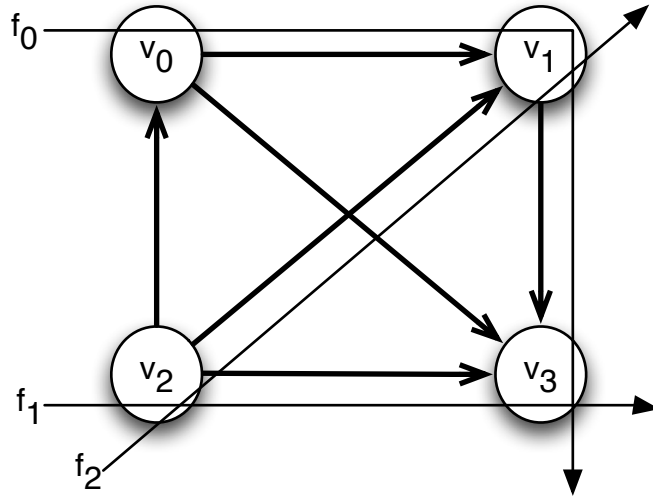
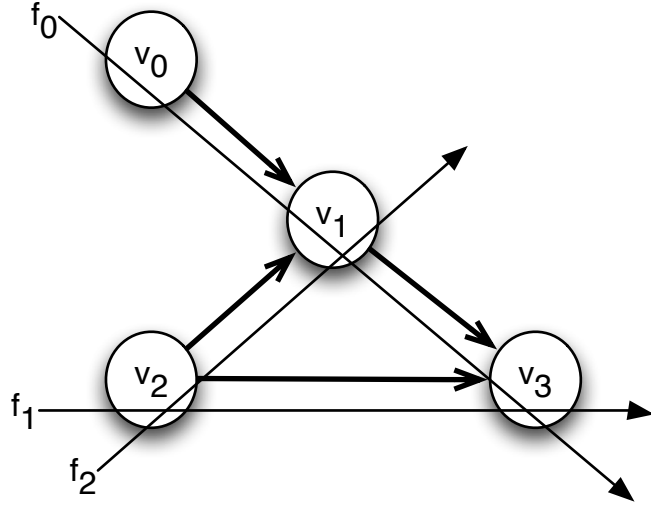


# FeedForward\_1SC\_3Flows\_1AC\_3Paths



- $\beta_{v_0} = \beta_{v_1} = \beta_{v_2} = \beta_{v_3} = \beta_{R_{v_i}, T_{v_i}} = \beta_{20,20}, i \in \{0, 1, 3\}$
- $\alpha^{f_0} = \alpha^{f_1} = \alpha^{f_2} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}, j \in \{0, 1, 2\}$

The above topology can be transformed into an equivalent one by removing the unused edges:



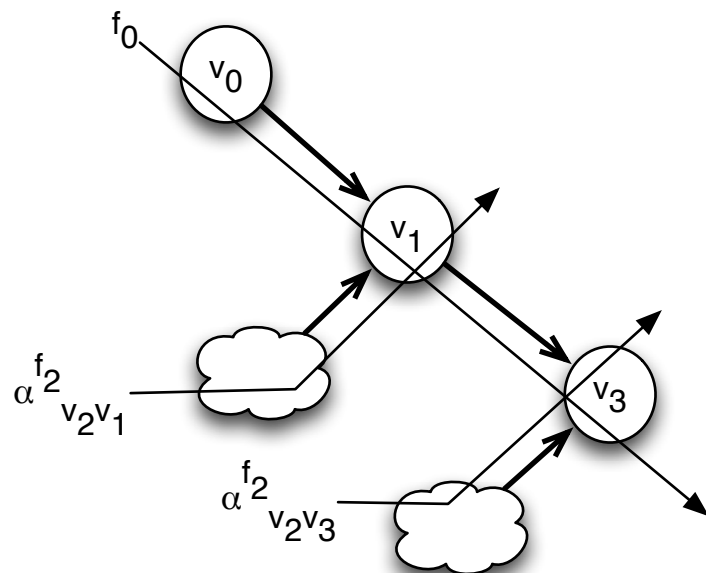
computeOutputBound( $v_2, f_i$ ) = $(\alpha_{v_2}^{f_i})^*, i \in \{1, 2\}$		FIFO_MUX	ARB_MUX
$\alpha_{v_2}^{xf_i} = \alpha_{v_2}^{xf_1} = \alpha_{v_2}^{xf_2} = \alpha^{f_1} = \alpha^{f_2}$		$= \gamma_{5,25}$	
$\beta_{v_2}^{l.o.f_i} = [\beta_{v_2} - \alpha_{v_2}^{xf_i}]^+ = \beta_{R_{v_2}^{l.o.f_i}, T_{v_2}^{l.o.f_i}}$	$R_{v_2}^{l.o.f_i}$	$[R_{v_2} - r_{v_2}^{xf_i}]^+ = 15$	
	$T_{v_2}^{l.o.f_i}$	$\beta_{v_2} = b_{v_2}^{xf_i}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$	$\beta_{v_2} = \alpha_{v_2}^{xf_i}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$
	$=$	$= \beta_{15, 21\frac{1}{4}}$	$= \beta_{15, 28\frac{1}{3}}$
	$(r_{v_2}^{f_i})^*$	$= 5$	
$(\alpha_{v_2}^{f_i})^* = \alpha^{f_i} \oslash \beta_{v_2}^{l.o.f_i} = \gamma_{(r_{v_2}^{f_i})^*, (b_{v_2}^{f_i})^*}$	$(b_{v_2}^{f_i})^*$	$\alpha^{f_i}(T_{v_2}^{l.o.f_i}) = 5 \cdot 21\frac{1}{4} + 25 = 131\frac{1}{4}$	$\alpha^{f_i}(T_{v_2}^{l.o.f_i}) = 5 \cdot 28\frac{1}{3} + 25 = 166\frac{2}{3}$
	$=$	$= \gamma_{5, 131\frac{1}{4}}$	$= \gamma_{5, 166\frac{2}{3}}$

$\text{computeOutputBound}(v_0, f_0) = (\alpha_{v_0}^{f_0})^* = \alpha_{v_0 v_1}^{f_0}$		FIFO_MUX	ARB_MUX
$\alpha_{v_0}^{x f_0}$		$= \gamma_{0,0}$	
$\beta_{v_0}^{\text{l.o.}, f_0} = [\beta_{v_0} - \alpha_{v_0}^{x f_0}]^+ = \beta_{v_0}$		$= \beta_{20,20}$	
$(\alpha_{v_0}^{f_0})^* = \alpha_{v_0 v_1}^{f_0} = \alpha^{f_0} \odot \beta_{v_0} = \gamma_{r_{v_0 v_1}^{f_0}, b_{v_0 v_1}^{f_0}}$	$r_{v_0 v_1}^{f_0}$	$= 5$	
	$b_{v_0 v_1}^{f_0}$	$\alpha^{f_0}(T_{v_0}) = 5 \cdot 20 + 25 = 125$	
	$=$	$= \gamma_{5,125}$	

$\text{computeOutputBound}(v_1, f_0) = (\alpha_{v_1}^{f_0})^* = \alpha_{v_1 v_3}^{f_0}$		FIFO_MUX	ARB_MUX
$\alpha_{v_1}^{x f_0} = \alpha_{v_2 v_1}^{f_2} = (\alpha_{v_2}^{f_2})^*$		$= \gamma_{5,131\frac{1}{4}}$	$= \gamma_{5,166\frac{2}{3}}$
$\beta_{v_1}^{\text{l.o.}, f_0} = [\beta_{v_1} - \alpha_{v_1}^{x f_0}]^+ = \beta_{R_{v_1}^{\text{l.o.}, f_0}, T_{v_1}^{\text{l.o.}, f_0}}$	$R_{v_1}^{\text{l.o.}, f_0}$	$[R_{v_1} - r_{v_1}^{x f_0}]^+ = 15$	
	$T_{v_1}^{\text{l.o.}, f_0}$	$\beta_{v_1} = b_{v_1}^{x f_0}$ $20 \cdot [t - 20]^+ = 131\frac{1}{4}$ $t = 26\frac{9}{16}$	$\beta_{v_1} = \alpha_{v_1}^{x f_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 166\frac{2}{3}$ $t = 37\frac{7}{8}$
	$=$	$= \beta_{15,26\frac{9}{16}}$	$= \beta_{15,37\frac{7}{8}}$
	$=$	$= \beta_{15,26\frac{9}{16}}$	$= \beta_{15,37\frac{7}{8}}$
$(\alpha_{v_1}^{f_0})^* = (\alpha_{v_0}^{f_0})^* \odot \beta_{v_1}^{\text{l.o.}, f_0} = \gamma_{r_{v_1 v_3}^{f_0}, b_{v_1 v_3}^{f_0}}$	$r_{v_1 v_3}^{f_0}$	$= 5$	
	$b_{v_1 v_3}^{f_0}$	$(\alpha_{v_0}^{f_0})^*(T_{v_1}^{\text{l.o.}, f_0}) = 5 \cdot 26\frac{9}{16} + 125 = 257\frac{13}{16}$	$(\alpha_{v_0 v_1}^{f_0})^*(T_{v_1}^{\text{l.o.}, f_0}) = 5 \cdot 37\frac{7}{8} + 125 = 313\frac{8}{9}$
	$=$	$= \gamma_{5,257\frac{13}{16}}$	$= \gamma_{5,313\frac{8}{9}}$

Flow  $f_0$  (comparable to Tandem\_1SC\_2Flows\_1SC\_2Paths)

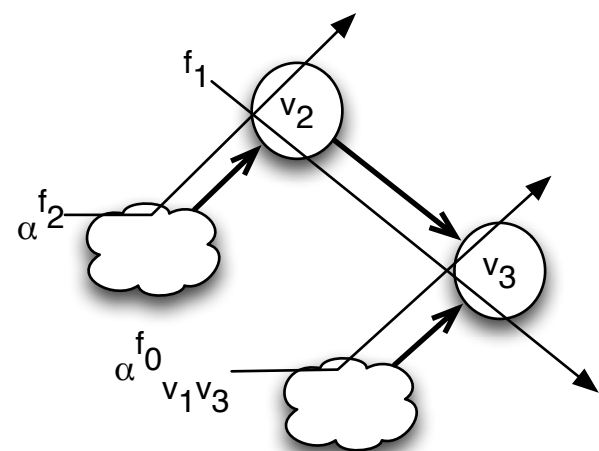
Output bound abstraction of  $f_0$ 's cross flows leads to a tree topology comparable to Tandem\_1SC\_2Flows\_1SC\_2Paths:



TFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0} = \alpha_{v_0}^{f_0}$	$= \gamma_{5,25}$	
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$	FIFO per micro flow $\beta_{v_0} = b_{v_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$
	$B_{v_0}^{f_0}$	$\alpha_{v_0}(T_{v_0}) = 20 \cdot 5 + 25$ $= 125$	
$v_1$	$\alpha_{v_1} = (\alpha_{v_0}^{f_0})^* + (\alpha_{v_2}^{f_2})^*$	$= \gamma_{5,125} + \gamma_{5,131\frac{1}{4}} = \gamma_{10,256\frac{1}{4}}$	$= \gamma_{5,125} + \gamma_{5,166\frac{2}{3}} = \gamma_{10,291\frac{2}{3}}$
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{v_1}$ $20 \cdot [t - 20]^+ = 256\frac{1}{4}$ $t = 32\frac{13}{16}$	$\beta_{v_1} = \alpha_{v_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 291\frac{2}{3}$ $t = 69\frac{1}{6}$
	$B_{v_1}^{f_0}$	$\alpha_{v_1}(T_{v_1}) = 10 \cdot 20 + 256\frac{1}{4}$ $= 456\frac{1}{4}$	$\alpha_{v_1}(T_{v_1}) = 10 \cdot 20 + 291\frac{2}{3}$ $= 491\frac{2}{3}$
$v_3$	$\alpha_{v_3} = (\alpha_{v_1}^{f_0})^* + (\alpha_{v_2}^{f_1})^*$	$= \gamma_{5,257\frac{13}{16}} + \gamma_{5,131\frac{1}{4}} = \gamma_{10,389\frac{1}{16}}$	$= \gamma_{5,313\frac{8}{9}} + \gamma_{5,166\frac{2}{3}} = \gamma_{10,480\frac{5}{9}}$
	$D_{v_3}^{f_0}$	$\beta_{v_3} = b_{v_3}$ $20 \cdot [t - 20]^+ = 389\frac{1}{16}$ $t = 39\frac{29}{64}$	$\beta_{v_3} = \alpha_{v_3}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 480\frac{5}{9}$ $t = 88\frac{5}{90}$
	$B_{v_3}^{f_0}$	$\alpha_{v_3}(T_{v_3}) = 10 \cdot 20 + 389\frac{1}{16}$ $= 589\frac{1}{16}$	$\alpha_{v_3}(T_{v_3}) = 10 \cdot 20 + 480\frac{5}{9}$ $= 680\frac{5}{9}$
$D^{f_0}$		$\sum_{i=\{0,1,3\}} D_{v_i}^{f_0} = 93\frac{33}{64}$	$\sum_{i=\{0,1,3\}} D_{v_i}^{f_0} = 178\frac{17}{36}$
$B^{f_0}$		$\max_{i=\{0,1,3\}} b_{v_i}^{f_0} = 589\frac{1}{16}$	$\max_{i=\{0,1,3\}} b_{v_i}^{f_0} = 680\frac{5}{9}$

SFA, PMOO		FIFO_MUX (SFA only)	ARB_MUX
$v_0$	$\alpha_{v_0}^{xf_0} = \gamma_{r_{v_0}^{xf_0}, b_{v_0}^{xf_0}}$	$= \gamma_{0,0}$	
	$\beta_{v_0}^{l.o.f_0} = [\beta_{v_0} - \alpha_{v_0}^{xf_0}]^+$	$= \beta_{20,20}$	
$v_1$	$\alpha_{v_1}^{xf_0} = (\alpha_{v_2}^{f_1})^*$	$= \gamma_{5,131\frac{1}{4}}$	$= \gamma_{5,166\frac{2}{3}}$
	$\beta_{v_1}^{l.o.f_0} = [\beta_{v_1} - \alpha_{v_1}^{xf_0}]^+$	$= \beta_{15,26\frac{9}{16}}$	$= \beta_{15,37\frac{7}{9}}$
$v_3$	$\alpha_{v_3}^{xf_0} = (\alpha_{v_2}^{f_2})^*$		$= \gamma_{5,131\frac{1}{4}}$
	$\beta_{v_3}^{l.o.f_0} = [\beta_{v_3} - \alpha_{v_3}^{xf_0}]^+ = \beta_{R_{v_3}^{l.o.f_0}, T_{v_3}^{l.o.f_0}}$		$= \gamma_{5,166\frac{2}{3}}$
	$R_{v_3}^{l.o.f_0}$	$[R_{v_3} - r_{v_3}^{xf_0}]^+ = 15$	
	$T_{v_3}^{l.o.f_0}$	$\beta_{v_3} = b_{v_3}^{xf_0}$ $20 \cdot [t - 20]^+ = 131\frac{1}{4}$ $t = 26\frac{9}{16}$	$\beta_{v_3} = \alpha_{v_3}^{xf_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 166\frac{2}{3}$ $t = 37\frac{7}{9}$
	$=$	$= \beta_{15,26\frac{9}{16}}$	$= \beta_{15,37\frac{7}{9}}$
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$		$\bigotimes_{i=\{0,1,3\}} \beta_{v_i}^{l.o.f_0} = \beta_{15,73\frac{1}{8}}$	$\bigotimes_{i=\{0,1,3\}} \beta_{v_i}^{l.o.f_0} = \beta_{15,95\frac{5}{9}}$
$D^{f_0}$		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $15 \cdot [t - 73\frac{1}{8}]^+ = 25$ $t = 74\frac{19}{24}$	$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $15 \cdot [t - 95\frac{5}{9}]^+ = 25$ $t = 97\frac{2}{9}$
$B^{f_0}$		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 73\frac{1}{8} + 25$ $= 390\frac{5}{8}$	$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 95\frac{5}{9} + 25$ $= 502\frac{7}{9}$

Flow  $f_1$

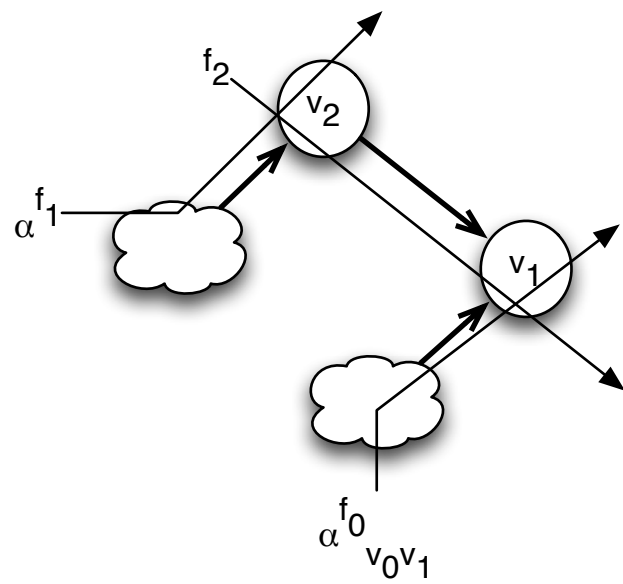


TFA		FIFO_MUX	ARB_MUX
$v_2$	$\alpha_{v_2} = \alpha^{f_1} + \alpha^{f_2}$	$= \gamma_{10,50}$	
	$D_{v_2}^{f_1}$	$\beta_{v_2} = b_{v_2}$ $20 \cdot [t - 20]^+ = 50$ $t = 22\frac{1}{2}$	$\beta_{v_2} = \alpha_{v_2}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 50$ $t = 45$
	$B_{v_2}^{f_1}$	$\alpha_{v_2}(T_{v_2}) = 20 \cdot 10 + 50$ $= 250$	
$v_3$	$\alpha_{v_3} = (\alpha_{v_1}^{f_0})^* + (\alpha_{v_2}^{f_1})^*$	$= \gamma_{5,257\frac{13}{16}} + \gamma_{5,131\frac{1}{4}} = \gamma_{10,389\frac{1}{16}}$	
	$D_{v_3}^{f_1}$	$\beta_{v_3} = b_{v_3}$ $20 \cdot [t - 20]^+ = 389\frac{1}{16}$ $t = 39\frac{29}{64}$	$\beta_{v_3} = \alpha_{v_3}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 480\frac{5}{9}$ $t = 88\frac{5}{90}$
	$B_{v_3}^{f_1}$	$\alpha_{v_3}(T_{v_3}) = 10 \cdot 20 + 389\frac{1}{16}$ $= 589\frac{1}{16}$	
$D^{f_1}$		$\sum_{i=2}^3 D_{v_i}^{f_1} = 61\frac{61}{64}$	$\sum_{i=2}^3 D_{v_i}^{f_1} = 185\frac{5}{9}$
$B^{f_1}$		$\max_{i=\{2,3\}} b_{v_i}^{f_1} = 589\frac{1}{16}$	$\max_{i=\{2,3\}} b_{v_i}^{f_1} = 680\frac{5}{9}$



SFA, PMOO			FIFO_MUX (SFA only)	ARB_MUX	
$v_2$	$\alpha_{v_2}^{xf_1} = \alpha_{v_2}^{f_2} = \alpha^{f_2}$		$= \gamma_{5,25}$		
	$\beta_{v_2}^{l.o.f_1} = [\beta_{v_2} - \alpha_{v_2}^{xf_1}]^+$		$= \beta_{15,21\frac{1}{4}}$	$= \beta_{15,28\frac{1}{3}}$	
$v_3$	$\alpha_{v_3}^{xf_1} = \alpha_{v_3}^{f_0} = \alpha_{v_1v_3}^{f_0}$		$= \gamma_{5,257\frac{13}{16}}$	$= \gamma_{5,313\frac{8}{9}}$	
	$\beta_{v_3}^{l.o.f_1} = [\beta_{v_3} - \alpha_{v_3}^{xf_1}]^+ = \beta_{R_{v_3}^{l.o.f_1}, T_{v_3}^{l.o.f_1}}$	$R_{v_3}^{l.o.f_1}$	$[R_{v_3} - r_{v_3}^{xf_1}]^+ = 15$		
		$T_{v_3}^{l.o.f_1}$	$\beta_{v_3} = b_{v_3}^{xf_1}$	$\beta_{v_3} = \alpha_{v_3}^{xf_1}$	
			$20 \cdot [t - 20]^+ = 257\frac{13}{16}$	$20 \cdot [t - 20]^+ = 5 \cdot t + 313\frac{8}{9}$	
			$t = 32\frac{57}{64}$	$t = 47\frac{16}{27}$	
	$=$	$= \beta_{15,32\frac{57}{64}}$	$= \beta_{15,47\frac{16}{27}}$		
$\beta_{e2e}^{l.o.f_1} = \beta_{R_{e2e}^{l.o.f_1}, T_{e2e}^{l.o.f_1}}$			$\bigotimes_{i=2}^3 \beta_{v_i}^{l.o.f_1} = \beta_{15,54\frac{9}{64}}$	$\bigotimes_{i=2}^3 \beta_{v_i}^{l.o.f_1} = \beta_{15,75\frac{25}{27}}$	
$D^{f_1}$			$\beta_{e2e}^{l.o.f_1} = b^{f_1}$	$\beta_{e2e}^{l.o.f_1} = b^{f_1}$	
			$15 \cdot [t - 54\frac{9}{64}]^+ = 25$	$15 \cdot [t - 75\frac{25}{27}]^+ = 25$	
			$t = 55\frac{155}{192}$	$t = 77\frac{16}{27}$	
$B^{f_1}$			$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 54\frac{9}{64} + 25$	$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 75\frac{25}{27} + 25$	
			$= 295\frac{45}{64}$	$= 404\frac{17}{27}$	

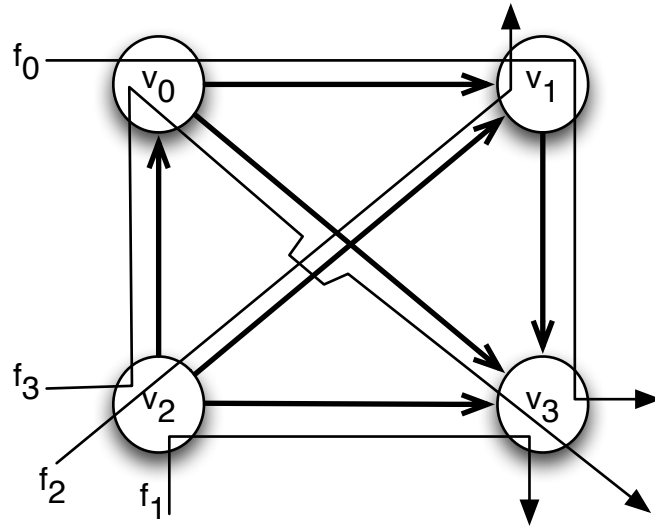
Flow  $f_2$



TFA		FIFO_MUX	ARB_MUX
$v_2$	$\alpha_{v_2} = \alpha^{f_1} + \alpha^{f_2}$	$= \gamma_{10,50}$	
	$D_{v_2}^{f_2}$	$\beta_{v_2} = b_{v_2}$ $20 \cdot [t - 20]^+ = 50$ $t = 22\frac{1}{2}$	$\beta_{v_2} = \alpha_{v_2}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 50$ $t = 45$
	$B_{v_2}^{f_2}$	$\alpha_{v_2}(T_{v_2}) = 20 \cdot 10 + 50$ $= 250$	
$v_1$	$\alpha_{v_3} = (\alpha_{v_0}^{f_0})^* + (\alpha_{v_2}^{f_1})^*$	$= \gamma_{5,125} + \gamma_{5,131\frac{1}{4}} = \gamma_{10,256\frac{1}{4}}$	$= \gamma_{5,125} + \gamma_{5,166\frac{2}{3}} = \gamma_{10,291\frac{2}{3}}$
	$D_{v_1}^{f_2}$	$\beta_{v_1} = b_{v_1}$ $20 \cdot [t - 20]^+ = 256\frac{1}{4}$ $t = 32\frac{13}{16}$	$\beta_{v_1} = \alpha_{v_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 291\frac{2}{3}$ $t = 69\frac{1}{6}$
	$B_{v_1}^{f_2}$	$\alpha_{v_1}(T_{v_1}) = 10 \cdot 20 + 256\frac{1}{4}$ $= 456\frac{1}{4}$	$\alpha_{v_1}(T_{v_1}) = 10 \cdot 20 + 291\frac{2}{3}$ $= 491\frac{2}{3}$
$D^{f_2}$		$\sum_{i=1}^2 D_{v_i}^{f_2} = 55\frac{5}{16}$	$\sum_{i=1}^2 D_{v_i}^{f_2} = 114\frac{1}{6}$
$B^{f_2}$		$\max_{i=\{1,2\}} b_{v_i}^{f_2} = 456\frac{1}{4}$	$\max_{i=\{1,2\}} b_{v_i}^{f_2} = 491\frac{2}{3}$

SFA, PMOO		FIFO_MUX (SFA only)	ARB_MUX
$v_2$	$\alpha_{v_2}^{xf_2} = \alpha_{v_2}^{f_1} = \alpha^{f_1}$	$= \gamma_{5,25}$	
	$\beta_{v_2}^{l.o.f_2} = [\beta_{v_2} - \alpha_{v_2}^{xf_1}]^+$	$= \beta_{15,21\frac{1}{4}}$	$= \beta_{15,28\frac{1}{3}}$
$v_1$	$\alpha_{v_1}^{xf_1} = (\alpha_{v_0}^{f_0})^*$		$= \gamma_{5,125}$
	$\beta_{v_1}^{l.o.f_2} = [\beta_{v_1} - \alpha_{v_1}^{xf_2}]^+ = \beta_{R_{v_1}^{l.o.f_2}, T_{v_1}^{l.o.f_2}}$	$R_{v_1}^{l.o.f_2}$	$[R_{v_1} - r_{v_1}^{xf_2}]^+ = 15$
		$\beta_{v_1} = b_{v_1}$	$\beta_{v_1} = \alpha_{v_1}^{xf_2}$
		$20 \cdot [t - 20]^+ = 125$	$20 \cdot [t - 20]^+ = 5 \cdot t + 125$
		$t = 26\frac{1}{4}$	$t = 35$
	$=$		$= \beta_{15,26\frac{1}{4}}$
$\beta_{e2e}^{l.o.f_2} = \beta_{R_{e2e}^{l.o.f_2}, T_{e2e}^{l.o.f_2}}$		$\bigotimes_{i=1}^2 \beta_{v_i}^{l.o.f_2} = \beta_{15,47\frac{1}{2}}$	$\bigotimes_{i=1}^2 \beta_{v_i}^{l.o.f_2} = \beta_{15,63\frac{1}{3}}$
$D^{f_2}$		$\beta_{e2e}^{l.o.f_2} = b^{f_2}$	$\beta_{e2e}^{l.o.f_2} = b^{f_2}$
		$15 \cdot [t - 47\frac{1}{2}]^+ = 25$	$15 \cdot [t - 63\frac{1}{3}]^+ = 25$
		$t = 49\frac{1}{6}$	$t = 65$
$B^{f_2}$		$\alpha^{f_2}(T_{e2e}^{l.o.f_2}) = 5 \cdot 47\frac{1}{2} + 25$	$\alpha^{f_1}(T_{e2e}^{l.o.f_2}) = 5 \cdot 63\frac{1}{3} + 25$
		$= 262\frac{1}{2}$	$= 341\frac{2}{3}$

# FeedForward\_1SC\_4Flows\_1AC\_4Paths

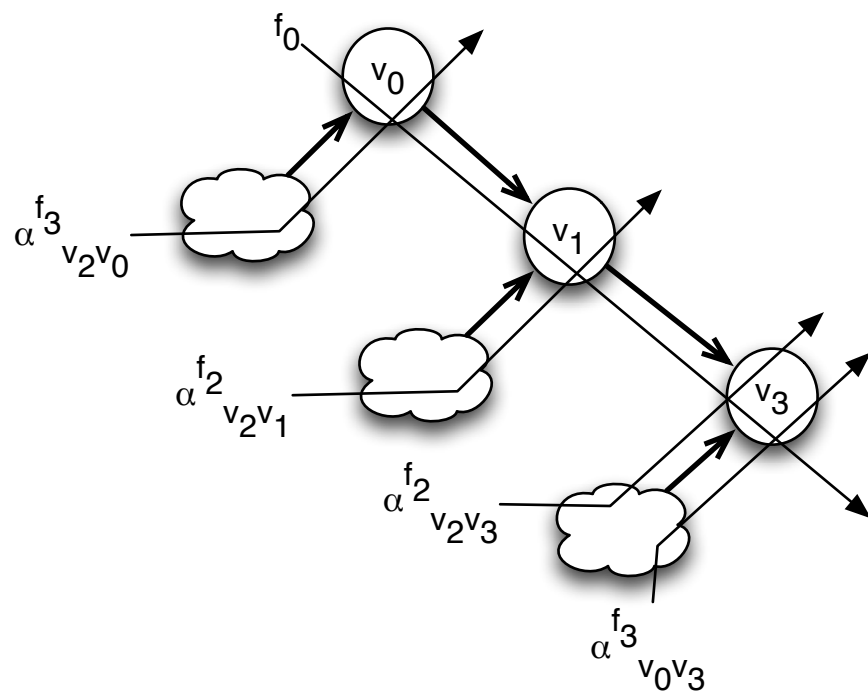


- $\beta_{v_0} = \beta_{v_1} = \beta_{v_2} = \beta_{v_3} = \beta_{R_{v_i}, T_{v_i}} = \beta_{20,20}, i \in \{0,1,3\}$
- $\alpha^{f_i} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}, j \in \{0,3\}$

computeOutputBound( $v_2, f_i$ ) = $(\alpha_{v_2}^{f_i})^*, i \in \{1, 2, 3\}$		FIFO_MUX	ARB_MUX
$\alpha_{v_2}^{x f_i} = \alpha_{v_2}^{x f_1} = \alpha_{v_2}^{x f_2} = \alpha_{v_2}^{x f_3}$		$= \gamma_{10,50}$	
$\beta_{v_2}^{l.o.f_i} = [\beta_{v_2} - \alpha_{v_2}^{x f_i}]^+ = \beta_{R_{v_2}^{l.o.f_i}, T_{v_2}^{l.o.f_i}}$	$R_{v_2}^{l.o.f_i}$	$[R_{v_2} - r_{v_2}^{x f_i}]^+ = 15$	
	$T_{v_2}^{l.o.f_i}$	$\beta_{v_2} = b_{v_2}^{x f_i}$ $20 \cdot [t - 20]^+ = 50$ $t = 22\frac{1}{2}$	$\beta_{v_2} = \alpha_{v_2}^{x f_i}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 50$ $t = 45$
	$=$	$= \beta_{10,22\frac{1}{2}}$	$= \beta_{10,45}$
	$(r_{v_2}^{f_i})^*$	$= 5$	
$(\alpha_{v_2}^{f_i})^* = \alpha^{f_i} \odot \beta_{v_2}^{l.o.f_i} = \gamma_{(r_{v_2}^{f_i})^*, (b_{v_2}^{f_i})^*}$	$(b_{v_2}^{f_i})^*$	$\alpha^{f_i}(T_{v_2}^{l.o.f_i}) = 5 \cdot 22\frac{1}{2} + 25 = 137\frac{1}{2}$	$\alpha^{f_i}(T_{v_2}^{l.o.f_i}) = 5 \cdot 45 + 25 = 250$
	$=$	$= \gamma_{5,137\frac{1}{2}}$	$= \gamma_{5,250}$
computeOutputBound( $v_0, f_0$ ) = $(\alpha_{v_0}^{f_0})^* = \alpha_{v_0 v_1}^{f_0}$		FIFO_MUX	ARB_MUX
$\alpha_{v_0}^{x f_0} = \alpha_{v_2 v_0}^{f_3} = (\alpha_{v_2}^{f_3})^*$		$= \gamma_{5,137\frac{1}{2}}$	$= \gamma_{5,250}$
$\beta_{v_0}^{l.o.f_0} = [\beta_{v_0} - \alpha_{v_0}^{x f_0}]^+ = \beta_{R_{v_0}^{l.o.f_0}, T_{v_0}^{l.o.f_0}}$	$R_{v_0}^{l.o.f_0}$	$[R_{v_0} - r_{v_0}^{x f_0}]^+ = 15$	
	$T_{v_0}^{l.o.f_0}$	$\beta_{v_0} = b_{v_0}^{x f_0}$ $20 \cdot [t - 20]^+ = 137\frac{1}{2}$ $t = 26\frac{7}{8}$	$\beta_{v_0} = \alpha_{v_0}^{x f_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 250$ $t = 43\frac{1}{3}$
	$=$	$= \beta_{15,26\frac{7}{8}}$	$= \beta_{15,43\frac{1}{3}}$
	$r_{v_0 v_1}^{f_0}$	$= 5$	
$(\alpha_{v_0}^{f_0})^* = \alpha_{v_0 v_1}^{f_0} = \alpha^{f_0} \odot \beta_{v_0}^{l.o.f_0} = \gamma_{r_{v_0 v_1}^{f_0}, b_{v_0 v_1}^{f_0}}$	$b_{v_0 v_1}^{f_0}$	$\alpha^{f_0}(T_{v_0}^{l.o.f_0}) = 5 \cdot 26\frac{7}{8} + 25 = 159\frac{3}{8}$	$\alpha^{f_0}(T_{v_0}^{l.o.f_0}) = 5 \cdot 43\frac{1}{3} + 25 = 241\frac{2}{3}$
	$=$	$= \gamma_{5,159\frac{3}{8}}$	$= \gamma_{5,241\frac{2}{3}}$

computeOutputBound( $v_0, f_3$ ) = $(\alpha_{v_0}^{f_3})^* = \alpha_{v_0 v_3}^{f_3}$		FIFO_MUX	ARB_MUX
$\alpha_{v_0}^{x f_3} = \alpha^{f_0}$		$= \gamma_{5,25}$	
$\beta_{v_0}^{l.o.f_3} = [\beta_{v_0} - \alpha_{v_0}^{x f_3}]^+ = [\beta_{v_0} - \alpha^{f_0}]^+ = \beta_{R_{v_0}^{l.o.f_3}, T_{v_0}^{l.o.f_3}}$	$R_{v_0}^{l.o.f_3}$	$[R_{v_0} - r_{v_0}^{x f_3}]^+ = 15$	
	$T_{v_0}^{l.o.f_3}$	$\beta_{v_0} = b_{v_0}^{f_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$	$\beta_{v_0} = \alpha^{f_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$
	$=$	$= \beta_{15, 21\frac{1}{4}}$	$= \beta_{15, 28\frac{1}{3}}$
	$r_{v_0 v_3}^{f_3}$	$= 5$	
$(\alpha_{v_0}^{f_3})^* = (\alpha_{v_2}^{f_3})^* \odot \beta_{v_0}^{l.o.f_3} = \gamma_{r_{v_0 v_3}^{f_3}, b_{v_0 v_3}^{f_3}}$	$b_{v_0 v_3}^{f_3}$	$(\alpha_{v_2}^{f_3})^*(T_{v_0}^{l.o.f_3}) = 5 \cdot 21\frac{1}{4} + 137\frac{1}{2} = 243\frac{3}{4}$	$(\alpha_{v_2}^{f_3})^*(T_{v_0}^{l.o.f_3}) = 5 \cdot 28\frac{1}{3} + 250 = 391\frac{2}{3}$
	$=$	$= \gamma_{5, 243\frac{3}{4}}$	$= \gamma_{5, 391\frac{2}{3}}$
computeOutputBound( $v_1, f_0$ ) = $(\alpha_{v_1}^{f_0})^* = \alpha_{v_1 v_3}^{f_0}$		FIFO_MUX	ARB_MUX
$\alpha_{v_1}^{x f_0} = \alpha_{v_2 v_1}^{f_2} = (\alpha_{v_2}^{f_2})^*$		$= \gamma_{5, 137\frac{1}{2}}$	$= \gamma_{5, 250}$
$\beta_{v_1}^{l.o.f_0} = [\beta_{v_1} - \alpha_{v_1}^{x f_0}]^+ = \beta_{R_{v_1}^{l.o.f_0}, T_{v_1}^{l.o.f_0}}$	$R_{v_1}^{l.o.f_0}$	$[R_{v_1} - r_{v_1}^{x f_0}]^+ = 15$	
	$T_{v_1}^{l.o.f_0}$	$\beta_{v_1} = b_{v_1}^{x f_0}$ $20 \cdot [t - 20]^+ = 137\frac{1}{2}$ $t = 26\frac{7}{8}$	$\beta_{v_1} = \alpha_{v_1}^{x f_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 250$ $t = 43\frac{1}{3}$
	$=$	$= \beta_{15, 26\frac{7}{8}}$	$= \beta_{15, 43\frac{1}{3}}$
	$r_{v_1 v_3}^{f_0}$	$= 5$	
$(\alpha_{v_1}^{f_0})^* = (\alpha_{v_0}^{f_0})^* \odot \beta_{v_1}^{l.o.f_0} = \gamma_{r_{v_1 v_3}^{f_0}, b_{v_1 v_3}^{f_0}}$	$b_{v_1 v_3}^{f_0}$	$(\alpha_{v_0}^{f_0})^*(T_{v_1}^{l.o.f_0}) = 5 \cdot 26\frac{7}{8} + 159\frac{3}{8} = 293\frac{3}{4}$	$(\alpha_{v_0}^{f_0})^*(T_{v_1}^{l.o.f_0}) = 5 \cdot 43\frac{1}{3} + 241\frac{2}{3} =$
	$=$	$= \gamma_{5, 293\frac{3}{4}}$	$= \gamma_{5, 458\frac{1}{3}}$

Flow  $f_0$





TFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0} = \alpha^{f_0} + \alpha_{v_2 v_0}^{f_3} = \alpha^{f_0} + (\alpha_{v_2}^{f_3})^*$	$= \gamma_{5,25} + \gamma_{5,137\frac{1}{2}} = \gamma_{10,162\frac{1}{2}}$	$= \gamma_{5,25} + \gamma_{5,250} = \gamma_{10,275}$
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}$ $20 \cdot [t - 20]^+ = 162\frac{1}{2}$ $t = 28\frac{1}{8}$	$\beta_{v_0} = \alpha_{v_0}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 275$ $t = 67\frac{1}{2}$
	$B_{v_0}^{f_0}$	$\alpha_{v_0}(T_{v_0}) = 10 \cdot 20 + 162\frac{1}{2}$ $= 262\frac{1}{2}$	$\alpha_{v_0}(T_{v_0}) = 10 \cdot 20 + 275$ $= 475$
$v_1$	$\alpha_{v_1} = \alpha_{v_0 v_1}^{f_0} + \alpha_{v_2 v_1}^{f_2} = (\alpha_{v_0}^{f_0})^* + (\alpha_{v_2}^{f_1})^*$	$= \gamma_{5,159\frac{3}{8}} + \gamma_{5,137\frac{1}{2}} = \gamma_{10,296\frac{7}{8}}$	$= \gamma_{5,241\frac{2}{3}} + \gamma_{5,250} = \gamma_{10,491\frac{2}{3}}$
	$D_{v_1}^{f_0}$	$\beta_{v_1} = b_{v_1}$ $20 \cdot [t - 20]^+ = 296\frac{7}{8}$ $t = 34\frac{27}{32}$	$\beta_{v_1} = \alpha_{v_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 491\frac{2}{3}$ $t = 89\frac{1}{6}$
	$B_{v_1}^{f_0}$	$\alpha_{v_1}(T_{v_1}) = 10 \cdot 20 + 296\frac{7}{8}$ $= 496\frac{7}{8}$	$\alpha_{v_1}(T_{v_1}) = 10 \cdot 20 + 491\frac{2}{3}$ $= 691\frac{2}{3}$
$v_3$	$\alpha_{v_3} = (\alpha_{v_1}^{f_0})^* + (\alpha_{v_2}^{f_1})^* + (\alpha_{v_0}^{f_3})^*$	$= \gamma_{5,293\frac{3}{4}} + \gamma_{5,137\frac{1}{2}} + \gamma_{5,243\frac{3}{4}} = \gamma_{15,675}$	$= \gamma_{5,458\frac{1}{3}} + \gamma_{5,250} + \gamma_{5,391\frac{2}{3}} = \gamma_{15,1100}$
	$D_{v_3}^{f_0}$	$\beta_{v_3} = b_{v_3}$ $20 \cdot [t - 20]^+ = 675$ $t = 53\frac{3}{4}$	$\beta_{v_3} = \alpha_{v_3}$ $20 \cdot [t - 20]^+ = 15 \cdot t + 1100$ $t = 300$
	$B_{v_3}^{f_0}$	$\alpha_{v_3}(T_{v_3}) = 15 \cdot 20 + 675$ $= 975$	$\alpha_{v_3}(T_{v_3}) = 15 \cdot 20 + 1100$ $= 1400$
$D^{f_0}$		$D_{v_0}^{f_0} + D_{v_1}^{f_0} + D_{v_3}^{f_0} = 116\frac{23}{32}$	$D_{v_0}^{f_0} + D_{v_1}^{f_0} + D_{v_3}^{f_0} = 456\frac{2}{3}$
$B^{f_0}$		$\max\{B_{v_0}^{f_0}, B_{v_1}^{f_0}, B_{v_3}^{f_0}\} = 975$	$\max\{B_{v_0}^{f_0}, B_{v_1}^{f_0}, B_{v_3}^{f_0}\} = 1400$

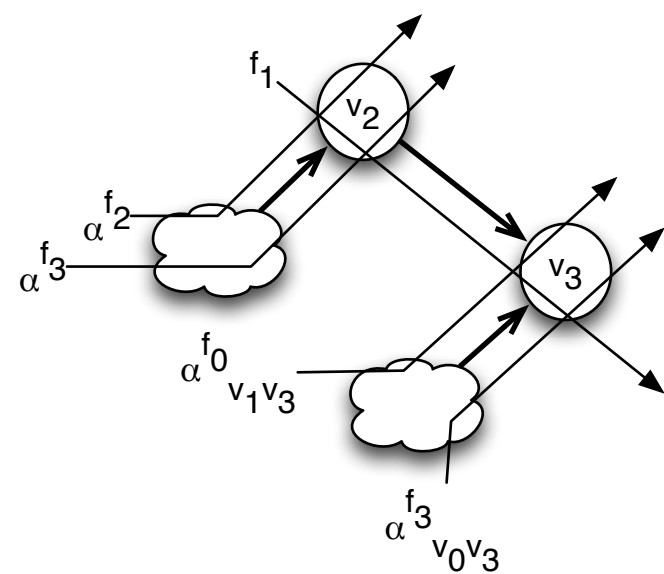
SFA		FIFO_MUX	ARB_MUX
$v_0$	$\alpha_{v_0}^{xf_0} = (\alpha_{v_2}^{f_3})^*$	$= \gamma_{5,137\frac{1}{2}}$	$= \gamma_{5,250}$
	$\beta_{v_0}^{l.o.f_0} = [\beta_{v_0} - \alpha_{v_0}^{xf_3}]^+$	$= \beta_{15,26\frac{7}{8}}$	$= \beta_{15,43\frac{1}{3}}$
$v_1$	$\alpha_{v_1}^{xf_0} = (\alpha_{v_2}^{f_1})^*$	$= \gamma_{5,137\frac{1}{2}}$	$= \gamma_{5,250}$
	$\beta_{v_1}^{l.o.f_0} = [\beta_{v_1} - \alpha_{v_1}^{xf_0}]^+$	$= \beta_{15,26\frac{7}{8}}$	$= \beta_{15,43\frac{1}{3}}$
$v_3$	$\alpha_{v_3}^{xf_0} = (\alpha_{v_2}^{f_2})^* + (\alpha_{v_0}^{f_3})^*$		$= \gamma_{5,137\frac{1}{2}} + \gamma_{5,243\frac{3}{4}} = \gamma_{10,381\frac{1}{4}}$
	$\beta_{v_3}^{l.o.f_0} = [\beta_{v_3} - \alpha_{v_3}^{xf_0}]^+ = \beta_{R_{v_3}^{l.o.f_0}, T_{v_3}^{l.o.f_0}}$	$R_{v_3}^{l.o.f_0}$	$[R_{v_3} - r_{v_3}^{xf_0}]^+ = 10$
		$T_{v_3}^{l.o.f_0}$	$\beta_{v_3} = b_{v_3}^{xf_0}$ $20 \cdot [t - 20]^+ = 381\frac{1}{4}$ $t = 39\frac{1}{16}$
		$\beta_{v_3} = \alpha_{v_3}^{xf_0}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 641\frac{2}{3}$ $t = 104\frac{1}{6}$	
		$=$	$= \beta_{10,39\frac{1}{16}}$
$\beta_{e2e}^{l.o.f_0} = \beta_{R_{e2e}^{l.o.f_0}, T_{e2e}^{l.o.f_0}}$		$\bigotimes_{i=\{0,1,3\}} \beta_{v_i}^{l.o.f_0} = \beta_{10,92\frac{13}{16}}$	$\bigotimes_{i=\{0,1,3\}} \beta_{v_i}^{l.o.f_0} = \beta_{10,190\frac{5}{6}}$
$D^{f_0}$		$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $10 \cdot [t - 92\frac{13}{16}]^+ = 25$ $t = 95\frac{5}{16}$	$\beta_{e2e}^{l.o.f_0} = b^{f_0}$ $10 \cdot [t - 190\frac{5}{6}]^+ = 25$ $t = 193\frac{1}{3}$
$B^{f_0}$		$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 92\frac{13}{16} + 25$ $= 489\frac{1}{16}$	$\alpha^{f_0}(T_{e2e}^{l.o.f_0}) = 5 \cdot 190\frac{5}{6} + 25$ $= 979\frac{1}{6}$

PMOO yields a bounds different to / worse than SFA ARB\_MUX, however, results should be equal as there are no interference free tandems of servers whose service curves could be folded before subtracting the arrival.

Setting PMOO's max recursion depth to 0, i.e., forcing to use computeOutputBound and thus the results shown above for everything outside the flow of interest's path, even improves the bounds.

Needs to be investigated, there must be caused by bugs.

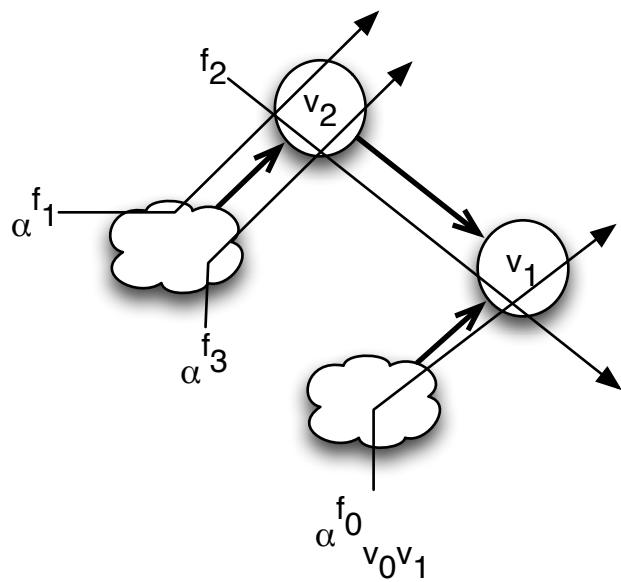
Flow  $f_1$



TFA		FIFO_MUX	ARB_MUX
$v_2$	$\alpha_{v_1} = \alpha^{f_1} + \alpha^{f_2} + \alpha^{f_3}$	$= 3 \cdot \gamma_{5,25} = \gamma_{15,75}$	
	$D_{v_2}^{f_1}$	$\beta_{v_2} = b_{v_2}$ $20 \cdot [t - 20]^+ = 75$ $t = 23\frac{3}{4}$	$\beta_{v_2} = \alpha_{v_2}$ $20 \cdot [t - 20]^+ = 15 \cdot t + 75$ $t = 95$
	$B_{v_2}^{f_1}$	$\alpha_{v_2}(T_{v_2}) = 15 \cdot 20 + 75$ $= 375$	
$v_3$	$\alpha_{v_3} = (\alpha_{v_2}^{f_1})^* + (\alpha_{v_1}^{f_0})^* + (\alpha_{v_0}^{f_3})^*$	$= \gamma_{5,137\frac{1}{2}} + \gamma_{5,293\frac{3}{4}} + \gamma_{5,243\frac{3}{4}} = \gamma_{15,675}$	$= \gamma_{5,250} + \gamma_{5,458\frac{1}{3}} + \gamma_{5,391\frac{2}{3}} = \gamma_{15,1100}$
	$D_{v_3}^{f_1}$	$\beta_{v_3} = b_{v_3}$ $20 \cdot [t - 20]^+ = 675$ $t = 53\frac{3}{4}$	$\beta_{v_3} = \alpha_{v_3}$ $20 \cdot [t - 20]^+ = 15 \cdot t + 1100$ $t = 300$
	$B_{v_3}^{f_1}$	$\alpha_{v_3}(T_{v_3}) = 15 \cdot 20 + 675$ $= 975$	$\alpha_{v_3}(T_{v_3}) = 15 \cdot 20 + 1100$ $= 1400$
$D^{f_1}$		$D_{v_2}^{f_1} + D_{v_3}^{f_1} = 77\frac{1}{2}$	$D_{v_2}^{f_1} + D_{v_3}^{f_1} = 395$
$B^{f_1}$		$\max\{B_{v_2}^{f_1}, B_{v_3}^{f_1}\} = 975$	$\max\{B_{v_2}^{f_1}, B_{v_3}^{f_1}\} = 1400$

SFA			FIFO_MUX	ARB_MUX
$v_2$	$\alpha_{v_2}^{xf_1} = \alpha^{f_2} + \alpha^{f_3}$		$= 2 \cdot \gamma_{2,25} = \gamma_{10,50}$	
	$\beta_{v_2}^{l.o.f_1} = [\beta_{v_2} - \alpha_{v_2}^{xf_1}]^+$		$= \beta_{10,22\frac{1}{2}}$	$= \beta_{10,45}$
$v_3$	$\alpha_{v_3}^{xf_1} = (\alpha_{v_1}^{f_0})^* + (\alpha_{v_0}^{f_3})^*$		$= \gamma_{5,293\frac{3}{4}} + \gamma_{5,243\frac{3}{4}} = \gamma_{10,537\frac{1}{2}}$	$= \gamma_{5,458\frac{1}{3}} + \gamma_{5,391\frac{2}{3}} = \gamma_{10,850}$
	$\beta_{v_3}^{l.o.f_1} = [\beta_{v_3} - \alpha_{v_3}^{xf_1}]^+ = \beta_{R_{v_3}^{l.o.f_1}, T_{v_3}^{l.o.f_1}}$	$R_{v_3}^{l.o.f_1}$	$[R_{v_3} - r_{v_3}^{xf_1}]^+ = 10$	
		$T_{v_3}^{l.o.f_1}$	$\beta_{v_3} = b_{v_3}^{xf_1}$ $20 \cdot [t - 20]^+ = 537\frac{1}{2}$ $t = 46\frac{7}{8}$	$\beta_{v_3} = \alpha_{v_3}^{xf_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 850$ $t = 125$
		$=$	$= \beta_{10,46\frac{7}{8}}$	$= \beta_{10,125}$
$\beta_{e2e}^{l.o.f_1} = \beta_{R_{e2e}^{l.o.f_1}, T_{e2e}^{l.o.f_1}}$		$\bigotimes_{i=2}^3 \beta_{v_i}^{l.o.f_1} = \beta_{10,69\frac{3}{8}}$	$\bigotimes_{i=2}^3 \beta_{v_i}^{l.o.f_1} = \beta_{10,170}$	
$D^{f_1}$		$\beta_{e2e}^{l.o.f_1} = b^{f_1}$ $10 \cdot [t - 69\frac{3}{8}]^+ = 25$ $t = 71\frac{7}{8}$	$\beta_{e2e}^{l.o.f_1} = b^{f_1}$ $10 \cdot [t - 170]^+ = 25$ $t = 172\frac{1}{2}$	
$B^{f_1}$		$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 69\frac{3}{8} + 25$ $= 371\frac{7}{8}$	$\alpha^{f_1}(T_{e2e}^{l.o.f_1}) = 5 \cdot 170 + 25$ $= 875$	

PMOO yields a bounds different to / worse than SFA ARB\_MUX. needs to be investigated.



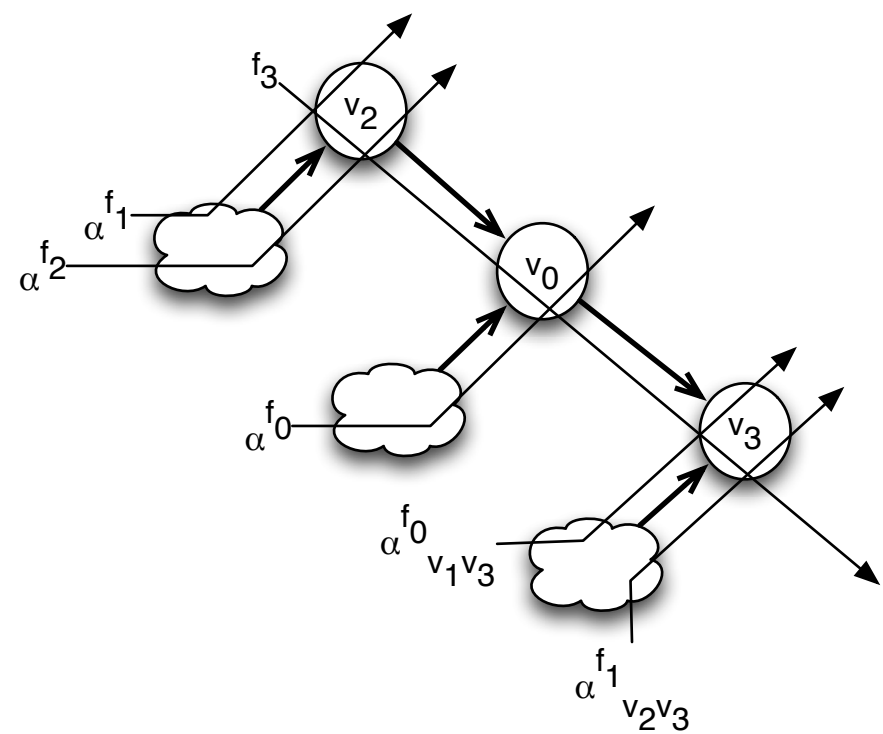


TFA		FIFO_MUX	ARB_MUX
$v_2$	$\alpha_{v_1} = \alpha^{f_2} + \alpha^{f_1} + \alpha^{f_3}$	$= 3 \cdot \gamma_{5,25} = \gamma_{15,75}$	
	$D_{v_2}^{f_2}$	$\beta_{v_2} = b_{v_2}$ $20 \cdot [t - 20]^+ = 75$ $t = 23\frac{3}{4}$	$\beta_{v_2} = \alpha_{v_2}$ $20 \cdot [t - 20]^+ = 15 \cdot t + 75$ $t = 95$
	$B_{v_2}^{f_2}$	$\alpha_{v_2}(T_{v_2}) = 15 \cdot 20 + 75$ $= 375$	
$v_1$	$\alpha_{v_1} = (\alpha_{v_2}^{f_2})^* + (\alpha_{v_0}^{f_0})^*$	$= \gamma_{5,137\frac{1}{2}} + \gamma_{5,159\frac{3}{8}} = \gamma_{10,296\frac{7}{8}}$	$= \gamma_{5,250} + \gamma_{5,241\frac{2}{3}} = \gamma_{10,491\frac{2}{3}}$
	$D_{v_1}^{f_2}$	$\beta_{v_1} = b_{v_1}$ $20 \cdot [t - 20]^+ = 296\frac{7}{8}$ $t = 34\frac{27}{32}$	$\beta_{v_1} = \alpha_{v_1}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 491\frac{2}{3}$ $t = 89\frac{1}{6}$
	$B_{v_1}^{f_2}$	$\alpha_{v_1}(T_{v_1}) = 10 \cdot 20 + 296\frac{7}{8}$ $= 496\frac{7}{8}$	$\alpha_{v_1}(T_{v_1}) = 10 \cdot 20 + 491\frac{2}{3}$ $= 691\frac{2}{3}$
$D^{f_2}$		$D_{v_2}^{f_2} + D_{v_1}^{f_2} = 58\frac{19}{32}$	$D_{v_2}^{f_2} + D_{v_1}^{f_2} = 184\frac{1}{6}$
$B^{f_2}$		$\max\{B_{v_2}^{f_2}, B_{v_1}^{f_2}\} = 496\frac{7}{8}$	$\max\{B_{v_2}^{f_2}, B_{v_1}^{f_2}\} = 691\frac{2}{3}$

SFA		FIFO_MUX	ARB_MUX
$v_2$	$\alpha_{v_2}^{xf_2} = \alpha^{f_1} + \alpha^{f_3}$	$= 2 \cdot \gamma_{2,25} = \gamma_{10,50}$	
	$\beta_{v_2}^{l.o.f_2} = [\beta_{v_2} - \alpha_{v_2}^{xf_2}]^+$	$= \beta_{10,22\frac{1}{2}}$	$= \beta_{10,45}$
$v_1$	$\alpha_{v_1}^{xf_2} = (\alpha_{v_0}^{f_0})^*$	$= \gamma_{5,159\frac{3}{8}}$	$= \gamma_{5,241\frac{2}{3}}$
	$\beta_{v_1}^{l.o.f_2} = [\beta_{v_1} - \alpha_{v_1}^{xf_2}]^+ = \beta_{R_{v_1}^{l.o.f_2}, T_{v_1}^{l.o.f_2}}$	$R_{v_1}^{l.o.f_2}$	$[R_{v_2} - r_{v_2}^{xf_2}]^+ = 15$
		$\beta_{v_1} = b_{v_1}^{xf_2}$	$\beta_{v_1} = \alpha_{v_1}^{xf_2}$
		$20 \cdot [t - 20]^+ = 159\frac{3}{8}$ $t = 27\frac{31}{32}$	$20 \cdot [t - 20]^+ = 5 \cdot t + 241\frac{2}{3}$ $t = 42\frac{7}{9}$
	$=$	$= \beta_{10,27\frac{31}{32}}$	$= \beta_{10,42\frac{7}{9}}$
$\beta_{e2e}^{l.o.f_2} = \beta_{R_{e2e}^{l.o.f_2}, T_{e2e}^{l.o.f_2}}$		$\bigotimes_{i=1}^2 \beta_{v_i}^{l.o.f_2} = \beta_{10,50\frac{15}{32}}$	$\bigotimes_{i=1}^2 \beta_{v_i}^{l.o.f_2} = \beta_{10,87\frac{7}{9}}$
$D^{f_2}$		$\beta_{e2e}^{l.o.f_2} = b^{f_2}$ $10 \cdot [t - 50\frac{15}{32}]^+ = 25$ $t = 52\frac{31}{32}$	$\beta_{e2e}^{l.o.f_2} = b^{f_2}$ $10 \cdot [t - 87\frac{7}{9}]^+ = 25$ $t = 90\frac{5}{18}$
$B^{f_2}$		$\alpha^{f_2}(T_{e2e}^{l.o.f_2}) = 5 \cdot 50\frac{15}{32} + 25$ $= 277\frac{11}{32}$	$\alpha^{f_2}(T_{e2e}^{l.o.f_2}) = 5 \cdot 87\frac{7}{9} + 25$ $= 463\frac{8}{9}$

PMOO yields a bounds different to / worse than SFA ARB\_MUX. needs to be investigated.

Flow  $f_3$

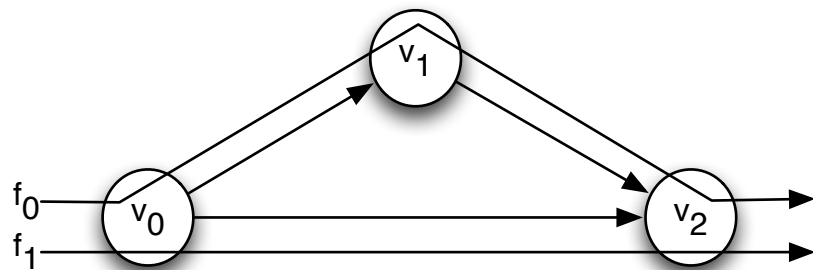


TFA		FIFO_MUX	ARB_MUX
$v_2$	$\alpha_{v_2} = \alpha^{f_3} + \alpha^{f_1} + \alpha^{f_2}$	$= 3 \cdot \gamma_{5,25} = \gamma_{15,75}$	
	$D_{v_2}^{f_3}$	$\beta_{v_2} = b_{v_2}$ $20 \cdot [t - 20]^+ = 75$ $t = 23\frac{3}{4}$	$\beta_{v_2} = \alpha_{v_2}$ $20 \cdot [t - 20]^+ = 15 \cdot t + 75$ $t = 95$
	$B_{v_2}^{f_3}$	$\alpha_{v_2}(T_{v_2}) = 15 \cdot 20 + 75$ $= 375$	
$v_0$	$\alpha_{v_0} = \alpha^{f_0} + \alpha_{v_2 v_0}^{f_3} = \alpha^{f_0} + (\alpha_{v_2}^{f_3})^*$	$= \gamma_{5,25} + \gamma_{5,137\frac{1}{2}} = \gamma_{10,162\frac{1}{2}}$	$= \gamma_{5,25} + \gamma_{5,250} = \gamma_{10,275}$
	$D_{v_0}^{f_3}$	$\beta_{v_0} = b_{v_0}$ $20 \cdot [t - 20]^+ = 162\frac{1}{2}$ $t = 28\frac{1}{8}$	$\beta_{v_0} = \alpha_{v_0}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 275$ $t = 67\frac{1}{2}$
	$B_{v_0}^{f_3}$	$\alpha_{v_0}(T_{v_0}) = 10 \cdot 20 + 162\frac{1}{2}$ $= 262\frac{1}{2}$	$\alpha_{v_0}(T_{v_0}) = 10 \cdot 20 + 275$ $= 475$
$v_3$	$\alpha_{v_3} = (\alpha_{v_1}^{f_0})^* + (\alpha_{v_2}^{f_1})^* + (\alpha_{v_0}^{f_3})^*$	$= \gamma_{5,293\frac{3}{4}} + \gamma_{5,137\frac{1}{2}} + \gamma_{5,243\frac{3}{4}} = \gamma_{15,675}$	$= \gamma_{5,458\frac{1}{3}} + \gamma_{5,250} + \gamma_{5,391\frac{2}{3}} = \gamma_{15,1100}$
	$D_{v_3}^{f_3}$	$\beta_{v_3} = b_{v_3}$ $20 \cdot [t - 20]^+ = 675$ $t = 53\frac{3}{4}$	$\beta_{v_3} = \alpha_{v_3}$ $20 \cdot [t - 20]^+ = 15 \cdot t + 1100$ $t = 300$
	$B_{v_3}^{f_3}$	$\alpha_{v_3}(T_{v_3}) = 15 \cdot 20 + 675$ $= 975$	$\alpha_{v_3}(T_{v_3}) = 15 \cdot 20 + 1100$ $= 1400$
$D^{f_3}$		$D_{v_2}^{f_3} + D_{v_0}^{f_3} + D_{v_3}^{f_3} = 105\frac{5}{8}$	$D_{v_2}^{f_3} + D_{v_0}^{f_3} + D_{v_3}^{f_3} = 462\frac{1}{2}$
$B^{f_3}$		$\max\{B_{v_2}^{f_3}, B_{v_0}^{f_3}, B_{v_3}^{f_3}\} = 975$	$\max\{B_{v_2}^{f_3}, B_{v_0}^{f_3}, B_{v_3}^{f_3}\} = 1400$

SFA			FIFO_MUX	ARB_MUX
$v_2$	$\alpha_{v_2}^{xf_3} = \alpha^{f_1} + \alpha^{f_2}$		$= 2 \cdot \gamma_{2,25} = \gamma_{10,50}$	
	$\beta_{v_2}^{l.o.f_3} = [\beta_{v_2} - \alpha_{v_2}^{xf_3}]^+$		$= \beta_{10,22\frac{1}{2}}$	$= \beta_{10,45}$
$v_0$	$\alpha_{v_0}^{xf_3} = \alpha^{f_0}$		$= \gamma_{5,25}$	
	$\beta_{v_0}^{l.o.f_3} = [\beta_{v_0} - \alpha_{v_0}^{xf_3}]^+$		$= \beta_{15,21\frac{1}{4}}$	$= \beta_{15,28\frac{1}{3}}$
$v_3$	$\alpha_{v_3}^{xf_3} = (\alpha_{v_1}^{f_0})^* + (\alpha_{v_2}^{f_1})^*$		$= \gamma_{5,293\frac{3}{4}} + \gamma_{5,137\frac{1}{2}} = \gamma_{10,431\frac{1}{4}}$	$= \gamma_{5,458\frac{1}{3}} + \gamma_{5,250} = \gamma_{10,708\frac{1}{3}}$
	$\beta_{v_3}^{l.o.f_3} = [\beta_{v_3} - \alpha_{v_3}^{xf_3}]^+ = \beta_{R_{v_3}^{l.o.f_3}, T_{v_3}^{l.o.f_3}}$	$R_{v_3}^{l.o.f_3}$	$[R_{v_3} - r_{v_3}^{xf_3}]^+ = 10$	
		$T_{v_3}^{l.o.f_3}$	$\beta_{v_3} = b_{v_3}^{xf_3}$	$\beta_{v_3} = \alpha_{v_3}^{xf_3}$
			$20 \cdot [t - 20]^+ = 431\frac{1}{4}$	$20 \cdot [t - 20]^+ = 10 \cdot t + 708\frac{1}{3}$
			$t = 41\frac{9}{16}$	$t = 110\frac{5}{6}$
	$=$	$= \beta_{10,41\frac{9}{16}}$	$= \beta_{10,110\frac{5}{6}}$	
$\beta_{e2e}^{l.o.f_3} = \beta_{R_{e2e}^{l.o.f_3}, T_{e2e}^{l.o.f_3}}$			$\bigotimes_{i=\{2,0,3\}} \beta_{v_i}^{l.o.f_3} = \beta_{10,85\frac{5}{16}}$	$\bigotimes_{i=\{2,0,3\}} \beta_{v_i}^{l.o.f_3} = \beta_{10,184\frac{1}{6}}$
$D^{f_3}$			$\beta_{e2e}^{l.o.f_3} = b^{f_3}$	$\beta_{e2e}^{l.o.f_3} = b^{f_3}$
			$10 \cdot [t - 85\frac{5}{16}]^+ = 25$	$10 \cdot [t - 184\frac{1}{6}]^+ = 25$
			$t = 87\frac{13}{16}$	$t = 186\frac{2}{3}$
$B^{f_3}$			$\alpha^{f_3}(T_{e2e}^{l.o.f_3}) = 5 \cdot 85\frac{5}{16} + 25$	$\alpha^{f_3}(T_{e2e}^{l.o.f_3}) = 5 \cdot 184\frac{1}{6} + 25$
			$= 451\frac{9}{16}$	$= 945\frac{5}{6}$

PMOO yields a bounds different to / worse than SFA ARB\_MUX. needs to be investigated.

# FeedForward\_1SC\_2Flows\_1AC\_2Paths



- $\beta_{v_0} = \beta_{v_1} = \beta_{v_2} = \beta_{R_{v_i}, T_{v_i}} = \beta_{20,20}, i \in \{0, 1, 3\}$
- $\alpha^{f_0} = \alpha^{f_1} = \gamma_{r^{f_j}, b^{f_j}} = \gamma_{5,25}, j \in \{0, 1, 2\}$



$\text{computeOutputBound}(v_0, f_0) = (\alpha_{v_0}^{f_0})^* = \alpha_{v_0 v_2}^{f_0}$		FIFO_MUX	ARB_MUX
$\alpha_{v_0}^{x f_0} = \alpha^{f_1}$		$= \gamma_{5,25}$	
$\beta_{v_0}^{l.o.f_0} = [\beta_{v_0} - \alpha_{v_0}^{x f_0}]^+$	$R_{v_0}^{l.o.f_0}$	$= 15$	
	$T_{v_0}^{l.o.f_0}$	$\beta_{v_0} = b_{v_0}^{x f_0}$ $20 \cdot [t - 20]^+ = 25$ $t = 21\frac{1}{4}$	$\beta_{v_0} = \alpha_{v_0}^{x f_0}$ $20 \cdot [t - 20]^+ = 5 \cdot t + 25$ $t = 28\frac{1}{3}$
	$=$	$= \beta_{15,21\frac{1}{4}}$	$= \beta_{15,28\frac{1}{3}}$
	$=$	$= 5$	$= 5$
$\alpha_{v_0 v_2}^{f_0} = \alpha^{f_0} \oslash \beta_{v_0}^{l.o.f_0}$	$r_{v_0 v_2}^{f_0}$	$\alpha^{f_0}(T_{v_0}^{l.o.f_0}) = 131\frac{1}{4}$	$\alpha^{f_0}(T_{v_0}^{l.o.f_0}) = 166\frac{2}{3}$
	$b_{v_0 v_2}^{f_0}$	$= \gamma_{5,131\frac{1}{4}}$	$= \gamma_{5,166\frac{2}{3}}$
	$=$	$= \gamma_{5,131\frac{1}{4}}$	$= \gamma_{5,166\frac{2}{3}}$
$\text{computeOutputBound}(v_0, f_1) = (\alpha_{v_0}^{f_1})^* = \alpha_{v_0 v_1}^{f_1}$		FIFO_MUX	ARB_MUX
$= \text{computeOutputBound}(v_0, f_0) = (\alpha_{v_0}^{f_0})^* = \alpha_{v_0 v_2}^{f_0}$		$= \gamma_{5,131\frac{1}{4}}$	$= \gamma_{5,166\frac{2}{3}}$
$\text{computeOutputBound}(v_1, f_1) = (\alpha_{v_1}^{f_1})^* = \alpha_{v_1 v_2}^{f_1}$		FIFO_MUX	ARB_MUX
$\alpha_{v_1} = \alpha_{v_0 v_1}^{f_1}$		$= \gamma_{5,131\frac{1}{4}}$	$= \gamma_{5,166\frac{2}{3}}$
$\alpha_{v_1}^{x f_1}$		$= \gamma_{0,0}$	
$\beta_{v_1}^{l.o.f_1} = [\beta_{v_1} - \alpha_{v_1}^{x f_1}]^+$		$= \beta_{20,20}$	
$\alpha_{v_1 v_2}^{f_1} = \alpha_{v_1}^{f_1} \oslash \beta_{v_1}^{l.o.f_1} = \alpha^{f_1} \oslash \beta_{v_1}^{l.o.f_1}$	$r_{v_1 v_2}^{f_1}$	$= 5$	$= 5$
	$b_{v_1 v_2}^{f_1}$	$\alpha^{f_0}(T_{v_0}^{l.o.f_0}) = 231\frac{1}{4}$	$\alpha^{f_0}(T_{v_0}^{l.o.f_0}) = 266\frac{2}{3}$
	$=$	$= \gamma_{5,231\frac{1}{4}}$	$= \gamma_{5,266\frac{2}{3}}$

computeFifoOutputBound( $v_0, f_0$ ) = $(\alpha_{v_0}^{f_0})^* = \alpha_{v_0 v_2}^{f_0}$		FIFO_MUX	ARB_MUX
flow of interest $f_1$			
$\alpha_{v_0}^{f_0} = \alpha^{f_0}$		$= \gamma_{5,25}$	
$\alpha_{v_0}^{x f_0}$		$= \gamma_{0,0}$	
$\beta_{v_0}^{\text{SFA l.o. } f_0} = [\beta_{v_0} - \alpha_{v_0}^{x f_0}]^+$		$= \beta_{20,20}$	
$\alpha_{v_0 v_2}^{f_0} = \alpha^{f_0} \oslash \beta_{v_0}^{\text{l.o. } f_0}$	$r_{v_0 v_2}^{f_0}$	$= 5$	
	$b_{v_0 v_2}^{f_0}$	$\alpha^{f_0}(T_{v_0}^{\text{l.o. } f_0}) = 125$	
	$=$	$= \gamma_{5,125}$	

**Flow  $f_0$**

TFA		FIFO _MUX	ARB _MUX
$v_0$	$\alpha_{v_1} = \alpha_{v_0}^{f_0} + \alpha_{v_1}^{f_1}$	$= \gamma_{10,50}$	
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}$ $20 \cdot [t - 20]^+ = 50$ $t = 22\frac{1}{2}$	$\beta_{v_0} = \alpha_{v_0}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 50$ $t = 45$
	$B_{v_0}^{f_0}$	$\alpha_{v_0}(T_{v_0}) = 10 \cdot 20 + 50$ $= 250$	
$v_0 v_2$	$\alpha_{v_0 v_2} = \alpha_{v_0 v_2}^{f_0}$	$= \gamma_{5,131\frac{1}{4}}$	$= \gamma_{5,166\frac{2}{3}}$
$v_1 v_2$	$\alpha_{v_1 v_2} = \alpha_{v_1 v_2}^{f_1}$	$= \gamma_{5,231\frac{1}{4}}$	$= \gamma_{5,266\frac{2}{3}}$
$v_2$	$\alpha_{v_2} = \alpha_{v_0 v_2} + \alpha_{v_1 v_2}$	$= \gamma_{10,362\frac{1}{2}}$	
	$D_{v_2}^{f_0}$	$\beta_{v_2} = b_{v_2}$ $20 \cdot [t - 20]^+ = 362\frac{1}{2}$ $t = 38\frac{1}{8}$	$\beta_{v_2} = \alpha_{v_2}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 433\frac{1}{3}$ $t = 83\frac{1}{3}$
	$B_{v_2}^{f_0}$	$\alpha_{v_2}(T_{v_2}) = 10 \cdot 20 + 362\frac{1}{2}$ $= 562\frac{1}{2}$	
$D^{f_0}$		$= 60\frac{5}{8}$	$= 128\frac{1}{3}$
$B^{f_0}$		$\max_{i=\{0,2\}} b_{v_i}^{f_0} = 562\frac{1}{2}$	$\max_{i=\{0,2\}} b_{v_i}^{f_0} = 633\frac{1}{3}$

SFA FIFO\_MUX:

$$\begin{aligned}
\beta_{e2e}^{l.o.f_0} &= [\beta_{v_0}^{SFA \text{ l.o.}xf_0} - \alpha_{v_0}^{xf_0}]^+ \otimes [\beta_{v_2}^{SFA \text{ l.o.}xf_0} - \alpha_{v_2}^{xf_0}]^+ \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - \alpha_{v_1v_2}^{f_1}]^+ \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - (\alpha_{v_1}^{f_1} \oslash \beta_{v_1}^{l.o.f_1})]^+ \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - ((\alpha^{f_1} \oslash \beta_{v_0}^{SFA \text{ l.o.}f_1}) \oslash \beta_{v_1})]^+ \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - ((\alpha^{f_1} \oslash \beta_{v_0}) \oslash \beta_{v_1})]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes [\beta_{20,20} - ((\gamma_{5,25} \oslash \beta_{20,20}) \oslash \beta_{20,20})]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes [\beta_{20,20} - (\gamma_{5,125} \oslash \beta_{20,20})]^+ \\
&= \beta_{15,21\frac{1}{4}} \otimes [\beta_{20,20} - \gamma_{5,225}]^+ \\
&= \beta_{15,21\frac{1}{4}} \otimes \beta_{15,31\frac{1}{4}} \\
&= \beta_{15,52\frac{1}{2}}
\end{aligned}$$

$$\begin{aligned}
D^{f_1} &= \frac{R_{e2e}^{l.o.f_1} \cdot T_{e2e}^{l.o.f_1} + b^{f_1}}{R_{e2e}^{l.o.f_1}} \\
&= \frac{15 \cdot 52\frac{1}{2} + 25}{15} \\
&= 54\frac{1}{6}
\end{aligned}$$

$$\begin{aligned}
B^{f_1} &= \alpha^{f_1}(T_{e2e}^{l.o.f_1}) \\
&= 5 \cdot 52\frac{1}{2} + 25 \\
&= 287\frac{1}{2}
\end{aligned}$$

$$\begin{aligned}
\beta_{e2e}^{l.o.,f_0} &= [\beta_{v_0}^{SFA \text{ l.o.}xf_0} - \alpha_{v_0}^{xf_0}]^+ \otimes [\beta_{v_2}^{SFA \text{ l.o.}xf_0} - \alpha_{v_2}^{xf_0}]^+ \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - \alpha_{v_1v_2}^{f_1}]^+ \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - (\alpha_{v_1}^{f_1} \otimes \beta_{v_1}^{l.o.,f_1})]^+ \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - ((\alpha^{f_1} \otimes \beta_{v_0}^{l.o.,f_1}) \otimes \beta_{v_1})]^+ \text{ dnclib: not SFA l.o. because v0 is not the direct predecessor of v2 om the foi's path} \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - ((\alpha^{f_1} \otimes [\beta_{v_0} - \alpha^{f_0}]^+) \otimes \beta_{v_1})]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes [\beta_{20,20} - ((\gamma_{5,25} \otimes [\beta_{20,20} - \gamma_{5,25}]^+) \otimes \beta_{20,20})]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes [\beta_{20,20} - ((\gamma_{5,25} \otimes \beta_{20,21\frac{1}{4}}) \otimes \beta_{20,20})]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes [\beta_{20,20} - (\gamma_{5,131\frac{1}{4}} \otimes \beta_{20,20})]^+ \\
&= \beta_{15,21\frac{1}{4}} \otimes [\beta_{20,20} - \gamma_{5,231\frac{1}{4}}]^+ \\
&= \beta_{15,21\frac{1}{4}} \otimes \beta_{15,31\frac{9}{16}} \\
&= \beta_{15,52\frac{13}{16}}
\end{aligned}$$

$$\begin{aligned}
D^{f_1} &= \frac{R_{e2e}^{l.o.,f_1} \cdot T_{e2e}^{l.o.,f_1} + b^{f_1}}{R_{e2e}^{l.o.,f_1}} \\
&= \frac{15 \cdot 52\frac{13}{16} + 25}{15} \\
&= 54\frac{23}{48}
\end{aligned}$$

$$\begin{aligned}
B^{f_1} &= \alpha^{f_1}(T_{e2e}^{l.o.,f_1}) \\
&= 5 \cdot 52\frac{13}{16} + 25 \\
&= 289\frac{1}{16}
\end{aligned}$$

SFA, PMOO ARB\_MUX:

$$\begin{aligned}
\beta_{e2e}^{l.o.f_0} &= [\beta_{v_0}^{SFA \text{ l.o.}xf_0} - \alpha_{v_0}^{xf_0}]^+ \otimes [\beta_{v_2}^{SFA \text{ l.o.}xf_0} - \alpha_{v_2}^{xf_0}]^+ \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - \alpha_{v_1v_2}^{f_1}]^+ \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - (\alpha_{v_1}^{f_1} \oslash \beta_{v_1}^{l.o.f_1})]^+ \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - ((\alpha^{f_1} \oslash \beta_{v_0}^{SFA \text{ l.o.}f_1}) \oslash \beta_{v_1})]^+ \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - ((\alpha^{f_1} \oslash \beta_{v_0}) \oslash \beta_{v_1})]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes [\beta_{20,20} - ((\gamma_{5,25} \oslash \beta_{20,20}) \oslash \beta_{20,20})]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes [\beta_{20,20} - (\gamma_{5,125} \oslash \beta_{20,20})]^+ \\
&= \beta_{15,28\frac{1}{3}} \otimes [\beta_{20,20} - \gamma_{5,225}]^+ \\
&= \beta_{15,28\frac{1}{3}} \otimes \beta_{15,41\frac{2}{3}} \\
&= \beta_{15,70}
\end{aligned}$$

$$\begin{aligned}
D^{f_1} &= \frac{R_{e2e}^{l.o.f_1} \cdot T_{e2e}^{l.o.f_1} + b^{f_1}}{R_{e2e}^{l.o.f_1}} \\
&= \frac{15 \cdot 70 + 25}{15} \\
&= 71\frac{2}{3}
\end{aligned}$$

$$\begin{aligned}
B^{f_1} &= \alpha^{f_1}(T_{e2e}^{l.o.f_1}) \\
&= 5 \cdot 70 + 25 \\
&= 375
\end{aligned}$$

$$\begin{aligned}
\beta_{e2e}^{l.o.,f_0} &= [\beta_{v_0}^{SFA \text{ l.o.}xf_0} - \alpha_{v_0}^{xf_0}]^+ \otimes [\beta_{v_2}^{SFA \text{ l.o.}xf_0} - \alpha_{v_2}^{xf_0}]^+ \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - \alpha_{v_1v_2}^{f_1}]^+ \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - (\alpha_{v_1}^{f_1} \otimes \beta_{v_1}^{l.o.,f_1})]^+ \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - ((\alpha^{f_1} \otimes \beta_{v_0}^{l.o.,f_1}) \otimes \beta_{v_1})]^+ \text{ dnclib: not SFA l.o. because v0 is not the direct predecessor of v2 om the foi's path} \\
&= [\beta_{v_0} - \alpha^{f_1}]^+ \otimes [\beta_{v_2} - ((\alpha^{f_1} \otimes [\beta_{v_0} - \alpha^{f_0}]^+) \otimes \beta_{v_1})]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes [\beta_{20,20} - ((\gamma_{5,25} \otimes [\beta_{20,20} - \gamma_{5,25}]^+) \otimes \beta_{20,20})]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes [\beta_{20,20} - ((\gamma_{5,25} \otimes \beta_{20,28\frac{1}{3}}) \otimes \beta_{20,20})]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes [\beta_{20,20} - (\gamma_{5,166\frac{2}{3}} \otimes \beta_{20,20})]^+ \\
&= \beta_{15,28\frac{1}{3}} \otimes [\beta_{20,20} - \gamma_{5,266\frac{2}{3}}]^+ \\
&= \beta_{15,28\frac{1}{3}} \otimes \beta_{15,44\frac{4}{9}} \\
&= \beta_{15,72\frac{7}{9}}
\end{aligned}$$

$$\begin{aligned}
D^{f_1} &= \frac{R_{e2e}^{l.o.,f_1} \cdot T_{e2e}^{l.o.,f_1} + b^{f_1}}{R_{e2e}^{l.o.,f_1}} \\
&= \frac{15 \cdot 72\frac{7}{9} + 25}{15} \\
&= 74\frac{4}{9}
\end{aligned}$$

$$\begin{aligned}
B^{f_1} &= \alpha^{f_1}(T_{e2e}^{l.o.,f_1}) \\
&= 5 \cdot 72\frac{7}{9} + 25 \\
&= 388\frac{8}{9}
\end{aligned}$$

**Flow  $f_1$**

TFA		FIFO _MUX	ARB _MUX
$v_0$	$\alpha_{v_1} = \alpha_{v_0}^{f_0} + \alpha_{v_1}^{f_1}$	$= \gamma_{10,50}$	
	$D_{v_0}^{f_0}$	$\beta_{v_0} = b_{v_0}$ $20 \cdot [t - 20]^+ = 50$ $t = 22\frac{1}{2}$	$\beta_{v_0} = \alpha_{v_0}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 50$ $t = 45$
	$B_{v_0}^{f_0}$	$\alpha_{v_0}(T_{v_0}) = 10 \cdot 20 + 50$ $= 250$	
$v_0 v_1$	$\alpha_{v_0 v_1} = \alpha_{v_0 v_1}^{f_1}$	$= \gamma_{5,131\frac{1}{4}}$	$= \gamma_{5,166\frac{2}{3}}$
$v_1$	$\alpha_{v_1} = \alpha_{v_0 v_1}^{f_1}$	$= \gamma_{5,131\frac{1}{4}}$	$= \gamma_{5,166\frac{2}{3}}$
	$D_{v_1}^{f_1}$	$\beta_{v_1} = b_{v_1}$ $20 \cdot [t - 20]^+ = 131\frac{1}{4}$ $t = 26\frac{9}{16}$	FIFO per micro flow $\beta_{v_1} = b_{v_1}$ $20 \cdot [t - 20]^+ = 166\frac{2}{3}$ $t = 28\frac{1}{3}$
	$B_{v_1}^{f_1}$	$\alpha_{v_1}(T_{v_1}) = 5 \cdot 20 + 131\frac{1}{4}$ $= 231\frac{1}{4}$	$\alpha_{v_1}(T_{v_1}) = 5 \cdot 20 + 166\frac{2}{3}$ $= 266\frac{2}{3}$
$v_0 v_2$	$\alpha_{v_0 v_2} = \alpha_{v_0 v_2}^{f_0}$	$= \gamma_{5,131\frac{1}{4}}$	$= \gamma_{5,166\frac{2}{3}}$
$v_1 v_2$	$\alpha_{v_1 v_2} = \alpha_{v_1 v_2}^{f_1}$	$= \gamma_{5,231\frac{1}{4}}$	$= \gamma_{5,266\frac{2}{3}}$
$v_2$	$\alpha_{v_2} = \alpha_{v_0 v_2} + \alpha_{v_1 v_2}$	$= \gamma_{10,362\frac{1}{2}}$	$= \gamma_{10,433\frac{1}{3}}$
	$D_{v_2}^{f_1}$	$\beta_{v_2} = b_{v_2}$ $20 \cdot [t - 20]^+ = 362\frac{1}{2}$ $t = 38\frac{1}{8}$	$\beta_{v_2} = \alpha_{v_2}$ $20 \cdot [t - 20]^+ = 10 \cdot t + 433\frac{1}{3}$ $t = 83\frac{1}{3}$
	$B_{v_2}^{f_1}$	$\alpha_{v_2}(T_{v_2}) = 10 \cdot 20 + 362\frac{1}{2}$ $= 562\frac{1}{2}$	$\alpha_{v_2}(T_{v_2}) = 10 \cdot 20 + 433\frac{1}{3}$ $= 633\frac{1}{3}$
$D^{f_1}$		$\sum_{i=0}^2 \beta_{v_i}^{f_1} = 87\frac{3}{16}$	$\sum_{i=0}^2 \beta_{v_i}^{f_1} = 156\frac{2}{3}$
$B^{f_1}$		$\max_{i=0}^2 b_{v_i}^{f_1} = 562\frac{1}{2}$	$\max_{i=0}^2 b_{v_i}^{f_1} = 633\frac{1}{3}$



SFA FIFO\_MUX:

$$\begin{aligned}
\beta_{\text{e2e}}^{\text{l.o.},f_1} &= [\beta_{v_0}^{\text{SFA l.o.},xf_1} - \alpha_{v_0}^{xf_1}]^+ \otimes [\beta_{v_1}^{\text{SFA l.o.},xf_1} - \alpha_{v_1}^{xf_1}]^+ \otimes [\beta_{v_2}^{\text{SFA l.o.},xf_1} - \alpha_{v_2}^{xf_1}]^+ \\
&= [\beta_{v_0} - \alpha^{f_0}]^+ \otimes \beta_{v_1} \otimes [\beta_{v_2} - \alpha_{v_0 v_2}^{f_0}]^+ \\
&= [\beta_{v_0} - \alpha^{f_0}]^+ \otimes \beta_{v_1} \otimes [\beta_{v_2} - (\alpha_{v_0}^{f_0} \odot \beta_{v_0}^{\text{SFA l.o.},xf_1})]^+ \\
&= [\beta_{v_0} - \alpha^{f_0}]^+ \otimes \beta_{v_1} \otimes [\beta_{v_2} - (\alpha^{f_0} \odot \beta_{v_0})]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes \beta_{20,20} \otimes [\beta_{20,20} - (\gamma_{5,25} \odot \beta_{20,20})]^+ \\
&= \beta_{15,21\frac{1}{4}} \otimes \beta_{20,20} \otimes [\beta_{20,20} - \gamma_{5,125}]^+ \\
&= \beta_{15,21\frac{1}{4}} \otimes \beta_{20,20} \otimes \beta_{15,26\frac{1}{4}} \\
&= \beta_{15,67\frac{1}{2}}
\end{aligned}$$

$$\begin{aligned}
D^{f_1} &= \frac{R_{\text{e2e}}^{\text{l.o.},f_1} \cdot T_{\text{e2e}}^{\text{l.o.},f_1} + b^{f_1}}{R_{\text{e2e}}^{\text{l.o.},f_1}} \\
&= \frac{15 \cdot 67\frac{1}{2} + 25}{15} \\
&= 69\frac{1}{6}
\end{aligned}$$

$$\begin{aligned}
B^{f_1} &= \alpha^{f_1}(T_{\text{e2e}}^{\text{l.o.},f_1}) \\
&= 5 \cdot 67\frac{1}{2} + 25 \\
&= 362\frac{1}{2}
\end{aligned}$$

$$\begin{aligned}
\beta_{e2e}^{l.o.f_1} &= [\beta_{v_0}^{SFA \text{ l.o.}xf_1} - \alpha_{v_0}^{xf_1}]^+ \otimes [\beta_{v_1}^{SFA \text{ l.o.}xf_1} - \alpha_{v_1}^{xf_1}]^+ \otimes [\beta_{v_2}^{SFA \text{ l.o.}xf_1} - \alpha_{v_2}^{xf_1}]^+ \\
&= [\beta_{v_0} - \alpha^{f_0}]^+ \otimes \beta_{v_1} \otimes [\beta_{v_2} - \alpha_{v_0v_2}^{f_0}]^+ \\
&= [\beta_{v_0} - \alpha^{f_0}]^+ \otimes \beta_{v_1} \otimes [\beta_{v_2} - (\alpha_{v_0}^{f_0} \odot \beta_{v_0}^{l.o.xf_1})]^+ \text{ dnclib: not SFA l.o. because v0 is not the direct predecessor of v2 om the foi's path} \\
&= [\beta_{v_0} - \alpha^{f_0}]^+ \otimes \beta_{v_1} \otimes [\beta_{v_2} - (\alpha^{f_0} \odot [\beta_{v_0} - \alpha^{f_1}]^+)]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes \beta_{20,20} \otimes [\beta_{20,20} - (\gamma_{5,25} \odot [\beta_{20,20} - \gamma_{5,25}]^+)]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes \beta_{20,20} \otimes [\beta_{20,20} - (\gamma_{5,25} \odot \beta_{15,21\frac{1}{4}})]^+ \\
&= \beta_{15,21\frac{1}{4}} \otimes \beta_{20,20} \otimes [\beta_{20,20} - \gamma_{5,131\frac{1}{4}}]^+ \\
&= \beta_{15,21\frac{1}{4}} \otimes \beta_{20,20} \otimes \beta_{15,26\frac{9}{16}} \\
&= \beta_{15,67\frac{13}{16}}
\end{aligned}$$

$$\begin{aligned}
D^{f_1} &= \frac{R_{e2e}^{l.o.f_1} \cdot T_{e2e}^{l.o.f_1} + b^{f_1}}{R_{e2e}^{l.o.f_1}} \\
&= \frac{15 \cdot 67\frac{13}{16} + 25}{15} \\
&= 69\frac{23}{48}
\end{aligned}$$

$$\begin{aligned}
B^{f_1} &= \alpha^{f_1}(T_{e2e}^{l.o.f_1}) \\
&= 5 \cdot 67\frac{13}{16} + 25 \\
&= 364\frac{1}{16}
\end{aligned}$$

SFA, PMOO ARB\_MUX:

$$\begin{aligned}
\beta_{\text{e2e}}^{\text{l.o.},f_1} &= [\beta_{v_0}^{\text{SFA l.o.},xf_1} - \alpha_{v_0}^{xf_1}]^+ \otimes [\beta_{v_1}^{\text{SFA l.o.},xf_1} - \alpha_{v_1}^{xf_1}]^+ \otimes [\beta_{v_2}^{\text{SFA l.o.},xf_1} - \alpha_{v_2}^{xf_1}]^+ \\
&= [\beta_{v_0} - \alpha^{f_0}]^+ \otimes \beta_{v_1} \otimes [\beta_{v_2} - \alpha_{v_0 v_2}^{f_0}]^+ \\
&= [\beta_{v_0} - \alpha^{f_0}]^+ \otimes \beta_{v_1} \otimes [\beta_{v_2} - (\alpha_{v_0}^{f_0} \otimes \beta_{v_0}^{\text{SFA l.o.},xf_1})]^+ \\
&= [\beta_{v_0} - \alpha^{f_0}]^+ \otimes \beta_{v_1} \otimes [\beta_{v_2} - (\alpha^{f_0} \otimes \beta_{v_0})]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes \beta_{20,20} \otimes [\beta_{20,20} - (\gamma_{5,25} \otimes \beta_{20,20})]^+ \\
&= \beta_{15,28\frac{1}{3}} \otimes \beta_{20,20} \otimes [\beta_{20,20} - \gamma_{5,125}]^+ \\
&= \beta_{15,28\frac{1}{3}} \otimes \beta_{20,20} \otimes \beta_{15,35} \\
&= \beta_{15,83\frac{1}{3}}
\end{aligned}$$

$$\begin{aligned}
D^{f_1} &= \frac{R_{\text{e2e}}^{\text{l.o.},f_1} \cdot T_{\text{e2e}}^{\text{l.o.},f_1} + b^{f_1}}{R_{\text{e2e}}^{\text{l.o.},f_1}} \\
&= \frac{15 \cdot 83\frac{1}{3} + 25}{15} \\
&= 85
\end{aligned}$$

$$\begin{aligned}
B^{f_1} &= \alpha^{f_1}(T_{\text{e2e}}^{\text{l.o.},f_1}) \\
&= 5 \cdot 83\frac{1}{3} + 25 \\
&= 441\frac{2}{3}
\end{aligned}$$

$$\begin{aligned}
\beta_{e2e}^{l.o.f_1} &= [\beta_{v_0}^{SFA \text{ l.o.}xf_1} - \alpha_{v_0}^{xf_1}]^+ \otimes [\beta_{v_1}^{SFA \text{ l.o.}xf_1} - \alpha_{v_1}^{xf_1}]^+ \otimes [\beta_{v_2}^{SFA \text{ l.o.}xf_1} - \alpha_{v_2}^{xf_1}]^+ \\
&= [\beta_{v_0} - \alpha^{f_0}]^+ \otimes \beta_{v_1} \otimes [\beta_{v_2} - \alpha_{v_0v_2}^{f_0}]^+ \\
&= [\beta_{v_0} - \alpha^{f_0}]^+ \otimes \beta_{v_1} \otimes [\beta_{v_2} - (\alpha_{v_0}^{f_0} \odot \beta_{v_0}^{l.o.xf_1})]^+ \text{ dnclib: not SFA l.o. because v0 is not the direct predecessor of v2 om the foi's path} \\
&= [\beta_{v_0} - \alpha^{f_0}]^+ \otimes \beta_{v_1} \otimes [\beta_{v_2} - (\alpha^{f_0} \odot [\beta_{v_0} - \alpha^{f_1}]^+)]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes \beta_{20,20} \otimes [\beta_{20,20} - (\gamma_{5,25} \odot [\beta_{20,20} - \gamma_{5,25}]^+)]^+ \\
&= [\beta_{20,20} - \gamma_{5,25}]^+ \otimes \beta_{20,20} \otimes [\beta_{20,20} - (\gamma_{5,25} \odot \beta_{15,28\frac{1}{3}})]^+ \\
&= \beta_{15,28\frac{1}{3}} \otimes \beta_{20,20} \otimes [\beta_{20,20} - \gamma_{5,166\frac{2}{3}}]^+ \\
&= \beta_{15,28\frac{1}{3}} \otimes \beta_{20,20} \otimes \beta_{15,37\frac{7}{9}} \\
&= \beta_{15,86\frac{1}{9}}
\end{aligned}$$

$$\begin{aligned}
D^{f_1} &= \frac{R_{e2e}^{l.o.f_1} \cdot T_{e2e}^{l.o.f_1} + b^{f_1}}{R_{e2e}^{l.o.f_1}} \\
&= \frac{15 \cdot 86\frac{1}{9} + 25}{15} \\
&= 87\frac{7}{9}
\end{aligned}$$

$$\begin{aligned}
B^{f_1} &= \alpha^{f_1}(T_{e2e}^{l.o.f_1}) \\
&= 5 \cdot 86\frac{1}{9} + 25 \\
&= 455\frac{5}{9}
\end{aligned}$$