

---

## Exercise Sheet 6

### Performance Modeling of Distributed Systems

Winter Term 2013/2014

#### Assignment 1 (Network Analysis)

Assume a dynamic  $S$ -server and two incoming flows  $A_1$  and  $A_2$ . Consider flow  $A_1$  to have priority over  $A_2$ , i.e. the service  $A_2$  receives, is the leftover service, which results after serving  $A_1$ . Derive the backlog bound for  $A_2$  for the case that

- $S, A_1$  and  $A_2$  being  $\sigma(\theta), \rho(\theta)$ -bounded.
- $S, A_1$  and  $A_2$  being tailbounded.

Hint:  $A_1$  and  $A_2$  are not assumed to be stochastically independent!

#### Assignment 2 (An Lower Output Bound)

Assume a dynamic  $S$ -server to be  $(\sigma_S(\theta), \rho_S(\theta))$ -bounded and a flow  $A$  to be  $(\sigma_A(\theta), \rho_A(\theta))$ -bounded, with  $-\rho_S(\theta) \rho_A(\theta)$ . Derive for a fitting  $\sigma$  the following lower output bound for the departure process  $D$ :

$$\mathbb{E}(e^{-\theta D(m,n)}) \leq e^{\theta\sigma(\theta) - \rho_A(\theta)(n-m)}$$