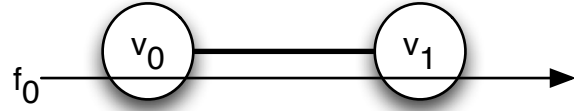


Tandem_1SC_1Flow.java



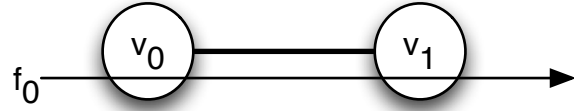
- $\beta_{v_0} = \beta_{v_1} = \beta_{R_{v_i}, T_{v_i}} = \beta_{10, 10}, i \in \{0, 1\}$
- $\alpha^{f_0} = \gamma_{r^{f_0}, b^{f_0}} = \gamma_{5, 25}$

TFA		FIFO_MUX	ARB_MUX
v_0	$\alpha_{v_0}^{\text{sum}}$	$= \gamma_{r_{v_0}^{\text{sum}}, b_{v_0}^{\text{sum}}} = \alpha^{f_0}$	
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}^{\text{sum}}$ $10 \cdot [t - 10]^+ = 25$ $t = 12.5$	$\beta_{v_0} = \alpha_{v_0}^{\text{sum}}$ $10 \cdot [t - 10]^+ = 5 \cdot t + 25$ $t = 25$
	$B_{v_1}^{f_0}$	$\alpha_{v_0}^{\text{sum}}(T_{v_0}) = 5 \cdot 10 + 25$ $= 75$	
v_1	$\alpha_{v_1}^{\text{sum}} = (\alpha_{v_0}^{\text{sum}})^*$	$r_{\alpha_{v_1}^{\text{sum}}}$	$= r_{v_0}^{\text{sum}} = r^{f_0} = 5$
		$b_{\alpha_{v_1}^{\text{sum}}}$	$\alpha_{v_0}^{\text{sum}}(T_{v_0}) = 75$
		$=$	$= \gamma_{5, 75}$
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{\alpha_{v_1}^{\text{sum}}}$ $10 \cdot [t - 10]^+ = 75$ $t = 17.5$	$\beta_{v_1} = \alpha_{v_1}^{\text{sum}}$ $10 \cdot [t - 10]^+ = 5 \cdot t + 75$ $t = 35$
	$B_{v_1}^{f_0}$	$\alpha_{v_1}^{\text{sum}}(T_{v_1}) = 5 \cdot 10 + 75$ $= 125$	
D^{f_0}		$\sum_{i=0}^1 D_{v_i}^{f_0} = 30$	$\sum_{i=0}^1 D_{v_i}^{f_0} = 60$
B^{f_0}		$\max_i b_{v_i}^{f_0} = 125$	

SFA			FIFO_MUX	ARB_MUX
v ₀	crosstraffic α ^{xf₀} _{v₀} = γ _{r^{xf₀}_{v₀}, b^{xf₀}_{v₀}}	r ^{xf₀} _{v₀}	0	
		b ^{xf₀} _{v₀}	0	
		=	= γ _{0,0}	
	left over service β ^{l.o.f₀} _{v₀} = β _{R^{l.o.f₀}_{v₀}, T^{l.o.f₀}_{v₀}}	R ^{l.o.f₀} _{v₀}	[R _{v₀} − r ^{xf₀} _{v₀}] ⁺ = 10	
		T ^{l.o.f₀} _{v₀}	β _{v₀} = b ^{xf₀} _{v₀} 10 · [t − 10] ⁺ = 0 t = 10	β _{v₀} = α ^{xf₀} _{v₀} 10 · [t − 10] ⁺ = 0 · t + 0 t = 10
		=	= β _{10,10} = β _{v₀}	
		=	= β _{10,10} = β _{v₀}	
	output of crosstraffic to same next node α ^{xf₀} _{v₀v₁} = γ _{r^{xf₀}_{v₀v₁}, b^{xf₀}_{v₀v₁}}	r ^{xf₀} _{v₀v₁}	0	
		b ^{xf₀} _{v₀v₁}	0	
		=	= γ _{0,0}	
v ₁	crosstraffic α ^{xf₀} _{v₁} = γ _{r^{xf₀}_{v₁}, b^{xf₀}_{v₁}}	r ^{xf₀} _{v₁}	0	
		b ^{xf₀} _{v₁}	0	
		=	= γ _{0,0}	
	left over service β ^{l.o.f₀} _{v₁} = β _{R^{l.o.f₀}_{v₁}, T^{l.o.f₀}_{v₁}}	R ^{l.o.f₀} _{v₁}	[R _{v₁} − r ^{xf₀} _{v₁}] ⁺ = 10	
		T ^{l.o.f₀} _{v₁}	β _{v₁} = b ^{xf₀} _{v₁} t = 10	β _{v₁} = α ^{xf₀} _{v₁} t = 10
		=	= β _{10,10} = β _{v₁}	
		=	= β _{10,10} = β _{v₁}	
	output of crosstraffic not needed			
β ^{l.o.f₀} _{e2e} = β _{R^{l.o.f₀}_{e2e}, T^{l.o.f₀}_{e2e}}		⊗ ¹ _{i=0} β ^{l.o.f₀} _{v_i} = β _{10,20}		
D ^{f₀}		β ^{l.o.f₀} _{e2e} = b ^{f₀} 10 · [t − 20] ⁺ = 25 t = 22.5		
B ^{f₀}		α ^{f₀} (T ^{l.o.f₀} _{e2e}) = 5 · 20 + 25 = 125		

PMOO		ARB_MUX
$\beta_{e2e} = \beta_{R_{e2e}, T_{e2e}}$		$\bigotimes_{i=0}^1 \beta_{v_i} = \beta_{10,20}$
crosstraffic $\alpha_{e2e}^{xf_0} = \gamma_{r_{e2e}^{xf_0}, b_{e2e}^{xf_0}}$	$r_{e2e}^{xf_0}$	0
	$b_{e2e}^{xf_0}$	0
	=	= $\gamma_{0,0}$
left over service $\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$	$R_{e2e}^{l.o.f_0}$	$[R_{e2e} - r_{e2e}^{xf_0}]^+ = 10$
	$T_{e2e}^{l.o.f_0}$	$\beta_{e2e} = \alpha_{e2e}^{xf_0}$ $t = 20$
	=	$\beta_{10,20} = \beta_{e2e}$
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$
		$10 \cdot [t - 20]^+ = 25$
		$t = 22.5$
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 20 + 25$
		= 125

Tandem_2SCs_1Flow.java



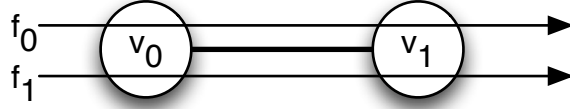
- $\beta_{v_0} = \beta_{R_{v_0}, T_{v_0}} = \beta_{10,10}$
- $\beta_{v_1} = \beta_{R_{v_1}, T_{v_1}} = \beta_{6,6}$
- $\alpha^{f_0} = \gamma_{r^{f_0}, b^{f_0}} = \gamma_{5,25}$

TFA		FIFO_MUX	ARB_MUX
v_0	$\alpha_{v_0}^{\text{sum}}$	$= \gamma_{r_{v_0}^{\text{sum}}, b_{v_0}^{\text{sum}}} = \alpha^{f_0}$	
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}^{\text{sum}}$ $10 \cdot [t - 10]^+ = 25$ $t = 12.5$	$\beta_{v_0} = \alpha_{v_0}^{\text{sum}}$ $10 \cdot [t - 10]^+ = 5 \cdot t + 25$ $t = 25$
	$B_{v_1}^{f_0}$	$\alpha_{v_0}^{\text{sum}}(T_{v_0}) = 5 \cdot 10 + 25$ $= 75$	
v_1	$\alpha_{v_1}^{\text{sum}} = (\alpha_{v_0}^{\text{sum}})^*$	$r_{\alpha_{v_1}^{\text{sum}}}$	$= r_{v_0}^{\text{sum}} = r^{f_0} = 5$
		$b_{\alpha_{v_1}^{\text{sum}}}$	$\alpha_{v_0}^{\text{sum}}(T_{v_0}) = 75$
		$=$	$= \gamma_{5,75}$
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{\alpha_{v_1}^{\text{sum}}}$ $6 \cdot [t - 6]^+ = 75$ $t = 18\frac{1}{2}$	$\beta_{v_1} = \alpha_{v_1}^{\text{sum}}$ $6 \cdot [t - 6]^+ = 5 \cdot t + 75$ $t = 111$
	$B_{v_1}^{f_0}$	$\alpha_{v_1}^{\text{sum}}(T_{v_1}) = 5 \cdot 6 + 75$ $= 105$	
D^{f_0}		$\sum_{i=0}^1 D_{v_i}^{f_0} = 31$	$\sum_{i=0}^1 D_{v_i}^{f_0} = 136$
B^{f_0}		$\max_i b_{v_i}^{f_0} = 105$	

SFA			FIFO _ MUX		ARB _ MUX	
v_0	crosstraffic $\alpha_{v_0}^{xf_0} = \gamma_{r_{v_0}^{xf_0}, b_{v_0}^{xf_0}}$	$r_{v_0}^{xf_0}$	0			
		$b_{v_0}^{xf_0}$	0			
		=	$= \gamma_{0,0}$			
	left over service $\beta_{v_0}^{l.o.f_0} = \beta_{R_{v_0}^{l.o.f_0}, T_{v_0}^{l.o.f_0}}$	$R_{v_0}^{l.o.f_0}$	$[R_{v_0} - r_{v_0}^{xf_0}]^+ = 10$			
		$T_{v_0}^{l.o.f_0}$	$\beta_{v_0} = b_{v_0}^{xf_0}$ $10 \cdot [t - 10]^+ =$ $t =$	$\beta_{v_0} = \alpha_{v_0}^{xf_0}$ $10 \cdot [t - 10]^+ =$ $t =$	$\alpha_{v_0}^{xf_0}$ $0 \cdot t + 0$ 10	
		=	$= \beta_{10,10} = \beta_{v_0}$			
	output of crosstraffic to same next node $\alpha_{v_0 v_1}^{xf_0} = \gamma_{r_{v_0 v_1}^{xf_0}, b_{v_0 v_1}^{xf_0}}$	$r_{v_0 v_1}^{xf_0}$	0			
		$b_{v_0 v_1}^{xf_0} = B_{v_0}^{xf_0}$	0			
		=	$= \gamma_{0,0}$			
	v_1	crosstraffic $\alpha_{v_1}^{xf_0} = \gamma_{r_{v_1}^{xf_0}, b_{v_1}^{xf_0}}$	$r_{v_1}^{xf_0}$	0		
$b_{v_1}^{xf_0}$			0			
=			$= \gamma_{0,0}$			
left over service $\beta_{v_1}^{l.o.f_0} = \beta_{R_{v_1}^{l.o.f_0}, T_{v_1}^{l.o.f_0}}$		$R_{v_1}^{l.o.f_0}$	$[R_{v_1} - r_{v_1}^{xf_0}]^+ = 6$			
		$T_{v_1}^{l.o.f_0}$	$\beta_{v_1} = b_{v_1}^{xf_0}$ $6 \cdot [t - 6]^+ =$ $t =$	$\beta_{v_1} = \alpha_{v_1}^{xf_0}$ $t =$	$\alpha_{v_1}^{xf_0}$ 6	
		=	$= \beta_{6,6} = \beta_{v_1}$			
output of crosstraffic not needed						
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$		$\bigotimes_{i=0}^1 \beta_{v_i}^{l.o.f_0} = \beta_{6,16}$				
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $6 \cdot [t - 16]^+ =$ $t =$				
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) =$ $=$				

PMOO		ARB_MUX
$\beta_{e2e} = \beta_{R_{e2e}, T_{e2e}}$		$\bigotimes_{i=0}^1 \beta_{v_i} = \beta_{6,16}$
crosstraffic $\alpha_{e2e}^{xf_0} = \gamma_{r_{e2e}^{xf_0}, b_{e2e}^{xf_0}}$	$r_{e2e}^{xf_0}$	0
	$b_{e2e}^{xf_0}$	0
	=	= $\gamma_{0,0}$
left over service $\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$	$R_{e2e}^{l.o.f_0}$	$[R_{e2e} - r_{e2e}^{xf_0}]^+ = 6$
	$T_{e2e}^{l.o.f_0}$	$\beta_{e2e} = \alpha_{e2e}^{xf_0}$ $t = 16$
	=	$\beta_{6,16} = \beta_{e2e}$
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $6 \cdot [t - 16]^+ = 25$ $t = 20\frac{1}{6}$
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 16 + 25$ = 105

Tandem_1SC_2Flows_1AC_1Path.java



- $\beta_{v_0} = \beta_{v_1} = \beta_{R_{v_i}, T_{v_i}} = \beta_{10,10}, i \in \{0,1\}$
- $\alpha^{f_0} = \alpha^{f_1} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}, j \in \{0,1\}$

Flows f_0, f_1

TFA results will be equal for all flows as they share the same path of servers.

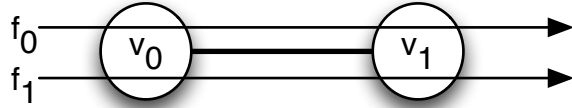
SFA, PMOO results will be equal for all flows as they share the same path of servers and the same arrival curves.

TFA		FIFO_MUX	ARB_MUX
v_0	$\alpha_{v_0}^{\text{sum}} = \gamma^{\text{sum}} = \gamma_{r_{v_0}^{\text{sum}}, b_{v_0}^{\text{sum}}}$	$\sum_{j=0}^1 \alpha^{f_j} = \gamma_{10,50}$	
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}^{\text{sum}}$ $10 \cdot [t - 10]^+ = 50$ $t = 15$	$\beta_{v_0} = \alpha_{v_0}^{\text{sum}}$ $10 \cdot [t - 10]^+ = 10 \cdot t + 50$ $0 \cdot t = 150$ $\Rightarrow D_{v_0}^{f_0} = \infty$
	$B_{v_1}^{f_0}$	$\alpha_{v_0}^{\text{sum}}(T_{v_0}) = 10 \cdot 10 + 50$ $= 150$	
v_1	$\alpha_{v_1}^{\text{sum}} = (\alpha_{v_0}^{\text{sum}})^*$	$r_{\alpha_{v_1}^{\text{sum}}}$	$= r_{v_0}^{\text{sum}} = 10$
		$b_{\alpha_{v_1}^{\text{sum}}}$	$\alpha_{v_0}^{\text{sum}}(T_{v_0}) = 150$
		$=$	$= \gamma_{10,150}$
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{\alpha_{v_1}^{\text{sum}}}$ $10 \cdot [t - 10]^+ = 150$ $t = 25$	$\beta_{v_1} = \alpha_{v_1}^{\text{sum}}$ $10 \cdot [t - 10]^+ = 10 \cdot t + 150$ $0 \cdot t = 250$ $\Rightarrow D_{v_1}^{f_0} = \infty$
	$B_{v_1}^{f_0}$	$\alpha_{v_1}^{\text{sum}}(T_{v_1}) = 10 \cdot 10 + 150$ $= 250$	
D^{f_0}		$\sum_{i=0}^1 D_{v_i}^{f_0} = 40$	$\sum_{i=0}^1 D_{v_i}^{f_0} = \infty$
B^{f_0}		$\max_i b_{v_i}^{f_0} = 250$	

SFA			FIFO_MUX		ARB_MUX	
v ₀	crosstraffic $\alpha_{v_0}^{xf_0} = \gamma_{r_{v_0}^{xf_0}, b_{v_0}^{xf_0}}$	$r_{v_0}^{xf_0}$	$r_{v_0}^{f_1} = r^{f_1} = 5$			
		$b_{v_0}^{xf_0}$	$b_{v_0}^{f_1} = b^{f_1} = 25$			
		=	$\gamma_{5,25} = \alpha^{f_1}$			
	left over service $\beta_{v_0}^{l.o.f_0} = \beta_{R_{v_0}^{l.o.f_0}, T_{v_0}^{l.o.f_0}}$	$R_{v_0}^{l.o.f_0}$	$[R_{v_0} - r_{v_0}^{xf_0}]^+ = 5$			
		$T_{v_0}^{l.o.f_0}$	$\beta_{v_0} = b_{v_0}^{xf_0}$ $10 \cdot [t - 10]^+ = 25$ $t = 12.5$	$\beta_{v_0} = \alpha_{v_0}^{xf_0}$ $10 \cdot [t - 10]^+ = 5 \cdot t + 25$ $t = 25$		
		=	$= \beta_{5,12.5}$		$= \beta_{5,25}$	
	output of crosstraffic to same next node $\alpha_{v_0 v_1}^{xf_0} = \gamma_{r_{v_0 v_1}^{xf_0}, b_{v_0 v_1}^{xf_0}}$	$r_{v_0 v_1}^{xf_0}$	$r_{v_0}^{f_1} = r^{f_1} = 5$			
		$b_{v_0 v_1}^{xf_0} = B_{v_0}^{xf_0}$	$\alpha_{v_0}^{xf_0}(T_{v_0}) = 5 \cdot 10 + 25$ $= 75$			
=		$= \gamma_{5,75}$				
v ₁	crosstraffic $\alpha_{v_1}^{xf_0} = \gamma_{r_{v_1}^{xf_0}, b_{v_1}^{xf_0}}$	$r_{v_1}^{xf_0}$	$= 5$			
		$b_{v_1}^{xf_0}$	$= 75$			
		=	$= \gamma_{5,75}$			
	left over service $\beta_{v_1}^{l.o.f_0} = \beta_{R_{v_1}^{l.o.f_0}, T_{v_1}^{l.o.f_0}}$	$R_{v_1}^{l.o.f_0}$	$[R_{v_1} - r_{v_1}^{xf_0}]^+ = 5$			
		$T_{v_1}^{l.o.f_0}$	$\beta_{v_1} = b_{v_1}^{xf_0}$ $10 \cdot [t - 10]^+ = 75$ $t = 17.5$	$\beta_{v_1} = \alpha_{v_1}^{xf_0}$ $10 \cdot [t - 10]^+ = 5 \cdot t + 75$ $t = 35$		
		=	$= \beta_{5,17.5}$		$= \beta_{5,35}$	
	output of crosstraffic not needed					
	$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$		$\bigotimes_{i=0}^1 \beta_{v_i}^{l.o.f_0} = \beta_{5,30}$		$\bigotimes_{i=0}^1 \beta_{v_i}^{l.o.f_0} = \beta_{5,60}$	
D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $5 \cdot [t - 30]^+ = 25$ $t = 35$		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $5 \cdot [t - 60]^+ = 25$ $t = 65$		
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 30 + 25$ $= 175$		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 60 + 25$ $= 325$		

PMOO	ARB_MUX
$\beta_{e2e} = \beta_{R_{e2e}, T_{e2e}}$	$\bigotimes_{i=0}^1 \beta_{v_i} = \beta_{10,20}$
crosstraffic	$r_{v_0}^{f_1} = r^{f_1} = 5$
$\alpha_{e2e}^{xf_0} = \gamma_{r_{e2e}^{xf_0}, b_{e2e}^{xf_0}}$	$b_{v_0}^{f_1} = b^{f_1} = 25$
$=$	$= \gamma_{5,25}$
left over service	$[R_{e2e} - r_{e2e}^{xf_0}]^+ = 5$
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$	$\beta_{e2e} = \alpha_{e2e}^{xf_0}$
$T_{e2e}^{l.o.f_0}$	$10 \cdot [t - 20]^+ = 5 \cdot t + 25$
$=$	$t = 45$
	$= \beta_{5,45}$
D^{f_0}	$\beta_{e2e}^{l.o.f_0} = b^{f_0}$
	$5 \cdot [t - 45]^+ = 25$
	$t = 50$
B^{f_0}	$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 45 + 25$
	$= 250$

Tandem_2SCs_2Flows_1AC_1Path.java



- $\beta_{v_0} = \beta_{R_{v_0}, T_{v_0}} = \beta_{10,10}$
- $\beta_{v_1} = \beta_{R_{v_1}, T_{v_1}} = \beta_{6,6}$
- $\alpha^{f_0} = \alpha^{f_1} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{2.5,12.5}, j \in \{0, 1\}$

Flows f_0, f_1

TFA results will be equal for all flows as they share the same path of servers.

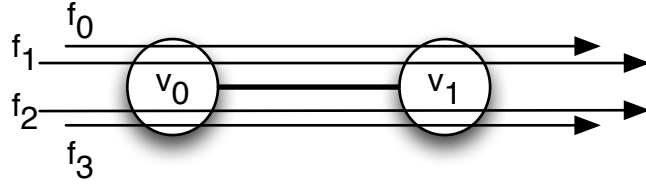
SFA, PMOO results will be equal for all flows as they share the same path of servers and the same arrival curves.

TFA		FIFO_MUX	ARB_MUX
v_0	$\alpha_{v_0}^{\text{sum}} = \gamma^{\text{sum}} = \gamma_{r_{v_0}^{\text{sum}}, b_{v_0}^{\text{sum}}}$	$\sum_{j=0}^1 \alpha^{f_j} = \gamma_{5,25}$	
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}^{\text{sum}}$ $10 \cdot [t - 10]^+ = 25$ $t = 12.5$	$\beta_{v_0} = \alpha_{v_0}^{\text{sum}}$ $10 \cdot [t - 10]^+ = 5 \cdot t + 25$ $t = 25$
	$B_{v_1}^{f_0}$	$\alpha_{v_0}^{\text{sum}}(T_{v_0}) = 5 \cdot 10 + 25$ $= 75$	
v_1	$\alpha_{v_1}^{\text{sum}} = (\alpha_{v_0}^{\text{sum}})^*$	$r_{\alpha_{v_1}^{\text{sum}}}$	$= r_{v_0}^{\text{sum}} = 5$
		$b_{\alpha_{v_1}^{\text{sum}}}$	$\alpha_{v_0}^{\text{sum}}(T_{v_0}) = 75$
		$=$	$= \gamma_{5,75}$
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{\alpha_{v_1}^{\text{sum}}}$ $6 \cdot [t - 6]^+ = 75$ $t = 18\frac{1}{2}$	$\beta_{v_1} = \alpha_{v_1}^{\text{sum}}$ $6 \cdot [t - 6]^+ = 5 \cdot t + 75$ $t = 111$
	$B_{v_1}^{f_0}$	$\alpha_{v_1}^{\text{sum}}(T_{v_1}) = 5 \cdot 6 + 75$ $= 105$	
D^{f_0}		$\sum_{i=0}^1 D_{v_i}^{f_0} = 31$	$\sum_{i=0}^1 D_{v_i}^{f_0} = 136$
$B^{f_0} = \max_i b_{v_i}^{f_0}$		$= 105$	

SFA			FIFO_MUX	ARB_MUX		
v ₀	crosstraffic α _{v₀} ^{x_{f₀}} = γ _{r_{v₀}^{x_{f₀}}, b_{v₀}^{x_{f₀}}}	r _{v₀} ^{x_{f₀}}	r _{v₀} ^{f₁} = r ^{f₁} = 2.5			
		b _{v₀} ^{x_{f₀}}	b _{v₀} ^{f₁} = b ^{f₁} = 12.5			
		=	= γ _{2.5, 12.5} = α ^{f₁}			
	left over service β _{v₀} ^{l.o.f₀} = β _{R_{v₀}^{l.o.f₀}, T_{v₀}^{l.o.f₀}}	R _{v₀} ^{l.o.f₀}	[R _{v₀} − r _{v₀} ^{x_{f₀}}] ⁺ = 7.5			
		T _{v₀} ^{l.o.f₀}	β _{v₀} = b _{v₀} ^{x_{f₀}} 10 · [t − 10] ⁺ = 12.5 t = 11.25	β _{v₀} = α _{v₀} ^{x_{f₀}} 10 · [t − 10] ⁺ = 2.5 · t + 12.5 t = 15		
		=	= β _{7.5, 11.25}			
	output of crosstraffic to same next node α _{v₀v₁} ^{x_{f₀}} = γ _{r_{v₀v₁}^{x_{f₀}}, b_{v₀v₁}^{x_{f₀}}}	r _{v₀v₁} ^{x_{f₀}}	r _{v₀} ^{f₁} = r ^{f₁} = 2.5			
		b _{v₀v₁} ^{x_{f₀}} = B _{v₀} ^{x_{f₀}}	α _{v₀} ^{x_{f₀}} (T _{v₀}) = 2.5 · 10 + 12.5 = 37.5			
		=	= γ _{2.5, 37.5}			
v ₁	crosstraffic α _{v₁} ^{x_{f₀}} = γ _{r_{v₁}^{x_{f₀}}, b_{v₁}^{x_{f₀}}}	r _{v₁} ^{x_{f₀}}	2.5			
		b _{v₁} ^{x_{f₀}}	37.5			
		=	= γ _{2.5, 37.5}			
	left over service β _{v₁} ^{l.o.f₀} = β _{R_{v₁}^{l.o.f₀}, T_{v₁}^{l.o.f₀}}	R _{v₁} ^{l.o.f₀}	[R _{v₁} − r _{v₁} ^{x_{f₀}}] ⁺ = 3.5			
		T _{v₁} ^{l.o.f₀}	β _{v₁} = b _{v₁} ^{x_{f₀}} 6 · [t − 6] ⁺ = 37.5 t = 12.25	β _{v₁} = α _{v₁} ^{x_{f₀}} 6 · [t − 6] ⁺ = 2.5 · t + 37.5 t = 21		
		=	= β _{3.5, 12.25}			
	output of crosstraffic not needed					
	β _{e2e} ^{l.o.f₀} = β _{R_{e2e}^{l.o.f₀}, T_{e2e}^{l.o.f₀}}		⊗ _{i=0} ¹ β _{v_i} ^{l.o.f₀} = β _{3.5, 23.5}		⊗ _{i=0} ¹ β _{v_i} ^{l.o.f₀} = β _{3.5, 36}	
	D ^{f₀}		β _{e2e} ^{l.o.f₀} = b ^{f₀} 3.5 · [t − 23.5] ⁺ = 12.5 t = 27 ¹ / ₁₄		β _{e2e} ^{l.o.f₀} = b ^{f₀} 3.5 · [t − 36] ⁺ = 12.5 t = 39 ⁴ / ₇	
	B ^{f₀}		α ^{f₀} (T _{e2e} ^{l.o.f₀}) = 2.5 · 23.5 + 12.5 = 71.25		α ^{f₀} (T _{e2e} ^{l.o.f₀}) = 2.5 · 36 + 12.5 = 102.5	

PMOO	ARB_MUX
$\beta_{e2e} = \beta_{R_{e2e}, T_{e2e}}$	$\bigotimes_{i=0}^1 \beta_{v_i} = \beta_{6,16}$
crosstraffic	$r_{v_0}^{f_1} = r^{f_1} = 2.5$
$\alpha_{e2e}^{xf_0} = \gamma_{r_{e2e}^{xf_0}, b_{e2e}^{xf_0}}$	$b_{v_0}^{f_1} = b^{f_1} = 12.5$
$=$	$= \gamma_{2.5, 12.5}$
left over service	$[R_{e2e} - r_{e2e}^{xf_0}]^+ = 3.5$
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$	$\beta_{e2e} = \alpha_{e2e}^{xf_0}$
$T_{e2e}^{l.o.f_0}$	$6 \cdot [t - 16]^+ = 2.5 \cdot t + 12.5$
$=$	$t = 31$
	$= \beta_{3.5, 31}$
D^{f_0}	$\beta_{e2e}^{l.o.f_0} = b^{f_0}$
	$3.5 \cdot [t - 31]^+ = 12.5$
	$t = 34\frac{4}{7}$
B^{f_0}	$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 2.5 \cdot 31 + 12.5$
	$= 90$

Tandem_1SCs_4Flows_1ACs_1Path.java



- $\beta_{v_0} = \beta_{v_1} = \beta_{R_{v_i}, T_{v_i}} = \beta_{10,10}, i \in \{0,1\}$
- $\alpha^{f_i} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{2,10}, j \in \{0,3\}$

Flows f_0, f_1, f_2, f_3

TFA results will be equal for all flows as they share the same path of servers.

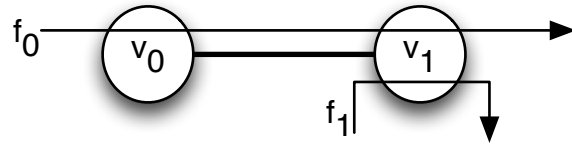
SFA, PMOO results will be equal for all flows as they share the same path of servers and the same arrival curves.

TFA		FIFO_MUX	ARB_MUX
v_0	$\alpha_{v_0}^{\text{sum}} = \gamma^{\text{sum}} = \gamma_{r_{v_0}^{\text{sum}}, b_{v_0}^{\text{sum}}}$	$\sum_{j=0}^3 \alpha^{f_j} = \gamma_{8,40}$	
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}^{\text{sum}}$ $10 \cdot [t - 10]^+ = 40$ $t = 14$	$\beta_{v_0} = \alpha_{v_0}^{\text{sum}}$ $10 \cdot [t - 10]^+ = 8 \cdot t + 40$ $t = 70$
	$B_{v_1}^{f_0}$	$\alpha_{v_0}^{\text{sum}}(T_{v_0}) = 8 \cdot 10 + 40$ $= 120$	
v_1	$\alpha_{v_1}^{\text{sum}} = (\alpha_{v_0}^{\text{sum}})^*$	$r_{\alpha_{v_1}^{\text{sum}}}$	$= r_{v_0}^{\text{sum}} = 8$
		$b_{\alpha_{v_1}^{\text{sum}}}$	$\alpha_{v_0}^{\text{sum}}(T_{v_0}) = 120$
		$=$	$= \gamma_{8,120}$
	$D_{v_1}^{f_j}$	$\beta_{v_1} = b_{\alpha_{v_1}^{\text{sum}}}$ $10 \cdot [t - 10]^+ = 120$ $t = 22$	$\beta_{v_1} = \alpha_{v_1}^{\text{sum}}$ $10 \cdot [t - 10]^+ = 8 \cdot t + 120$ $t = 110$
	$B_{v_1}^{f_j}$	$\alpha_{v_1}^{\text{sum}}(T_{v_1}) = 8 \cdot 10 + 120$ $= 200$	
D^{f_j}		$\sum_{i=0}^1 D_{v_i}^{f_j} = 36$	$\sum_{i=0}^1 D_{v_i}^{f_j} = 180$
$B^{f_j} = \max_i b_{v_i}^{f_j}$		$= 200$	

SFA			FIFO_MUX	ARB_MUX
v ₀	crosstraffic $\alpha_{v_0}^{xf_j} = \gamma_{r_{v_0}^{xf_j}, b_{v_0}^{xf_j}}$	$r_{v_0}^{xf_j}$	$\sum_{j=0}^2 r^{f_j} = 6$	
		$b_{v_0}^{xf_j}$	$\sum_{j=0}^3 b^{f_j} = 30$	
		=	$\gamma_{6,30} = \sum_{j=0}^3 \alpha^{f_j}$	
	left over service $\beta_{v_0}^{l.o.f_j} = \beta_{R_{v_0}^{l.o.f_j}, T_{v_0}^{l.o.f_j}}$	$R_{v_0}^{l.o.f_j}$	$[R_{v_0} - r_{v_0}^{xf_j}]^+ = 4$	
		$T_{v_0}^{l.o.f_j}$	$\beta_{v_0} = b_{v_0}^{xf_0}$ $10 \cdot [t - 10]^+ = 30$ $t = 13$	$\beta_{v_0} = \alpha_{v_0}^{xf_j}$ $10 \cdot [t - 10]^+ = 6 \cdot t + 30$ $t = 32.5$
		=	$= \beta_{4,13}$	$= \beta_{4,32.5}$
		=	$= \beta_{4,32.5}$	
	output of crosstraffic to same next node $\alpha_{v_0 v_1}^{xf_j} = \gamma_{r_{v_0 v_1}^{xf_j}, b_{v_0 v_1}^{xf_j}}$	$r_{v_0 v_1}^{xf_j}$	$= r_{v_0}^{xf_j} = 6$	
		$b_{v_0 v_1}^{xf_j} = B_{v_0}^{xf_j}$	$\alpha_{v_0}^{xf_j}(T_{v_0}) = 6 \cdot 10 + 30$ $= 90$	
		=	$= \gamma_{6,90}$	
v ₁	crosstraffic $\alpha_{v_1}^{xf_j} = \gamma_{r_{v_1}^{xf_j}, b_{v_1}^{xf_j}}$	$r_{v_1}^{xf_j}$	6	
		$b_{v_1}^{xf_0}$	90	
		=	$= \gamma_{6,90}$	
	left over service $\beta_{v_1}^{l.o.f_j} = \beta_{R_{v_1}^{l.o.f_j}, T_{v_1}^{l.o.f_j}}$	$R_{v_1}^{l.o.f_j}$	$[R_{v_1} - r_{v_1}^{xf_j}]^+ = 4$	
		$T_{v_1}^{l.o.f_j}$	$\beta_{v_1} = b_{v_1}^{xf_0}$ $10 \cdot [t - 10]^+ = 90$ $t = 19$	$\beta_{v_1} = \alpha_{v_1}^{xf_j}$ $10 \cdot [t - 10]^+ = 4 \cdot t + 90$ $t = 47.5$
		=	$= \beta_{4,19}$	$= \beta_{4,47.5}$
		=	$= \beta_{4,47.5}$	
	output of crosstraffic not needed			
	$\beta_{e2e}^{l.o.f_j} = \beta_{R_{e2e}^{l.o.f_j}, T_{e2e}^{l.o.f_j}}$		$\bigotimes_{i=0}^1 \beta_{v_i}^{l.o.f_j} = \beta_{4,32}$	$\bigotimes_{i=0}^1 \beta_{v_i}^{l.o.f_j} = \beta_{4,80}$
	D^{f_j}		$\beta_{e2e}^{l.o.f_j} = b^{f_j}$ $4 \cdot [t - 32]^+ = 10$ $t = 34.5$	$\beta_{e2e}^{l.o.f_j} = b^{f_j}$ $4 \cdot [t - 80]^+ = 10$ $t = 82.5$
B^{f_j}		$\alpha^{f_j}(T_{e2e}^{l.o.f_j}) = 2 \cdot 32 + 10$ $= 74$	$\alpha^{f_j}(T_{e2e}^{l.o.f_j}) = 2 \cdot 80 + 10$ $= 170$	

PMOO		ARB_MUX	
$\beta_{e2e} = \beta_{R_{e2e}, T_{e2e}}$		$\bigotimes_{i=0}^1 \beta_{v_i} = \beta_{10,20}$	
crosstraffic $\alpha_{e2e}^{xf_j} = \gamma_{r_{e2e}^{xf_j}, b_{e2e}^{xf_j}}$	$r_{e2e}^{xf_j}$	$\sum_{j=0}^2 r^{f_j} = 6$	
	$b_{e2e}^{xf_j}$	$\sum_{j=0}^3 b^{f_j} = 30$	
$=$		$= \gamma_{6,30}$	
left over service $\beta_{e2e}^{1.o.f_j} = \beta_{R_{e2e}^{1.o.f_j}, T_{e2e}^{1.o.f_j}}$	$R_{e2e}^{1.o.f_j}$	$[R_{e2e} - r_{e2e}^{xf_j}]^+ = 4$	
	$T_{e2e}^{1.o.f_j}$	$\beta_{e2e} = \alpha_{e2e}^{xf_j}$ $10 \cdot [t - 20]^+ = 6 \cdot t + 30$ $t = 57.5$	
$=$		$= \beta_{4,57.5}$	
D^{f_j}		$\beta_{e2e}^{1.o.f_j} = b^{f_j}$ $4 \cdot [t - 57.5]^+ = 10$ $t = 60$	
B^{f_j}		$\alpha^{f_j}(T_{e2e}^{1.o.f_j}) = 2 \cdot 57.5 + 10$ $= 125$	

Tandem_1SC_2Flows_1AC_2Paths.java



- $\beta_{v_0} = \beta_{v_1} = \beta_{R_{v_i}, T_{v_i}} = \beta_{20,20}, i \in \{0,1\}$
- $\alpha^{f_0} = \alpha^{f_1} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}, j \in \{0,1\}$

Flow f_0

TFA		FIFO_MUX	ARB_MUX
v_0	$\alpha_{v_0}^{\text{sum}}$	$= \gamma_{r_{v_0}^{\text{sum}}, b_{v_0}^{\text{sum}}} = \alpha^{f_0}$	
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}^{\text{sum}}$ $20 \cdot [t - 20]^+ = 25$ $t = 21.25$	$\beta_{v_0} = \alpha_{v_0}^{\text{sum}}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $15 \cdot t = 425$ $t = 28\frac{1}{3}$
	$B_{v_1}^{f_0}$	$\alpha_{v_0}^{\text{sum}}(T_{v_0}) = 5 \cdot 20 + 25$ $= 125$	
v_1	$\alpha_{v_1}^{\text{sum}} = (\alpha_{v_0}^{f_0})^* + \alpha^{f_1}$	$r_{\alpha_{v_1}^{\text{sum}}}$	$= 10$
		$b_{\alpha_{v_1}^{\text{sum}}}$	$\alpha_{v_0}^{f_0}(T_{v_0}) + b^{f_1} = 125 + 25 = 150$
		$=$	$= \gamma_{10,150}$
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{\alpha_{v_1}^{\text{sum}}}$ $20 \cdot [t - 20]^+ = 150$ $t = 27.5$	$\beta_{v_1} = \alpha_{v_1}^{\text{sum}}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 150$ $t = 55$
	$B_{v_1}^{f_0}$	$\alpha_{v_1}^{\text{sum}}(T_{v_1}) = 10 \cdot 20 + 150$ $= 350$	
D^{f_0}		$\sum_{i=0}^1 D_{v_i}^{f_0} = 48.75$	$\sum_{i=0}^1 D_{v_i}^{f_0} = 83\frac{1}{3}$
B^{f_0}		$\max_i b_{v_i}^{f_0} = 350$	

PMOO and SFA yield the same result because there is no tandem of servers to be convoluted before subtracting common crossflows.

SFA, PMOO			ARB_MUX
v_0	crosstraffic $\alpha_{v_0}^{xf_0} = \gamma_{r_{v_0}^{xf_0}, b_{v_0}^{xf_0}}$	$r_{v_0}^{xf_0}$	$= 0$
		$b_{v_0}^{xf_0}$	$= 0$
		$=$	$= \gamma_{0,0}$
	left over service $\beta_{v_0}^{l.o.f_0} = \beta_{R_{v_0}^{l.o.f_0}, T_{v_0}^{l.o.f_0}}$	$R_{v_0}^{l.o.f_0}$	$= 20$
		$T_{v_0}^{l.o.f_0}$	$= 20$
		$=$	$= \beta_{20,20}$
	output of crosstraffic to same next node $\alpha_{v_0 v_1}^{xf_0} = \gamma_{r_{v_0 v_1}^{xf_0}, b_{v_0 v_1}^{xf_0}}$	$r_{v_0 v_1}^{xf_0}$	$= 0$
		$b_{v_0 v_1}^{xf_0} = B_{v_0}^{xf_0}$	$= 0$
		$=$	$= \gamma_{0,0}$
v_1	crosstraffic $\alpha_{v_1}^{xf_0} = \gamma_{r_{v_1}^{xf_0}, b_{v_1}^{xf_0}}$	$r_{v_1}^{xf_0}$	$= 5$
		$b_{v_1}^{xf_0}$	$= 25$
		$=$	$= \gamma_{5,25}$
	left over service $\beta_{v_1}^{l.o.f_0} = \beta_{R_{v_1}^{l.o.f_0}, T_{v_1}^{l.o.f_0}}$	$R_{v_1}^{l.o.f_0}$	$[R_{v_1} - r_{v_1}^{xf_0}]^+ = 15$
		$T_{v_1}^{l.o.f_0}$	$\beta_{v_1} = \alpha_{v_1}^{xf_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$
		$=$	$= \beta_{15, 28\frac{1}{3}}$
	output of crosstraffic not needed		
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$			$\bigotimes_{i=0}^1 \beta_{v_i}^{l.o.f_0} = \beta_{15, 48\frac{1}{3}}$
D^{f_0}			$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $15 \cdot [t - 48\frac{1}{3}]^+ = 25$ $t = 50$
B^{f_0}			$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 48\frac{1}{3} + 25$ $= 266\frac{2}{3}$

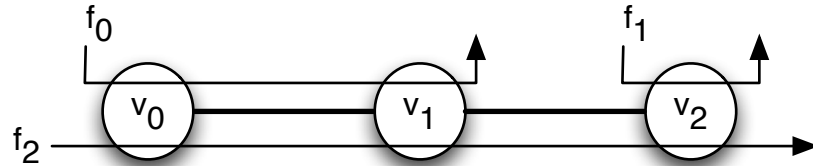
Flow f_1

TFA			FIFO_MUX	ARB_MUX
v ₁	α ^{sum} _{v₁} = (α ^{f₀} _{v₀}) [*] + α ^{f₁} _{v₁}	r α ^{sum} _{v₁}	= 10	
		b α ^{sum} _{v₁}	α ^{f₀} _{v₀} (T _{v₀}) + b ^{f₁} _{v₁} = 125 + 25 = 150	
		=	= γ _{10,150}	
	D ^{f₁} _{v₁}	β _{v₁} = b α ^{sum} _{v₁}	β _{v₁} = α ^{sum} _{v₁}	
		20 · [t − 20] ⁺ = 150	20 · [t − 20] ⁺ = 10 · t + 150	
	B ^{f₁} _{v₁}	t = 27.5	t = 55	
α ^{sum} _{v₁} (T _{v₁}) = 10 · 20 + 150				
= 350				
D ^{f₁}		∑ _{i=0} ¹ D ^{f₁} _{v_i} = 27.5	∑ _{i=0} ¹ D ^{f₁} _{v_i} = 55	
B ^{f₁}		max _i b ^{f₀} _{v_i} = 350		

PMOO and SFA yield the same result because there is no tandem of servers to be convoluted before subtracting common crossflows.

SFA, PMOO			ARB_MUX
v_0	output of crosstraffic	$r_{v_0 v_1}^{x f_1}$	$r_{v_0}^{f_0} = r^{f_0} = 5$
	to same next node	$b_{v_0 v_1}^{x f_1} = B_{v_0}^{x f_1}$	$\alpha_{v_0}^{x f_1}(T_{v_0}) = 5 \cdot 20 + 25$ $= 125$
	$\alpha_{v_0 v_1}^{x f_1} = \gamma_{r_{v_0 v_1}^{x f_1}, b_{v_0 v_1}^{x f_1}}$	$=$	$= \gamma_{5, 125}$
v_1	crosstraffic	$r_{v_1}^{x f_1}$	$= 5$
	$\alpha_{v_1}^{x f_1} = \gamma_{r_{v_1}^{x f_1}, b_{v_1}^{x f_1}}$	$b_{v_1}^{x f_1}$	$= 125$
		$=$	$= \gamma_{5, 125}$
	left over service	$R_{v_1}^{l.o.f_1}$	$[R_{v_1} - r_{v_1}^{x f_1}]^+ = 15$
	$\beta_{v_1}^{l.o.f_1} = \beta_{R_{v_1}^{l.o.f_1}, T_{v_1}^{l.o.f_1}}$	$T_{v_1}^{l.o.f_1}$	$\beta_{v_1} = \alpha_{v_1}^{x f_1}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 125$ $t = 35$
		$=$	$= \beta_{15, 35}$
		output of crosstraffic not needed	
$\beta_{e2e}^{l.o.f_1} = \beta_{R_{e2e}^{l.o.f_1}, T_{e2e}^{l.o.f_1}}$		$\bigotimes_{i=0}^1 \beta_{v_i}^{l.o.f_1} = \beta_{15, 35}$	
D^{f_1}		$\beta_{e2e}^{l.o.f_1} = b^{f_1}$ $15 \cdot [t - 35]^+ = 25$ $t = 36\frac{2}{3}$	
B^{f_1}		$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 35 + 25$ $= 200$	

Tandem_1SC_3Flows_1AC_3Paths.java



- $\beta_{v_0} = \beta_{v_1} = \beta_{v_2} = \beta_{R_{v_i}, T_{v_i}} = \beta_{20,20}, i \in \{0, 1, 2\}$
- $\alpha^{f_0} = \alpha^{f_1} = \alpha^{f_2} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}, j \in \{0, 1, 2\}$

Flow f_0 (comparable to Tandem_1SC_2Flows_1AC_1Path)

TFA		FIFO_MUX	ARB_MUX
v_0	$\alpha_{v_0}^{\text{sum}} = \gamma^{\text{sum}} = \gamma_{r_{v_0}^{\text{sum}}, b_{v_0}^{\text{sum}}}$	$\sum_{j=0}^1 \alpha^{f_j} = \gamma_{10,50}$	
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}^{\text{sum}}$ $20 \cdot [t - 20]^+ = 50$ $t = 22.5$	$\beta_{v_0} = \alpha_{v_0}^{\text{sum}}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 50$ $t = 45$
	$B_{v_1}^{f_0}$	$\alpha_{v_0}^{\text{sum}}(T_{v_0}) = 20 \cdot 10 + 50$ $= 250$	
v_1	$\alpha_{v_1}^{\text{sum}} = (\alpha_{v_0}^{\text{sum}})^*$	$r_{\alpha_{v_1}^{\text{sum}}}$	$= r_{v_0}^{\text{sum}} = 10$
		$b_{\alpha_{v_1}^{\text{sum}}}$	$\alpha_{v_0}^{\text{sum}}(T_{v_0}) = 10 \cdot 20 + 50 = 250$
		$=$	$= \gamma_{10,250}$
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{\alpha_{v_1}^{\text{sum}}}$ $20 \cdot [t - 20]^+ = 250$ $t = 32.5$	$\beta_{v_1} = \alpha_{v_1}^{\text{sum}}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 250$ $t = 65$
	$B_{v_1}^{f_0}$	$\alpha_{v_1}^{\text{sum}}(T_{v_1}) = 10 \cdot 20 + 250$ $= 450$	
D^{f_0}		$\sum_{i=0}^1 D_{v_i}^{f_0} = 55$	$\sum_{i=0}^1 D_{v_i}^{f_0} = 110$
B^{f_0}		$\max_i b_{v_i}^{f_0} = 450$	

SFA			FIFO _MUX		ARB _MUX	
v ₀	crosstraffic $\alpha_{v_0}^{xf_0} = \gamma_{r_{v_0}^{xf_0}, b_{v_0}^{xf_0}}$	$r_{v_0}^{xf_0}$	$r_{v_0}^{f_1} = r^{f_1} = 5$			
		$b_{v_0}^{xf_0}$	$b_{v_0}^{f_1} = b^{f_1} = 25$			
		=	$\gamma_{5,25} = \alpha^{f_1}$			
	left over service $\beta_{v_0}^{l.o.f_0} = \beta_{R_{v_0}^{l.o.f_0}, T_{v_0}^{l.o.f_0}}$	$R_{v_0}^{l.o.f_0}$	$[R_{v_0} - r_{v_0}^{xf_0}]^+ = 5$			
		$T_{v_0}^{l.o.f_0}$	$\beta_{v_0} = b_{v_0}^{xf_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21.25$	$\beta_{v_0} = \alpha_{v_0}^{xf_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$		
		=	$= \beta_{15,21.25}$			$= \beta_{15,28\frac{1}{3}}$
		=	$= \gamma_{5,125}$			
	output of crosstraffic to same next node $\alpha_{v_0 v_1}^{xf_0} = \gamma_{r_{v_0 v_1}^{xf_0}, b_{v_0 v_1}^{xf_0}}$	$r_{v_0 v_1}^{xf_0}$	$r_{v_0}^{f_1} = r^{f_1} = 5$			
		$b_{v_0 v_1}^{xf_0} = B_{v_0}^{xf_0}$	$\alpha_{v_0}^{xf_0}(T_{v_0}) = 5 \cdot 20 + 25$ $= 125$			
		=	$= \gamma_{5,125}$			
v ₁	crosstraffic $\alpha_{v_1}^{xf_0} = \gamma_{r_{v_1}^{xf_0}, b_{v_1}^{xf_0}}$	$r_{v_1}^{xf_0}$	$= 5$			
		$b_{v_1}^{xf_0}$	$= 125$			
		=	$= \gamma_{5,125}$			
	left over service $\beta_{v_1}^{l.o.f_0} = \beta_{R_{v_1}^{l.o.f_0}, T_{v_1}^{l.o.f_0}}$	$R_{v_1}^{l.o.f_0}$	$[R_{v_1} - r_{v_1}^{xf_0}]^+ = 15$			
		$T_{v_1}^{l.o.f_0}$	$\beta_{v_1} = b_{v_1}^{xf_0}$ $20 \cdot [t - 20]^+ = 125$ $t = 26.25$	$\beta_{v_1} = \alpha_{v_1}^{xf_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 125$ $t = 35$		
		=	$= \beta_{15,26.25}$			$= \beta_{15,35}$
		=	$= \gamma_{5,125}$			
	output of crosstraffic not needed					
	$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$		$\bigotimes_{i=0}^1 \beta_{v_i}^{l.o.f_0} = \beta_{15,47.5}$		$\bigotimes_{i=0}^1 \beta_{v_i}^{l.o.f_0} = \beta_{15,63\frac{1}{3}}$	
	D^{f_0}		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $15 \cdot [t - 47.5]^+ = 25$ $t = 49\frac{1}{6}$		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $15 \cdot [t - 63\frac{1}{3}]^+ = 25$ $t = 65$	
B^{f_0}		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 47.5 + 25$ $= 262.5$		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 63\frac{1}{3} + 25$ $= 341\frac{2}{3}$		

PMOO	ARB_MUX
$\beta_{e2e} = \beta_{R_{e2e}, T_{e2e}}$	$\bigotimes_{i=0}^1 \beta_{v_i} = \beta_{20,40}$
crosstraffic	$r_{v_0}^{f_1} = r^{f_1} = 5$
$\alpha_{e2e}^{xf_0} = \gamma_{r_{e2e}^{xf_0}, b_{e2e}^{xf_0}}$	$b_{v_0}^{f_1} = b^{f_1} = 25$
$=$	$= \gamma_{5,25}$
left over service	$[R_{e2e} - r_{e2e}^{xf_0}]^+ = 15$
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$	$\beta_{e2e} = \alpha_{e2e}^{xf_0}$
$T_{e2e}^{l.o.f_0}$	$20 \cdot [t - 40]^+ = 5 \cdot t + 25$
$=$	$t = 55$
	$= \beta_{15,55}$
D^{f_0}	$\beta_{e2e}^{l.o.f_0} = b^{f_0}$
	$15 \cdot [t - 55]^+ = 25$
	$t = 56\frac{2}{3}$
B^{f_0}	$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 55 + 25$
	$= 300$

Flow f_1 (comparable with Node_2Flows_2ACs)

The crossflow's arrival curve is the sum of the result of ComputeOutputBound(v_1, f_2) (see SFA below) and α^{f_1} .

TFA	FIFO_MUX	ARB_MUX
$\alpha^{\text{sum}} = \alpha_{v_1 v_2}^{f_2} + \alpha^{f_1} = \gamma_{r^{\text{sum}}, b^{\text{sum}}}$	$\gamma_{5,264 \frac{1}{16}} + \gamma_{5,25} = \gamma_{10,289 \frac{1}{16}}$	$\gamma_{5,355 \frac{5}{9}} + \gamma_{5,25} = \gamma_{10,380 \frac{5}{9}}$
Df_1	$\beta_{v_0} = b^{\text{sum}}$ $20 \cdot [t - 20]^+ = 289 \frac{1}{16}$ $t = 34 \frac{29}{64}$	$\beta_{v_0} = \alpha^{\text{sum}}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 380 \frac{5}{9}$ $t = 78 \frac{5}{90}$
Bf_1	$\alpha^{\text{sum}}(T_{v_0}) = 10 \cdot 20 + 289 \frac{1}{16}$ $= 489 \frac{1}{16}$	$\alpha^{\text{sum}}(T_{v_0}) = 10 \cdot 20 + 380 \frac{5}{9}$ $= 580 \frac{5}{9}$

Current ComputeOutputBpund(v_1, f_2)-version calculating $\alpha_{v_1 v_2}^{f_2}$ example:

$$\begin{aligned}
 \alpha_{v_1 v_2}^{f_2} &= \alpha_{v_0 v_1}^{f_2} \odot \beta_{v_1}^{1.o.f_2} \otimes \\
 (\text{for ARB_MUX}) &= \alpha_{v_0 v_1}^{f_2} \odot [\beta_{v_1} - \alpha_{v_0 v_1}^{f_0}]^+ \\
 &= \alpha_{v_0 v_1}^{f_2} \odot [\beta_{v_1} - (\alpha^{f_0} \odot \beta_{v_0}^{1.o.f_0})]^+ \\
 &= \alpha_{v_0 v_1}^{f_2} \odot [\beta_{v_1} - (\alpha^{f_0} \odot [\beta_{v_0} - \alpha^{f_2}]^+)]^+
 \end{aligned}$$

SFA		FIFO_MUX	ARB_MUX
$\beta_{v_0}^{l.o.f_0} = \beta_{v_0}^{l.o.f_2} = \beta_{R_{v_0}^{l.o.}, T_{v_0}^{l.o.}}$	$R_{v_0}^{l.o.}$	$= R_{v_0} - r^{f_0} = R_{v_0} - r^{f_2} = 15$	
	$T_{v_0}^{l.o.}$	$\beta_{v_0} = b_{v_0}^{f_{\{0,2\}}}$ $20 \cdot [t - 20]^+ = 25$ $t = 21.25$	$\beta_{v_0} = \alpha_{v_0}^{f_{\{0,2\}}}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$
	$=$	$= \beta_{15,21.25}$	$= \beta_{15,28\frac{1}{3}}$
	$r_{v_0 v_1}$	$= r^{f_0} = 5$	
$\alpha_{v_0 v_1}^{f_{\{0,2\}}} = \alpha^{f_0} \oslash \beta_{v_0}^{l.o.f_0} = \gamma_{r_{v_0 v_1}, b_{v_0 v_1}}$	$b_{v_0 v_1}$	$\alpha^{f_0}(T_{v_0}^{l.o.}) = 131.25$	$\alpha^{f_0}(T_{v_0}^{l.o.}) = 166\frac{2}{3}$
	$=$	$= \gamma_{5,131.25}$	$= \gamma_{5,166\frac{2}{3}}$
$\beta_{v_1}^{l.o.f_2} = [\beta_{v_1} - \alpha_{v_0 v_1}^{f_0}]^+ = \beta_{R_{v_1}^{l.o.f_2}, T_{v_1}^{l.o.f_2}}$	$R_{v_1}^{l.o.f_2}$	$= [R_{v_1} - r^{x f_2}]^+ = [R_{v_1} - r_{v_0 v_1}^{f_0}]^+ = 15$	
	$T_{v_1}^{l.o.f_2}$	$\beta_{v_1} = b_{v_0 v_1}^{f_0}$ $20 \cdot [t - 20]^+ = 131.25$ $t = 26\frac{9}{16}$	$\beta_{v_1} = \alpha_{v_0 v_1}^{f_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 166\frac{2}{3}$ $t = 37\frac{7}{9}$
	$=$	$= \beta_{15,26\frac{9}{16}}$	$= \beta_{15,37\frac{7}{9}}$
	$r_{v_1 v_2}$	$= r_{v_0 v_1}^{f_2} = 5$	
$\alpha_{v_1 v_2}^{f_2} = \alpha_{v_0, v_1}^{f_2} \oslash \beta_{v_1}^{l.o.f_2} = \gamma_{r_{v_1 v_2}, b_{v_1 v_2}}$	$b_{v_1 v_2}$	$\alpha_{v_0, v_1}^{f_2}(T_{v_1}^{l.o.f_2}) = 264\frac{1}{16}$	$\alpha_{v_0, v_1}^{f_2}(T_{v_1}^{l.o.f_2}) = 355\frac{5}{9}$
	$=$	$= \gamma_{5,264\frac{1}{16}}$	$= \gamma_{5,355\frac{5}{9}}$
$\beta_{v_2}^{l.o.f_1} = [\beta_{v_2} - \alpha_{v_1 v_2}^{f_2}]^+ = \beta_{R_{v_2}^{l.o.f_1}, T_{v_2}^{l.o.f_1}}$	$R_{v_2}^{l.o.f_1}$	$= R_{v_2} - r_{v_1 v_2}^{f_2} = 15$	
	$T_{v_2}^{l.o.f_1}$	$\beta_{v_1} = b_{v_1 v_2}^{f_2}$ $20 \cdot [t - 20]^+ = 264\frac{1}{16}$ $t = 33\frac{13}{64}$	$\beta_{v_1} = \alpha_{v_1 v_2}^{f_2}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 355\frac{5}{9}$ $t = 50\frac{10}{27}$
	$=$	$= \beta_{15,33\frac{13}{64}}$	$= \beta_{15,50\frac{10}{27}}$
	$r_{v_2}^{l.o.f_1}$	$= R_{v_2} - r_{v_1 v_2}^{f_2} = 15$	
D^{f_1}	$\beta_{v_2}^{l.o.f_1} = b^{f_1}$	$\beta_{v_2}^{l.o.f_1} = b^{f_1}$ $15 \cdot [t - 33\frac{13}{64}]^+ = 25$ $t = 34\frac{167}{192}$	$\beta_{v_2}^{l.o.f_1} = b^{f_1}$ $15 \cdot [t - 50\frac{10}{27}]^+ = 25$ $t = 52\frac{1}{27}$
	B^{f_1}	$\alpha^{f_1}(T_{v_2}^{l.o.f_1}) = 5 \cdot 33\frac{13}{64} + 25$ $= 191\frac{1}{64}$	$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 50\frac{10}{27} + 25$ $= 276\frac{23}{27}$

A recursive SFA calculation using the SFA left-over service curve to calculate $\alpha_{v_1 v_2}^{f_2}$ (similar approach to PMOO) yields slightly tighter bounds, however, it is not implemented in the DISCO Network Calculator yet.

SFA		FIFO_MUX	ARB_MUX
$\alpha_{v_2}^{x f_1} = \alpha^{f_2} \odot \beta_{e_{2e}}^{l.o.f_0} = \gamma_{r_{v_2}^{x f_1}, b_{v_2}^{x f_1}}$	$\beta_{e_{2e}}^{l.o.f_0}$	$= \beta_{15,47.5}$	$= \beta_{15,63\frac{1}{3}}$
	$r^{x f_1}$	$= r^{f_2} = 5$	
	$b^{x f_1}$	$\alpha^{f_2}(T_{e_{2e}}^{l.o.f_0}) = 5 \cdot 47.5 + 25$ $= 262.5$	$\alpha^{f_2}(T_{e_{2e}}^{l.o.f_0}) = 5 \cdot 63\frac{1}{3} + 25$ $= 341\frac{2}{3}$
	$=$	$= \gamma_{5,262.5}$	$= \gamma_{5,341\frac{2}{3}}$
$\beta_{e_{2e}}^{l.o.f_1} = \beta_{v_2}^{l.o.f_1} = \beta_{R_{v_2}^{l.o.f_1}, T_{v_2}^{l.o.f_1}}$	$R_{v_2}^{l.o.f_1}$	$= [R_{v_0} - r^{x f_1}]^+ = 15$	
	$T_{v_2}^{l.o.f_1}$	$\beta_{v_2} = b^{x f_1}$ $20 \cdot [t - 20]^+ = 262.5$ $t = 33.125$	$\beta_{v_2} = \alpha^{x f_1}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 341\frac{2}{3}$ $t = 49\frac{4}{9}$
	$=$	$= \beta_{15,33.125}$	$= \beta_{15,49\frac{4}{9}}$
D^{f_1}		$\beta_{e_{2e}}^{l.o.f_1} = b^{f_1}$ $15 \cdot [t - 33.125]^+ = 25$ $t = 34\frac{19}{24}$	$\beta_{e_{2e}}^{l.o.f_1} = b^{f_1}$ $15 \cdot [t - 49\frac{4}{9}]^+ = 25$ $t = 51\frac{1}{9}$
B^{f_1}		$\alpha^{f_1}(T_{e_{2e}}^{l.o.f_1}) = 5 \cdot 33\frac{1}{8} + 25$ $= 190\frac{5}{8}$	$\alpha^{f_1}(T_{e_{2e}}^{l.o.f_1}) = 5 \cdot 49\frac{4}{9} + 25$ $= 272\frac{2}{9}$

PMOO		ARB_MUX
$\alpha_{v_2}^{xf_1} = \alpha^{f_2} \oslash \beta_{e_{2e}}^{l.o.f_0} = \gamma_{r_{v_2}^{xf_1}, b_{v_2}^{xf_1}}$	$\beta_{e_{2e}}^{l.o.f_0}$	$= \beta_{15,55}$
	r^{xf_1}	$= f^{f_2} = 5$
	b^{xf_1}	$\alpha^{f_2}(T_{e_{2e}}^{l.o.f_0}) = 5 \cdot 55 + 25$ $= 300$
	$=$	$= \gamma_{5,300}$
$\beta_{e_{2e}}^{l.o.f_1} = \beta_{v_2}^{l.o.f_1} = \beta_{R_{v_2}^{l.o.f_1}, T_{v_2}^{l.o.f_1}}$	$R_{v_2}^{l.o.f_1}$	$= 15$
	$T_{v_2}^{l.o.f_1}$	$\beta_{v_2} = \alpha^{xf_1}$
		$20 \cdot [t - 20]^+ = 5 \cdot t + 300$ $t = 46\frac{2}{3}$
		$= \beta_{15,46\frac{2}{3}}$
D^{f_1}	$\beta_{e_{2e}}^{l.o.f_1} = b^{f_1}$	
	$15 \cdot [t - 46\frac{2}{3}]^+ = 25$ $t = 48\frac{1}{3}$	
B^{f_1}	$\alpha^{f_1}(T_{e_{2e}}^{l.o.f_1}) = 5 \cdot 46\frac{2}{3} + 25$	
	$= 258\frac{1}{3}$	

Flow f_2

TFA bounds for flow f_2 can be calculated from the results for f_0 and f_2 .

TFA	FIFO_MUX	ARB_MUX
$D^{f_2} = D^{f_0} + D^{f_1}$	$55 + 34\frac{29}{64} = 89\frac{29}{64}$	$110 + 78\frac{5}{90} = 188\frac{5}{90}$
$B^{f_2} = \max\{B^{f_0}, B^{f_1}\}$	$\max\{450, 489\frac{1}{16}\} = 489\frac{1}{16}$	$\max\{450, 508\frac{5}{9}\} = 508\frac{5}{9}$

Although SFA does not recursively calculate the necessary output bounds, it yields the right result if there's no cross traffic coming from outside the flow of interest's path.

SFA		FIFO_MUX	ARB_MUX
$\beta_{v_2}^{l.o.f_2} = [\beta_{v_0} - \alpha^{f_1}]^+ = \beta_{R_{v_2}^{l.o.f_2}, T_{v_2}^{l.o.f_2}}$	$R_{v_2}^{l.o.f_2}$	$= R_{v_2} - r^{f_1} = 15$	
	$T_{v_2}^{l.o.f_2}$	$\beta_{v_2} = b_{v_2}^{f_1}$ $20 \cdot [t - 20]^+ = 25$ $t = 21.25$	$\beta_{v_2} = \alpha_{v_2}^{f_1}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$
	$=$	$= \beta_{15, 21.25}$	$= \beta_{15, 28\frac{1}{3}}$
	$\beta_{e2e}^{l.o.f_2} = \beta_{e2e}^{l.o.f_0} \otimes \beta_{v_2}^{l.o.f_1}$	$= \beta_{15, 47\frac{1}{2}} \otimes \beta_{15, 21\frac{1}{4}} = \beta_{15, 68\frac{3}{4}}$	$= \beta_{15, 63\frac{1}{3}} \otimes \beta_{15, 28\frac{1}{3}} = \beta_{15, 91\frac{2}{3}}$
D^{f_2}		$\beta_{e2e}^{l.o.f_2} = b^{f_2}$ $15 \cdot [t - 68\frac{3}{4}]^+ = 25$ $t = 70\frac{5}{12}$	$\beta_{e2e}^{l.o.f_2} = b^{f_2}$ $15 \cdot [t - 91\frac{2}{3}]^+ = 25$ $t = 93\frac{1}{3}$
B^{f_2}		$\alpha^{f_2}(T_{v_2}^{l.o.f_2}) = 5 \cdot 68\frac{3}{4} + 25$ $= 368\frac{3}{4}$	$\alpha^{f_2}(T_{e2e}^{l.o.f_2}) = 5 \cdot 91\frac{2}{3} + 25$ $= 483\frac{1}{3}$

$$\beta_{e2e}^{l.o.f_2} = \beta_{e2e}^{l.o.f_0} \otimes \beta_{v_2}^{l.o.f_1} = \beta_{e2e}^{l.o.f_0} \otimes [\beta_{v_2} - \alpha^{f_1}]^+$$

PMOO	ARB_MUX
$\beta_{e2e}^{l.o.f_2} = \beta_{v_2}^{l.o.f_1} = \beta_{15,28\frac{1}{3}}$	
$\beta_{e2e}^{l.o.f_2} = \beta_{e2e}^{l.o.f_0} \otimes \beta_{v_2}^{l.o.f_1}$	$= \beta_{15,55} \otimes \beta_{15,28\frac{1}{3}} = \beta_{15,83\frac{1}{3}}$
D^{f_2}	$\beta_{e2e}^{l.o.f_2} = b^{f_1}$ $15 \cdot [t - 83\frac{1}{3}] = 25$ $t = 85$
B^{f_2}	$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 83\frac{1}{3} + 25$ $= 441\frac{2}{3}$