Technical Report 7685, INRIA.



Bouillard, A., Farhi, N., and Gaujal, B. (2012).

Packetization and packet curves in network calculus.

In *Proc. of the 6th International Conference on Performance Evaluation Methodologies and Tools (ValueTools 2012)*, Cargese, France.

Invited Paper.



Bouillard, A., Jouhet, L., and Thierry, E. (2009).

Service curves in Network Calculus: dos and don'ts.

Research Report RR-7094, INRIA.



Bouillard, A., Jouhet, L., and Thierry, E. (2009).

Tight performance bounds in the worst-case analysis of feed-forward networks.
Technical Report 7012, INRIA.



Bouillard, A., Jouhet, L., and Thierry, E. (2010a).

Comparison of different classes of service curves in network calculus.
In *Proc. of the 10th International Workshop on Discrete Event Systems (WODES 2010)*,
Technische Universität Berlin.



Bouillard, A., Jouhet, L., and Thierry, E. (2010b).

Tight performance bounds in the worst-case analysis of feed-forward networks.
In *Proceedings of the 29th Conference on Computer Communications (INFOCOM 2010)*, pages
1–9.



Bouillard, A. and Stea, G. (2012).

Exact worst-case delay for fifo-multiplexing tandems.
In *Proc. of the 6th International Conference on Performance Evaluation Methodologies and Tools (ValueTools 2012)*, Cargese, France.



Bouillard, A. and Thierry, E. (2008).

An algorithmic toolbox for network calculus.
Discrete Event Dynamic Systems, 18(1):3–49.
<http://www.springerlink.com/content/876x51r6647r8g68/>.



Boyer, M., Dufour, G., and Santinelli, L. (2013).

Continuity for network calculus.

In Proc of the 21th International Conference on Real-Time and Network Systems (RTNS 2013), pages 235–244, Sophia Antipolis, France. ACM.



Boyer, M., Migge, J., and Fumey, M. (2011).

PEGASE, a robust and efficient tool for worst case network traversal time.

In Proc. of the SAE 2011 AeroTech Congress & Exhibition, Toulouse, France. SAE International.



Boyer, M., Navet, N., and Fumey, M. (2012a).

Experimental assessment of timing verification techniques for afdx.

In Proc. of the 6th Int. Congress on Embedded Real Time Software and Systems, Toulouse, France.



Boyer, M., Santinelli, L., Navet, N., and Migge, Jörn and Fumey, M. (2014).

Integrating end-system frame scheduling for more accurate afdx timing analysis.

In Proc. of the 7th Int. Congress on Embedded Real Time Software and Systems (ERTSS 2014), Toulouse, France.



Boyer, M., Stea, G., and Mangoua Sofack, W. (2012b).

Deficit round robin with network calculus.

In Proc. of the 6th International Conference on Performance Evaluation Methodologies and Tools (ValueTools 2012), Cargese, France.



Chokshi, D. B. and Bhaduri, P. (2008).

Modeling fixed priority non-preemptive scheduling with real-time calculus.

In *Proc. of the 2008 14th IEEE int. conf. on Embedded and Real-Time Computing Systems and Applications (RTCSA'08)*, Washington, DC, USA. IEEE Computer Society.



Cruz, R. (1998).

SCED+: efficient management of quality of service guarantees.

In *Proc. of the 7th Annual Joint Conference of the IEEE Computer and Communications Societies (INFOCOM '98)*, volume 2, pages 625 –634 vol.2.



Grieu, J. (2004).

Analyse et évaluation de techniques de commutation Ethernet pour l'interconnexion des systèmes avioniques.

PhD thesis, Institut National Polytechnique de Toulouse (INPT), Toulouse.



Grieu, J., Frances, F., and Fraboul, C. (2003).

Preuve de déterminisme d'un réseau embarqué avionique.

In *Actes du Colloque Francophone sur l'Ingenierie des Protocoles (CFIP 2003)*, Paris.



Gutiérrez, J. J., Palencia, J. C., and Harbour, M. G. (2012).

Response time analysis in AFDX networks with sub-virtual links and prioritized switches.

In *Proc of the XV Jornadas de Tiempo Real*, Santander, Spain.



Henia, R., Hamann, A., Jersak, M., Racu, R., Richter, K., and Ernst, R. (2005).

System level performance analysis - the symta/s approach.

IEEE Proceedings on Computers and Digital Techniques, 152(2):148 – 166.



Jonsson, B., Perathoner, S., Thiele, L., and Yi, W. (2008).

Cyclic dependencies in modular performance analysis.

In *Proc. of the 8th Int. Conf on Embedded Software (EMSOFT'08)*, pages 179–188. ACM Press.



Le Corronc, E., Cottenceau, B., and Hardouin, L. (2010).

Flow control with $(\min, +)$ algebra.

In *4th International Symposium On Leveraging Applications of Formal Methods, Verification and Validation, 2010, Heraklion - Crete. ISOLA '10*.



Le Corronc, E., Cottenceau, B., and Hardouin, L. (2014).

Container of $(\min, +)$ -linear systems.

Journal of Discrete Event Dynamic Systems, 14(1):15–52.



Lenzini, L., Mingozzi, E., and Stea, G. (2004).

Delay bounds for FIFO aggregates: a case study.

Computer Communications, 28:287–299.



Mangoua Sofack, W. . and Boyer, M. (2012).

Non preemptive static priority with network calculus: Enhancement.

In *Proc. of the Workshop on Network Calculus (WoNeCa 2012)*, Kaiserslautern, Germany.



Rox, J. and Ernst, R. (2010).

Formal timing analysis of full duplex switched based ethernet network architectures.

In *Proc. of the SAE 2010 AeroTech Congress and Exhibition*. SAE International.



Schmitt, J., Zdarsky, F., and Fidler, M. (2008).

Delay bounds under arbitrary multiplexing: When network calculus leaves you in the lurch...

In *The 27th IEEE Conference on Computer Communications (INFOCOM 2008)*, pages 1669 –1677.



Wandeler, E. and Thiele, L. (2006).

Real-Time Calculus (RTC) Toolbox.

<http://www.mpa.ethz.ch/Rtctoolbox>.