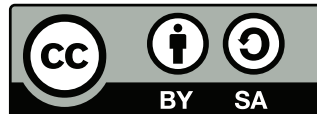


Network Calculus Tests – Single Server (S) Networks

Version 2.0 beta2 (2017-Jun-25)



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General Information

- The network calculus analyses presented in this document were created for the purpose of testing the Disco Deterministic Network Calculator (DiscoDNC)¹ – an open-source deterministic network calculus tool developed by the *Distributed Computer Systems (DISCO) Lab* at the University of Kaiserslautern.
- Naming of the individual network configurations depicts the name of the according functional test for the DiscoDNC.
- The naming scheme used in this document is detailed in `NetworkCalculus_NamingScheme.pdf`.
- Arrival bound computations are equivalent to the `PbooArrivalBound_Output_PerHop.java` class of the DiscoDNC.
- The end-to-end left-over service curve for PBOO arrival bounds can be computed by simply convolving the server-local ones.
- Arrival bounds for `PmooArrivalBound.java` and analyses using them are listed only if results are different to PBOO.

Changelog:

Version 1.1 (2014-Dec-30):

- Adapted to naming scheme version 1.1.

Version 2.0 beta2 (2017-Jun-25):

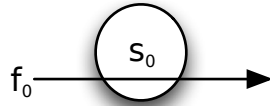
- Rework of the documentation according to code changes
 - New, more complete naming.
 - Separation of network and test.

Acknowledgements:

Version 1.1: Thanks to Yokanand Thirupathi and Paresh Chotala for pointing out some errors.

¹<http://disco.cs.uni-kl.de/index.php/projects/disco-dnc>

S_1SC_1F_1AC_Network



- $\beta_{s_0} = \beta_{R_{s_0}, T_{s_0}} = \beta_{10, 10}$
- $\mathcal{F} = \{f_0\}$
- $\alpha^{f_0} = \gamma_{r^{f_0}, b^{f_0}} = \gamma_{5, 25}$

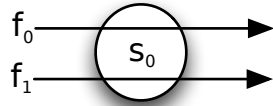
S_1SC_1F_1AC_Test

	TFA	FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0} = \alpha^{f_0}$		$= \gamma_{5, 25}$
	D^{f_0}	$\beta_{s_0} = b_{s_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$	FIFO per micro flow $\beta_{s_0} = b_{s_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$
	B^{f_0}		$\alpha_{s_0}(T_{s_0}) = 5 \cdot 10 + 25$ $= 75$

SFA		FIFO_MUX	ARB_MUX
s ₀	$\alpha_{s_0}^{x(f_0)}$		= $\gamma_{0,0}$
	$\beta_{e2e}^{1.o.f_0} = [\beta_{s_0} - \alpha_{s_0}^{x(f_0)}]^+ = \beta_{R_{e2e}^{1.o.f_0}, T_{e2e}^{1.o.f_0}} = \beta_{s_0}$		= $\beta_{10,10}$
	D^{f_0}		$\beta_{e2e}^{1.o.f_0} = b^{f_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$
	B^{f_0}		$\alpha^{f_0}(T_{e2e}^{1.o.f_0}) = 5 \cdot 10 + 25$ = 75

PMOO		ARB_MUX
s ₀	$\alpha_{s_0}^{\bar{x}(f_0)}$	= $\gamma_{0,0}$
	$\alpha_{s_0}^{x(f_0)}$	= $\gamma_{0,0}$
$\beta_{e2e}^{1.o.f_0} = \beta_{R_{e2e}^{1.o.f_0}, T_{e2e}^{1.o.f_0}}$	$R_{e2e}^{1.o.f_0} = R_{s_0} - r_{s_0}^{x(f_0)}$	= $10 - 0$ = 10
	$T_{e2e}^{1.o.f_0} = T_{s_0} + \frac{b_{s_0}^{\bar{x}(f_0)} + r_{s_0}^{x(f_0)} \cdot T_{s_0}}{R_{e2e}^{1.o.f_0}}$	= $10 + \frac{0 + 0 \cdot 10}{10}$ = 10
	=	= $\beta_{10,10}$
	D^{f_0}	$\beta_{e2e}^{1.o.f_0} = b^{f_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$
B^{f_0}	$\alpha^{f_0}(T_{e2e}^{1.o.f_0}) = 5 \cdot 10 + 25$ = 75	

S_1SC_2F_1AC_Network



- $\beta_{s_0} = \beta_{R_{s_0}, T_{s_0}} = \beta_{10,10}$
- $\mathcal{F} = \{f_0, f_1\}$
- $\alpha^{f_0} = \alpha^{f_1} = \gamma_{r^{f_n}, b^{f_n}} = \gamma_{5,25}, n \in \{0, 1\}$

S_1SC_2F_1AC_Test

Flows $f_n, n \in \{0, 1\}$

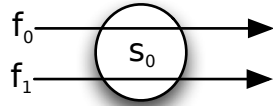
TFA results will be equal for all flows as they share the same path of servers.

	TFA	FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0} = \alpha^{f_0} + \alpha^{f_1}$	$= \gamma_{10,50}$	
	D^{f_n}	$\beta_{s_0} = b_{s_0}$ $10 \cdot [t - 10]^+ = 50$ $t = 15$	$\beta_{s_0} = \alpha_{s_0}$ $10 \cdot [t - 10]^+ = 10 \cdot t + 50$ $0 \cdot t = 150$ $\Rightarrow D^{f_n} = \infty$
	B^{f_n}	$\alpha_{s_0}(T_{s_0}) = 10 \cdot 10 + 50$ $= 150$	

SFA		FIFO_MUX	ARB_MUX	
s_0	$\alpha_{s_0}^{x(f_n)} = \alpha^{f_n}$		$= \gamma_{5,25}$	
	$\beta_{s_0}^{1.o.f_n} = \beta_{s_0} \ominus \alpha_{s_0}^{x(f_n)} = \beta_{R_{s_0}^{1.o.f_n}, T_{s_0}^{1.o.f_n}}$	$R_{s_0}^{1.o.f_n}$	$[R_{s_0} - r_{s_0}^{x(f_n)}]^+ = 5$	
		$T_{s_0}^{1.o.f_n}$	$\beta_{s_0} = b_{s_0}^{x(f_n)}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$	$\beta_{s_0} = \alpha_{s_0}^{x(f_n)}$ $10 \cdot [t - 10]^+ = 5 \cdot t + 25$ $t = 25$
		=	$= \beta_{5,12\frac{1}{2}}$	$= \beta_{5,25}$
	$\beta_{e2e}^{1.o.f_n} = \beta_{s_0}^{1.o.f_n}$		$= \beta_{5,12\frac{1}{2}}$	$= \beta_{5,25}$
D^{f_n}		$\beta_{e2e}^{1.o.f_n} = b^{f_n}$ $5 \cdot [t - 12\frac{1}{2}]^+ = 25$ $t = 17\frac{1}{2}$	$\beta_{e2e}^{1.o.f_n} = b^{f_n}$ $5 \cdot [t - 25]^+ = 25$ $t = 30$	
B^{f_n}		$\alpha^{f_n}(T_{e2e}^{1.o.f_n}) = 5 \cdot 12\frac{1}{2} + 25$ $= 87\frac{1}{2}$	$\alpha^{f_n}(T_{e2e}^{1.o.f_n}) = 5 \cdot 25 + 25$ $= 150$	

PMOO		ARB_MUX
s_0	$\alpha_{s_0}^{\bar{x}(f_n)} = \alpha^{f_n}$	$= \gamma_{5,25}$
	$\alpha_{s_0}^{x(f_n)} = \alpha^{f_n}$	$= \gamma_{5,25}$
$\beta_{e2e}^{1.o.f_n} = \beta_{R_{e2e}^{1.o.f_n}, T_{e2e}^{1.o.f_n}}$	$R_{e2e}^{1.o.f_n} = R_{s_0} - r_{s_0}^{x(f_n)}$	$= 10 - 5$
		$= 5$
	$T_{e2e}^{1.o.f_n} = T_{s_0} + \frac{b_{s_0}^{\bar{x}(f_n)} + r_{s_0}^{x(f_n)} \cdot T_{s_0}}{R_{e2e}^{1.o.f_0}}$	$= 10 + \frac{25 + 5 \cdot 10}{5}$
		$= 25$
	$=$	$= \beta_{5,25}$
Df_n		$\beta_{e2e}^{1.o.f_n} = b^{f_n}$
		$5 \cdot [t - 25]^+ = 25$
		$t = 30$
Bf_n		$\alpha^{f_n}(T_{e2e}^{1.o.f_n}) = 5 \cdot 25 + 25$
		$= 150$

S_1SC_2F_2AC_Network



- $\beta_{s_0} = \beta_{R_{s_0}, T_{s_0}} = \beta_{10,10}$
- $\mathcal{F} = \{f_0, f_1\}$
- $\alpha^{f_0} = \gamma_{r^{f_0}, b^{f_0}} = \gamma_{4,10}$
- $\alpha^{f_1} = \gamma_{r^{f_1}, b^{f_1}} = \gamma_{5,25}$

S_1SC_2F_2AC_Test

Flows $f_n, n \in \{0, 1\}$

TFA results will be equal for all flows as they share the same path of servers.

	TFA	FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0} = \alpha^{f_0} + \alpha^{f_1}$	$= \gamma_{9,35}$	
	D^{f_n}	$\beta_{s_0} = b_{s_0}$ $10 \cdot [t - 10]^+ = 35$ $t = 13\frac{1}{2}$	$\beta_{s_0} = \alpha_{s_0}$ $10 \cdot [t - 10]^+ = 9 \cdot t + 35$ $t = 135$
	B^{f_n}	$\alpha_{s_0}(T_{s_0}) = 9 \cdot 10 + 35 = 125$	

Flow f_0

SFA		FIFO_MUX	ARB_MUX	
s_0	$\alpha_{s_0}^{x(f_0)} = \alpha^{f_1}$	$= \gamma_{5,25}$		
	$\beta_{s_0}^{l.o.f_0} = \beta_{s_0} \ominus \alpha_{s_0}^{x(f_0)} = \beta_{R_{s_0}^{l.o.f_0}, T_{s_0}^{l.o.f_0}}$	$R_{s_0}^{l.o.f_0}$	$[R_{s_0} - r_{s_0}^{x(f_0)}]^+ = 5$	
		$T_{s_0}^{l.o.f_0}$	$\beta_{s_0} = b_{s_0}^{x(f_0)}$ $10 \cdot [t - 10]^+ = 25$ $t = 12\frac{1}{2}$	$\beta_{s_0} = \alpha_{s_0}^{x(f_0)}$ $10 \cdot [t - 10]^+ = 5 \cdot t + 25$ $t = 25$
		=	$= \beta_{5,12\frac{1}{2}}$	$= \beta_{5,25}$
	$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}} = \beta_{s_0}^{l.o.f_0}$		$= \beta_{5,12\frac{1}{2}}$	$= \beta_{5,25}$
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $5 \cdot [t - 12\frac{1}{2}]^+ = 10$ $t = 14\frac{1}{2}$	$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $5 \cdot [t - 25]^+ = 10$ $t = 27$	
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 4 \cdot 12\frac{1}{2} + 10$ $= 60$	$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 4 \cdot 25 + 10$ $= 110$	

PMOO		ARB_MUX
s_0	$\alpha_{s_0}^{\bar{x}(f_0)} = \alpha^{f_1}$	$= \gamma_{5,25}$
	$\alpha_{s_0}^{x(f_0)} = \alpha^{f_1}$	$= \gamma_{5,25}$
$\beta_{s_0}^{l.o.f_0} = \beta_{R_{s_0}^{l.o.f_0}, T_{s_0}^{l.o.f_0}}$	$R_{e2e}^{l.o.f_0} = R_{s_0} - r_{s_0}^{x(f_0)}$	$= 10 - 5$
		$= 5$
	$T_{e2e}^{l.o.f_0} = T_{s_0} + \frac{b_{s_0}^{\bar{x}(f_0)} + r_{s_0}^{x(f_0)} \cdot T_{s_0}}{R_{e2e}^{l.o.f_0}}$	$= 10 + \frac{25 + 5 \cdot 10}{5}$
		$= 25$
	$=$	$= \beta_{5,25}$
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$
		$5 \cdot [t - 25]^+ = 10$
		$t = 27$
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 4 \cdot 25 + 10$
		$= 110$

Flow f_1

SFA		FIFO_MUX	ARB_MUX	
s_0	$\alpha_{s_0}^{x(f_1)} = \alpha^{f_0}$	$= \gamma_{4,10}$		
	$\beta_{s_0}^{l.o.f_1} = \beta_{s_0} \ominus \alpha_{s_0}^{x(f_1)} = \beta_{R_{s_0}^{l.o.f_1}, T_{s_0}^{l.o.f_1}}$	$R_{s_0}^{l.o.f_1}$	$[R_{s_0} - r_{s_0}^{x(f_1)}]^+ = 6$	
		$T_{s_0}^{l.o.f_1}$	$\beta_{s_0} = b_{s_0}^{x(f_1)}$ $10 \cdot [t - 10]^+ = 10$ $t = 11$	$\beta_{s_0} = \alpha_{s_0}^{x(f_1)}$ $10 \cdot [t - 10]^+ = 4 \cdot t + 10$ $t = 18\frac{1}{3}$
		=	$= \beta_{6,11}$	$= \beta_{6,18\frac{1}{3}}$
	$\beta_{e2e}^{l.o.f_1} = \beta_{R_{e2e}^{l.o.f_1}, T_{e2e}^{l.o.f_1}} = \beta_{s_0}^{l.o.f_1}$		$= \beta_{6,11}$	$= \beta_{6,18\frac{1}{3}}$
	Df_1	$\beta_{e2e}^{l.o.f_1} = b^{f_1}$ $6 \cdot [t - 11]^+ = 25$ $t = 15\frac{1}{6}$	$\beta_{e2e}^{l.o.f_1} = b^{f_1}$ $6 \cdot [t - 18\frac{1}{3}]^+ = 25$ $t = 22\frac{1}{2}$	
Bf_1	$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 11 + 25$ $= 80$	$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 18\frac{1}{3} + 25$ $= 116\frac{2}{3}$		

PMOO		ARB_MUX
s_0	$\alpha_{s_0}^{\bar{x}(f_1)} = \alpha^{f_0}$	$= \gamma_{4,10}$
	$\alpha_{s_0}^{x(f_1)} = \alpha^{f_0}$	$= \gamma_{4,10}$
$\beta_{s_0}^{l.o.f_1} = \beta_{R_{s_0}^{l.o.f_1}, T_{s_0}^{l.o.f_1}}$	$R_{e2e}^{l.o.f_1} = R_{s_0} - r_{s_0}^{x(f_1)}$	$= 10 - 4$ $= 6$
	$T_{e2e}^{l.o.f_1} = T_{s_0} + \frac{b_{s_0}^{\bar{x}(f_1)} + r_{s_0}^{x(f_1)} \cdot T_{s_0}}{R_{e2e}^{l.o.f_1}}$	$= 10 + \frac{10 + 4 \cdot 10}{6}$ $= 18\frac{1}{3}$
	$=$	$= \beta_{6, 18\frac{1}{3}}$
D^{f_1}		$\beta_{e2e}^{l.o.f_1} = b^{f_1}$ $6 \cdot [t - 18\frac{1}{3}]^+ = 25$ $t = 22\frac{1}{2}$
B^{f_1}		$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 18\frac{1}{3} + 25$ $= 116\frac{2}{3}$

S_1SC_10F_10AC_Network

- $\beta_{s_0} = \beta_{R_{s_0}, T_{s_0}} = \beta_{10,10}$
- $\mathcal{F} = \{f_0, f_1, f_2, f_3, f_4, f_5, f_6, f_7, f_8, f_9\}$
- for $n = 0$ to 9 : $\alpha^{f_n} = \gamma_{r.f_n, b.f_n} = \gamma_{\frac{1}{10} \cdot (i+1), 1 \cdot (i+1)}$

We restrict the presentation of the SFA and the PMOO analysis to flows f_0 and f_6 .
The omitted computations follow the same scheme.

S_1SC_10F_10AC_Test

Flows $f_n, n \in \{0, \dots, 9\}$

TFA results will be equal for all flows as they share the same path of servers.

	TFA	FIFO_MUX	ARB_MUX
s_0	$\alpha_{s_0} = \sum_{n=0}^9 \alpha_i$	$= \gamma_{5\frac{1}{2}, 55}$	
	Df_n	$\beta_{s_0} = b_{s_0}$ $10 \cdot [t - 10]^+ = 55$ $t = 15\frac{1}{2}$	$\beta_{s_0} = \alpha_{s_0}$ $10 \cdot [t - 10]^+ = 5\frac{1}{2} \cdot t + 55$ $t = 34\frac{4}{9}$
	Bf_n	$\alpha_{s_0}(T_{s_0}) = 5\frac{1}{2} \cdot 10 + 55$ $= 110$	

Flow f_0

SFA		FIFO_MUX	ARB_MUX	
s ₀	$\alpha_{s_0}^{x(f_0)} = \sum_{n=1}^9 \alpha^{f_n} = \gamma_{r_{s_0}^{x(f_0)}, b_{s_0}^{x(f_0)}}$	$r_{s_0}^{x(f_0)}$	$\sum_{n=1}^9 r^{f_n} = 5\frac{2}{5}$	
		$b_{s_0}^{x(f_0)}$	$\sum_{n=1}^9 b^{f_n} = 54$	
		=	$= \gamma_{5\frac{2}{5}, 54}$	
	$\beta_{s_0}^{l.o.f_0} = R_{s_0} \ominus \alpha_{s_0}^{x(f_0)} = \beta_{R_{s_0}^{l.o.f_0}, T_{s_0}^{l.o.f_0}}$	$R_{s_0}^{l.o.f_0}$	$[R_{s_0} - r_{s_0}^{x(f_0)}]^+ = 4\frac{3}{5}$	
		$T_{s_0}^{l.o.f_0}$	$\beta_{s_0} = b_{s_0}^{x(f_0)}$ $10 \cdot [t - 10]^+ = 54$ $t = 15\frac{2}{5}$	$\beta_{s_0} = \alpha_{s_0}^{x(f_0)}$ $10 \cdot [t - 10]^+ = 5\frac{2}{5} \cdot t + 54$ $t = 33\frac{11}{23}$
		=	$= \beta_{4\frac{3}{5}, 15\frac{2}{5}}$	$= \beta_{4\frac{3}{5}, 33\frac{11}{23}}$
	$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}} = \beta_{s_0}^{l.o.f_0}$		$= \beta_{4\frac{3}{5}, 15\frac{2}{5}}$	$= \beta_{4\frac{3}{5}, 33\frac{11}{23}}$
	D^{f_0}	$\beta_{e2e}^{l.o.f_0} = b^{f_0}$	$\beta_{e2e}^{l.o.f_0} = b^{f_0}$	$\beta_{e2e}^{l.o.f_0} = b^{f_0}$
		$4\frac{3}{5} \cdot [t - 15\frac{2}{5}]^+ = 1$ $t = 15\frac{71}{115}$	$4\frac{3}{5} \cdot [t - 33\frac{11}{23}]^+ = 1$ $t = 33\frac{16}{23}$	
B^{f_0}	$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = \frac{1}{10} \cdot 15\frac{2}{5} + 1$	$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = \frac{1}{10} \cdot 33\frac{11}{23} + 1$		
	$= 2\frac{27}{50}$	$= 4\frac{8}{23}$		

PMOO		ARB_MUX
s_0	$\alpha_{s_0}^{\bar{x}(f_0)} = \sum_{n=1}^9 \alpha^{f_n} = \gamma_{r_{s_0}^{x(f_0)}, b_{s_0}^{x(f_0)}}$	$= \gamma_{5\frac{2}{5}, 54}$
	$\alpha_{s_0}^{x(f_0)} = \sum_{n=1}^9 \alpha^{f_n} = \gamma_{r_{s_0}^{x(f_0)}, b_{s_0}^{x(f_0)}}$	$= \gamma_{5\frac{2}{5}, 54}$
$\beta_{s_0}^{l.o.f_0} = \beta_{R_{s_0}^{l.o.f_0}, T_{s_0}^{l.o.f_0}}$	$R_{e2e}^{l.o.f_0} = R_{s_0} - r_{s_0}^{x(f_0)}$	$= 10 - 5\frac{2}{5}$
		$= 4\frac{3}{5}$
	$T_{e2e}^{l.o.f_0} = T_{s_0} + \frac{b_{s_0}^{\bar{x}(f_0)} + r_{s_0}^{x(f_0)} \cdot T_{s_0}}{R_{e2e}^{l.o.f_0}}$	$= 10 + \frac{54 + 5\frac{2}{5} \cdot 10}{4\frac{3}{5}}$
		$= 10 + \frac{108}{4\frac{3}{5}}$
	$=$	$= 33\frac{11}{23}$
	$=$	$= \beta_{4\frac{3}{5}, 33\frac{11}{23}}$
D^{f_0}	$\beta_{e2e}^{l.o.f_0} = b^{f_0}$	$4\frac{3}{5} \cdot [t - 33\frac{11}{23}]^+ = 1$
		$t = 33\frac{16}{23}$
B^{f_0}	$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = \frac{1}{10} \cdot 33\frac{11}{23} + 1$	$= 4\frac{8}{23}$

Flow f_6

SFA		FIFO_MUX	ARB_MUX	
s ₀	$\alpha^{x(f_6)} = \sum_{n=0}^5 \alpha^{f_n} + \sum_{n=7}^9 \alpha^{f_n} = \gamma_{r_{s_0}^{x(f_6)}, b_{s_0}^{x(f_6)}}$	$r_{s_0}^{x(f_6)}$	$(\sum_{n=0}^9 r^{f_n}) - r^{f_6} = 4\frac{4}{5}$	
		$b_{s_0}^{x(f_6)}$	$(\sum_{n=0}^9 b^{f_n}) - b^{f_6} = 48$	
		=	$= \gamma_{4\frac{4}{5}, 48}$	
	$\beta_{s_0}^{1.o.f_6} = \beta_{s_0} \ominus \alpha_{s_0}^{x(f_6)} = \beta_{R_{s_0}^{1.o.f_6}, T_{s_0}^{1.o.f_6}}$	$R_{s_0}^{1.o.f_6}$	$[R_{s_0} - r_{s_0}^{x(f_6)}]^+ = 5\frac{1}{5}$	$\beta_{s_0} = \alpha_{s_0}^{x(f_6)}$
		$T_{s_0}^{1.o.f_6}$	$10 \cdot [t - 10]^+ = 48$ $t = 14\frac{4}{5}$	$10 \cdot [t - 10]^+ = 4\frac{4}{5} \cdot t + 48$ $t = 28\frac{6}{13}$
		=	$= \beta_{5\frac{1}{5}, 14\frac{4}{5}}$	$= \beta_{5\frac{1}{5}, 28\frac{6}{13}}$
		$\beta_{e2e}^{1.o.f_6} = \beta_{R_{e2e}^{1.o.f_6}, T_{e2e}^{1.o.f_6}}$	$= \beta_{5\frac{1}{5}, 14\frac{4}{5}}$	$= \beta_{5\frac{1}{5}, 28\frac{6}{13}} = \beta_{s_0}^{1.o.f_6}$
	D^{f_6}	$\beta_{e2e}^{1.o.f_6} = b^{f_6}$	$\beta_{e2e}^{1.o.f_6} = b^{f_6}$	$\beta_{e2e}^{1.o.f_6} = b^{f_6}$
		$5\frac{1}{5} \cdot [t - 14\frac{4}{5}]^+ = 7$ $t = 16\frac{19}{130}$	$5\frac{1}{5} \cdot [t - 28\frac{6}{13}]^+ = 7$ $t = 29\frac{21}{26}$	
	B^{f_6}	$\alpha^{f_6}(T_{e2e}^{1.o.f_6}) = \frac{7}{10} \cdot 14\frac{4}{5} + 7$	$\alpha^{f_6}(T_{e2e}^{1.o.f_6}) = \frac{7}{10} \cdot 28\frac{6}{13} + 7$	
$= 17\frac{9}{25}$		$= 26\frac{12}{13}$		

PMOO		ARB_MUX
s_0	$\alpha^{\bar{x}(f_6)} = \sum_{n=0}^5 \alpha^{f_n} + \sum_{n=7}^9 \alpha^{f_n} = \gamma_{r_{s_0}^{x(f_6)}, b_{s_0}^{x(f_6)}}$	$= \gamma_{4\frac{4}{5}, 48}$
	$\alpha^{x(f_6)} = \sum_{n=0}^5 \alpha^{f_n} + \sum_{n=7}^9 \alpha^{f_n} = \gamma_{r_{s_0}^{x(f_6)}, b_{s_0}^{x(f_6)}}$	$= \gamma_{4\frac{4}{5}, 48}$
$\beta_{s_0}^{1.o.f_6} = \beta_{R_{s_0}^{1.o.f_6}, T_{s_0}^{1.o.f_6}}$	$R_{e2e}^{1.o.f_6} = R_{s_0} - r_{s_0}^{x(f_6)}$	$= 10 - 4\frac{4}{5}$ $= 5\frac{1}{5}$
	$T_{e2e}^{1.o.f_6} = T_{s_0} + \frac{b_{s_0}^{\bar{x}(f_6)} + r_{s_0}^{x(f_6)} \cdot T_{s_0}}{R_{e2e}^{1.o.f_6}}$	$= 10 + \frac{48 + 4\frac{4}{5} \cdot 10}{5\frac{1}{5}}$ $= 10 + \frac{96}{5\frac{1}{5}}$ $= 28\frac{6}{13}$
	$=$	$= \beta_{5\frac{1}{5}, 28\frac{6}{13}}$
D^{f_6}	$\beta_{e2e}^{1.o.f_6} = b^{f_6}$ $5\frac{1}{5} \cdot [t - 28\frac{6}{13}]^+ = 7$ $t = 29\frac{21}{26}$	
B^{f_6}	$\alpha^{f_6}(T_{e2e}^{1.o.f_6}) = \frac{7}{10} \cdot 28\frac{6}{13} + 7$ $= 26\frac{12}{13}$	